

# OVERVIEW OF OCEAN AND SEA ICE MODELLING

by

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*Lack of sufficient data collection and thereby general limitation regarding reliable descriptive analyses of the ocean inhibit satisfactory knowledge of the state and variable of the ocean.*

*In order to advance our understanding, provide forecasts and implement proper management system one need to find a compromise between observation requirements, actual data availability and mathematical model tools. This is also called optimal control problem (theory).*

**OCEAN AND SEA ICE MODELLING IS CAPITALIZING  
ON THIS**

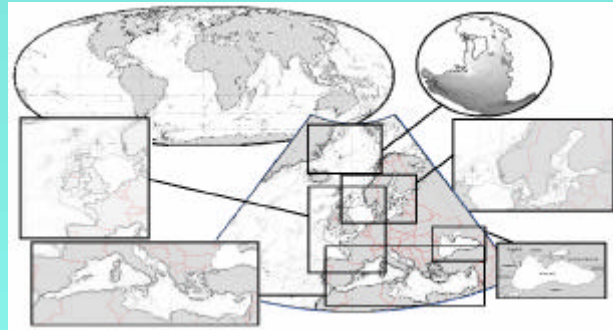
# ***CONTENT***

- ***Introduction***
- ***Typical temporal and spatial scales***
- ***Classical models***
- ***European Data Assimilation Systems***
- ***Need for improvements***
- ***References***

## *Modeling of the marine environment are characterized by:*

- *dimensions in physical space ( $\underline{X} - t$ );*
- *number of state variables - hydrodynamic, chemical, bio-geochemical;*
- *vertical coordinate system*
- *surface treatment (rigid lid, free surface)*
- *parameterization of vertical and horizontal diffusion (mixing in local models versus bulk models)*
- *geographical coverage, time period, specific events or processes;*
- *grid type (rectilinear, curvilinear orthogonal, curvilinear non-orthogonal);*
- *numerical method; finite difference (use squares) or finite element (use triangles)*
- *numerical scheme and choice of time discretization; explicit, implicit, semi-implicit*
- *numerical consistent scheme and stable scheme.*

*In physical space one can distinguish between local, regional and global models. Within each class the marine system can have distinct length-scales and time-scales. In fact length and time scales are somewhat coupled according to particular phenomenon (i.e. El Nino, tide, storm surges, etc). This constraints the choice of model resolution.*



*(after MERSEA*

*IP)*

*The model accuracy (or reliability) depends on the resolution, precisions of the calculations, and quality of the data used to determine parameters and boundary conditions. Models also need accurate bathymetry at the adequate resolution in order to properly account for topographic steering.*

*The models are commonly forced by atmospheric fields including surface wind vector (wind stress and input of turbulent energy) and fluxes of heat (radiative, sensible and latent) directly taken from atmospheric models.*

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## *Time-space characteristics*

Time scale	Frequency (s <sup>-1</sup> )	<u>Spectral windows</u> (highlighted processes)	<u>Smaller scale fluctuations</u> (filtered out processes)
1 s	1	<u>Microscale processes</u> 3 D "eddy" turbulence (+ surface waves)	Molecular diffusion
1 m	10 <sup>-2</sup>	<u>Mesialscale processes</u> Internal wave s Vertical microstructure Inhibited "bliny"* turbulence	Eddy turbulence
1 h	10 <sup>-4</sup>	<u>Mesoscale processes</u> Inertial oscillations	"Bliny turbulence"
1 d	10 <sup>-5</sup>	Tides, storm surges Diurnal variations	

## *Time-space characteristics*

Time scale	Frequency (s <sup>-1</sup> )	Spectral windows (highlighted processes)	Smaller scale fluctuations (filtered out processes)
1 w	10 <sup>-6</sup>	<u>Synop tiscal e proce sses</u> Fron tal currents Meande rs, "rossby"* turbul ence	Meso scale var iab ilit y
1 mon th	10 <sup>-7</sup>	<u>Sea sonal scale proce sses</u>	"Rossby turbul ence"
1 yea r	10 <sup>-8</sup>	<u>Globa l scale proc esses</u> Clim atic proces ses  <u>(Paleo) clim aticscale proces ses</u>	Sea sonal va riab ilit y

# Model dimensions in space and time

- 1 D; simple model chosen to simulate vertical structure, mixed layer dynamics including importance of turbulent mixing
- 2 D; depth integrated barotropic models (constant density in space/time are common for tides and storm surges modelling, and shallow water modelling)
- 3 D; depth resolving baroclinic models for variable vertical density

## Discretization of the continuity equation and equation of motion

$$\frac{\partial r}{\partial t} + \nabla \cdot r \underline{u} = 0 \quad \text{continuity equation}$$

$$\frac{d\underline{u}}{dt} = - \frac{1}{r} \cdot \nabla p - 2\underline{\omega} \times \underline{u} + \underline{g} + \underline{F} \quad \text{momentum equation}$$

pressure
Coriolis
gravity
other forces

2nd ENVISAT Summer School, ESA ESRIIN, 10-14 April 2004 (friction, tides,..)



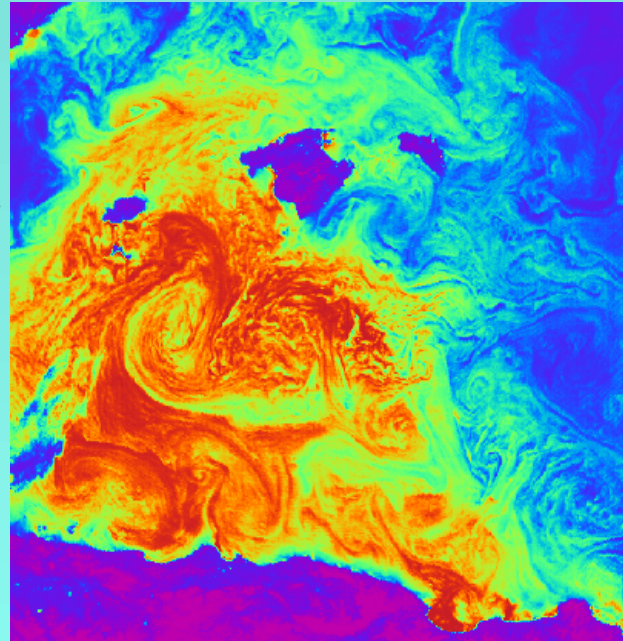


## *Some fundamental hydrodynamic quantities*

- *Rossby radius of deformation;*

$$R_d = (g h D\rho/\rho)^{1/2} / f$$

*typical horizontal scale of the weather in the ocean; defines the length scale at which rotation effects (scaled by Coriolis parameter  $f$ ) become as important as buoyancy effects determined by  $D\rho/\rho$*



- *Brunt-Vaisala frequency  $N$ ; the measure of the stratification or vertical gradient in density (buoyancy)*

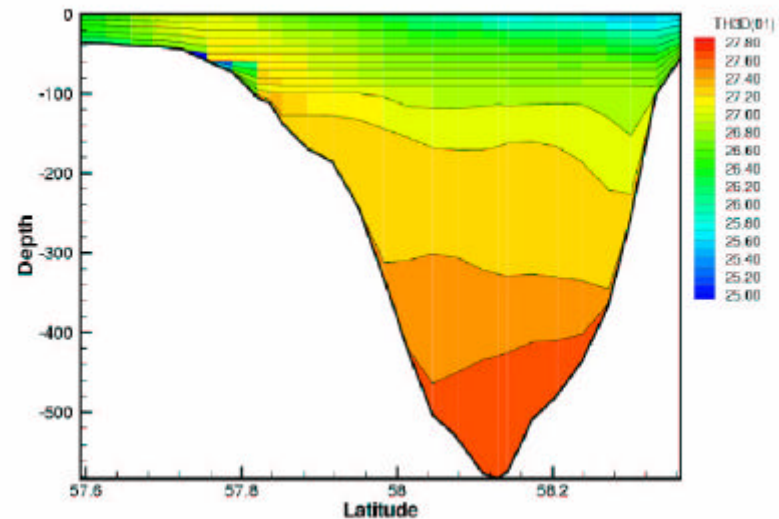
$$N^2 = g (- \rho / \rho dz)$$

## *choice of vertical coordinate system*

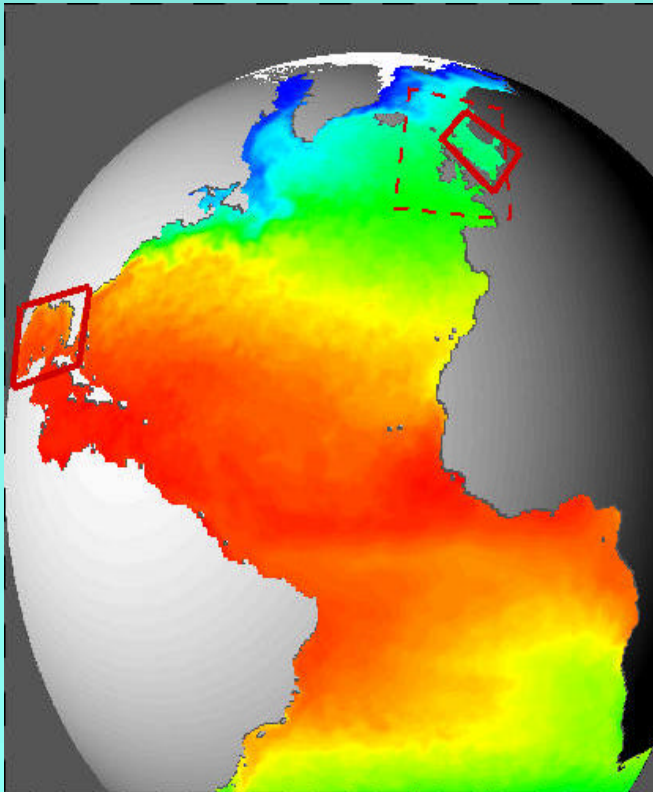
- *z level; discretization in the vertical at fixed depth values - level models*
- *isopycnal; a fixed number of layers with constant density*
- *sigma; a bathymetry following coordinate system in shallow water*

**LAYER  
MODELS**

***HYCOM: Hybrid coordinate ocean model (Bleck et al., 2002)-Combines all 3 coordinate systems; z-level for mixed layer representation, isopycnic for the interior ocean density, sigma for shallow water terrain following coordinates.***

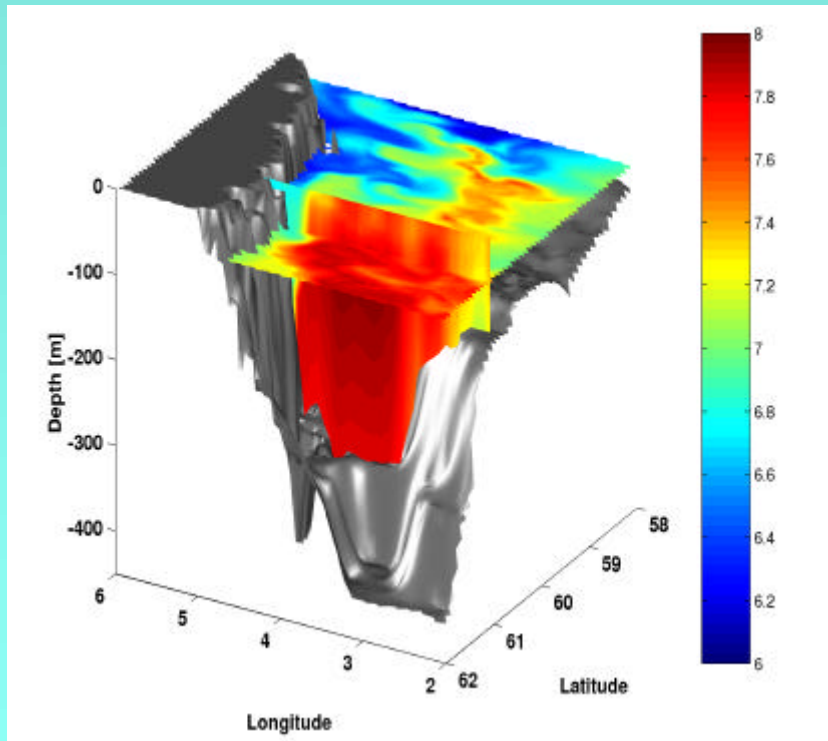


# *OCEAN MODELLING*



Models run at a global to basin scale are used to represent circulation of large oceanic water masses, whereas at a 'nested' regional or local scale with higher spatial resolution they provide finer detail, for example where eddy resolution is required. A nested model means that a high resolution regional model receives boundary conditions from an outer model with lower resolution. In this way one can insure proper representation of the general circulation into the regional area.

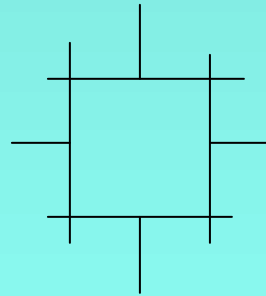
# *OCEAN MODELLING*



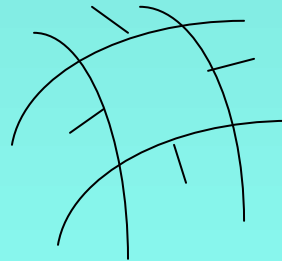
Ocean characteristics such as temperature, salinity and current velocity can be estimated in space and time by computer model simulation across a numerical ocean model grid. This means that one can get a fully 3-dimensional image of the ocean. Models can operate in hindcast mode to simulate historical time series of past conditions, and also in nowcast and forecast mode for operational applications.

# *Grid Type*

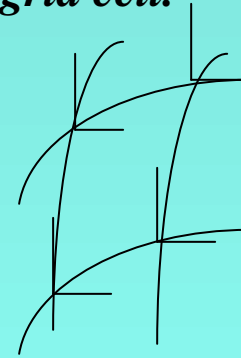
*Satellite observations are usually slightly more favorable than in-situ point observations regarding representation in a grid cell.*



*Rectilinear or Spherical (RS)*

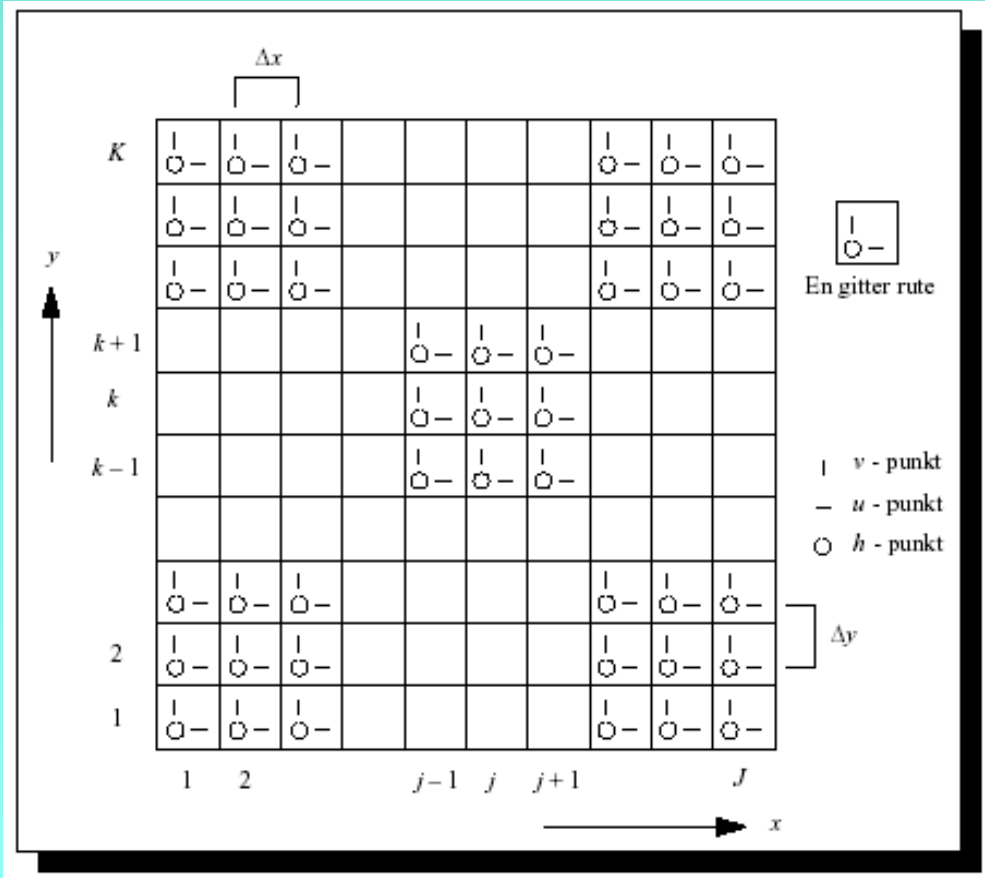


*Curvilinear Orthogonal (CO)*



*Curvilinear Non-orthogonal (NO)*

## Example of Arakawa C-grid



$h$ : pressure,  
temperature, salinity,  
sea level

$u$ :  $x$ -velocity

$v$ :  $y$ -velocity

*This is a so-called  
staggered grid with one  
grid-interval between  
variables  $h, u, v$  but  
where the latter two are  
shifted half a grid  
interval from  $h$ .*

*Ease the computations  
of  
pressure gradient cont.  
to velocity field.*

***Explicit scheme - only expressions at earlier time step  $n$  at right hand side***

$$\frac{u_j^{n+1} - u_j^n}{\Delta t} = \kappa \frac{u_{j-1}^n - 2u_j^n + u_{j+1}^n}{\Delta x^2}, \quad j = 2(1)J, \quad n = 0(1)N$$

***Implicit scheme - time step  $n+1$  also at right hand side***

$$u_j^{n+1} = u_j^{n-1} + \kappa \frac{2\Delta t}{\Delta x^2} (u_{j-1}^{n+1} - 2u_j^{n+1} + u_{j+1}^{n+1}); \quad j = 2(1)J, \quad n = 0(1)\dots$$

***Semi -implicit scheme - combines explicit and implicit schemes***

# ***SOME CLASSICAL OCEAN MODELS***

Authors	Identifier	Vertical Grid	Horizontal Grid	Vertical Diffusivity	Horizontal Diffusivity	Surface	System
Blumberg-Mellor	POM	$\sigma - C$	CO/C	TC or CVD	Smag or CHD	Free	
Bryan-Cox-Semtner	BCS	$z - C$	RS/B	RND/CA <sup>1</sup>	CHD	rigid	FOAM
Haidvogel	SPEM	$\sigma - C$ Spec	CO/C	BML	BiH	rigid	
R. Bleck et al.	MICOM	Iso- pycnic	CO	Bulk mixed layer	CHD	free	
Oberhuber	OBH	$\rho - C$	RS/B	BML	Smag	free	MICOM
R. Bleck	HYCOM	hybrid		KPP		free	TOPAZ
G. Madec	OPA	Z - C		TKE closure		rigid	MERCATOR



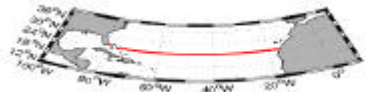
## Four european ocean data assimilation system

<b>MERCATOR FR</b>	<p><b>OPA</b> -Z coord./Rigid Lid</p> <p>-Simple thermo. ice model -<b>SPIN UP 15days</b> -TKE</p>	<p>-horiz. 1/15° (5-7km) <b>43 levels</b></p> <p>-Atl+Med from 10 to 70°N. -Relaxation to Medatlas (T.S) in Gulf of Cadiz below 500m</p>	<p>-Daily <b>ECMWF forcing</b></p> <p>-Relaxation to Reynolds SST and Reynaud SSS -Monthly river runoff -Data assimilation stopped at depth 500m</p>	<p>-<b>OI SOFA</b> -<b>SLA along track</b> (Jason1,ERS2/Envisat,GFO) once a week</p> <p>-MSSH from Rio et al.(data) in the Atlantic and blend of previous runs in MED</p>	<b>ATL MED</b>
<b>TOPAZ NO</b>	<p><b>HYCOM</b> -Hybrid coord/Free surface</p> <p>-dyn./thermodynamic sea ice -<b>SPIN UP 20years</b> -KPP mixing</p>	<p>-horiz. 20 to 30km <b>22 hybrid layers</b></p> <p>-Arctic+Atlantic till 40°S. Closed boundary without relaxation. No med basin.</p>	<p>-6 hourly <b>ECMWF forcing (Bulk formulae momentum&amp;heat)</b></p> <p>-Precip Clim+ Relaxation to Levitus SSS(60days) -No river runoff -Data assimilation stopped at depth 300m</p>	<p>-<b>EnKF</b></p> <p>-<b>SLA Maps</b>(SALTO-DUACS) once a week -<b>SST</b> from CLS AVHRR data once a week -<b>Maps of ice concentration</b></p> <p>-MSSH from OCCAM run</p>	<b>ATL</b>
<b>FOAM UK</b>	<p><b>HADLEY CENTRE</b> -Z coord./Rigid Lid</p> <p>-dyn./thermodynamic sea ice -<b>SPIN UP 5months</b> -Kraus-Turner</p>	<p>-horiz. 1/9° (12km) <b>20 levels</b></p> <p>-Atl+Med from 10 to 70°N. -No relaxation to Med Water</p>	<p>-6 Hourly <b>NWP-MetOffice forcing</b></p> <p>-Weak relaxation to Levitus SST and SSS. -No river runoff -Data assimilation stopped at depth 300m</p>	<p>-<b>OI Cooper&amp;Haines</b> -<b>SLA along track</b> (Jason1,GFO,Envisat) -<b>SST 2.5° gridded</b> (ARGO)Once a day. -<b>T+S profiles</b> at all depths -<b>gridded ice concentration</b> -MSSH from previous run</p>	<b>ATL MED</b>
<b>MFS IT</b>	<p><b>MOM</b> -Z coord./Rigid Lid</p> <p>-no ice model -<b>SPIN UP:7years</b> -cst vertical mixing+vertical adjustment</p>	<p>-horiz. 1/8° <b>31 levels</b></p> <p>- Med only -Transport through Gibraltar parameterized</p>	<p>-6 Hourly <b>ECMWF forcing (Bulk formulae momentum &amp; heat)</b></p> <p>-relaxation to satellite night time SST and SSS climato -No river runoff -Data assimilation stopped at depth 1000m</p>	<p>-<b>OI SOFA</b> -<b>SLA along track</b> (SALTO-DUACS) once a week -1/8° 1/8° <b>SST analysis mean maps</b> once a week -<b>T profiles</b> to 500m -MSSH from previous run with 1993-99 forcing.</p>	<b>MED</b>



# Zonal Section 26 26°N Salinity

WOCE A05 JUL AUG 1992



WOCE A01 JAN FEB 1998

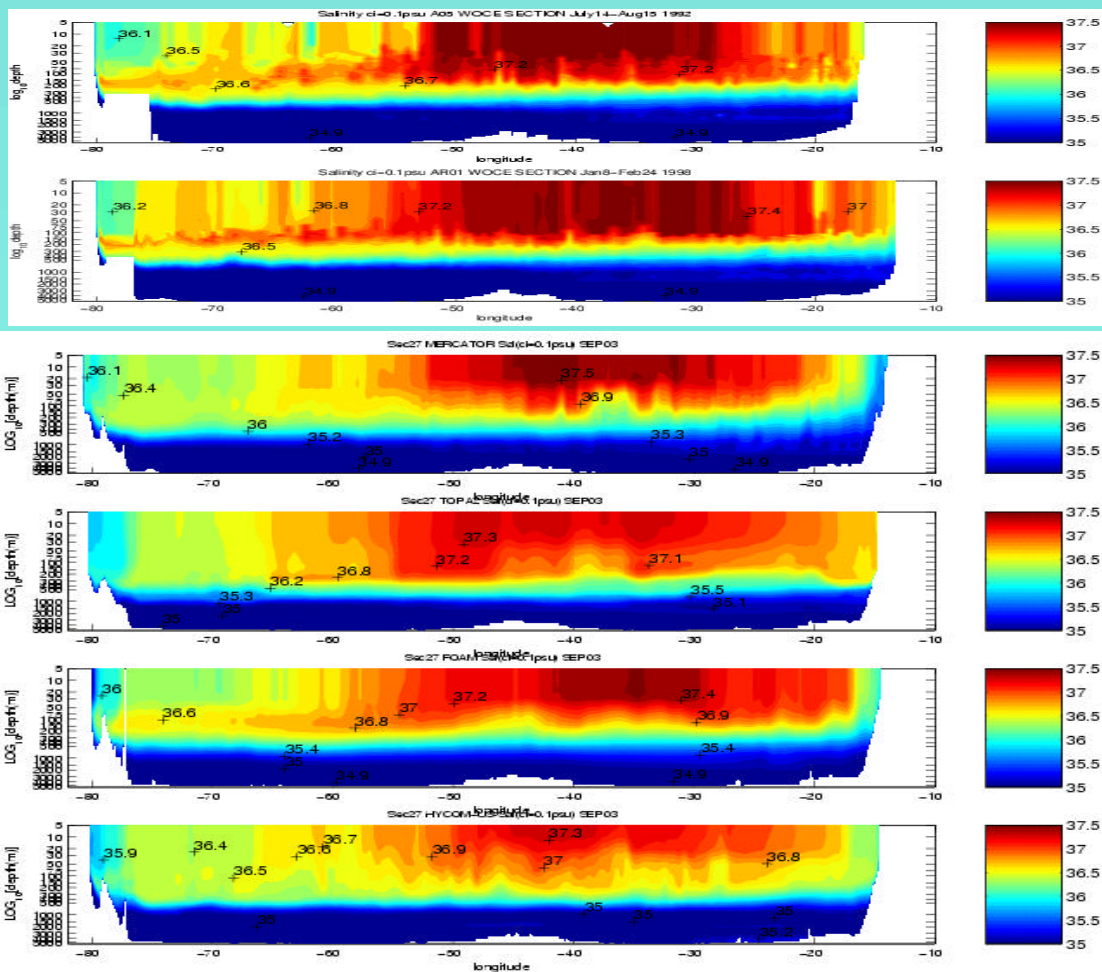


MERCATOR

TOPAZ

FOAM

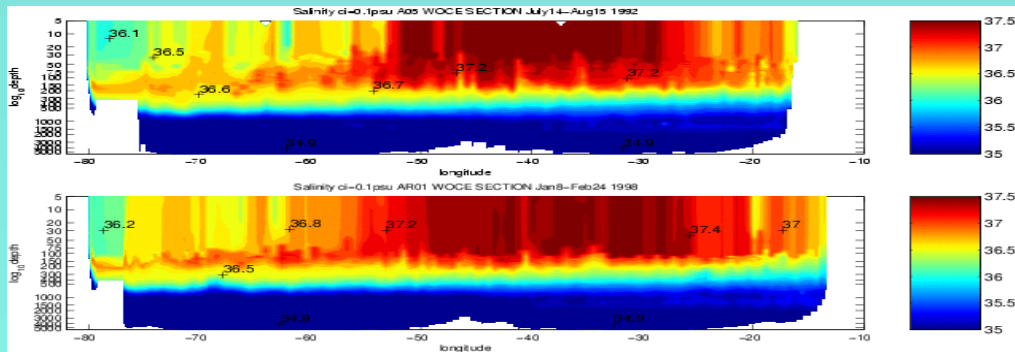
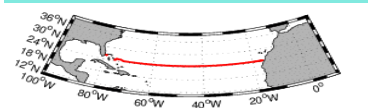
HYCOM



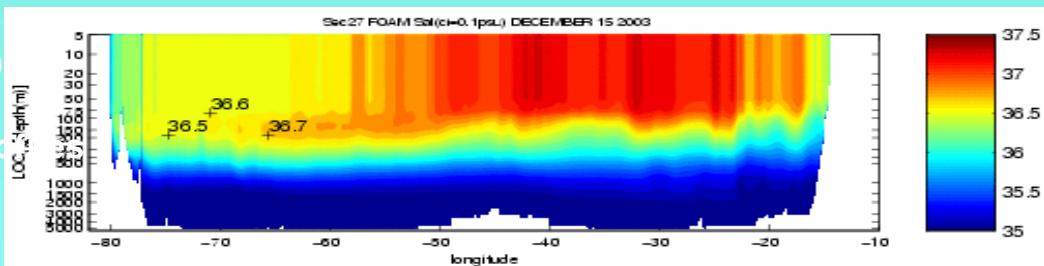
# IMPACT OF ASSIMILATION OF ARGO SALINITY PROFILE

Class2 Zonal Section 26°N Salinity

WOCE

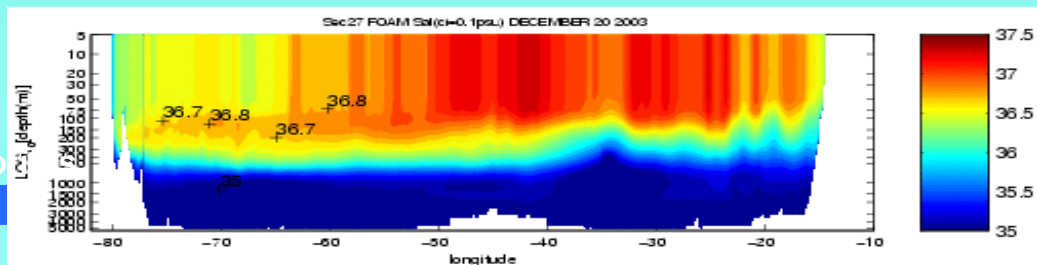


FOAM (DEC15 2003)  
Before assimilation  
of ARGO salinity profiles



assimilation of ARGO salinity profiles from DEC17 2003 on

FOAM (DEC20 2003)  
After assimilation  
of ARGO salinity profiles



IERSC/lhp

## *Ice models characteristics*

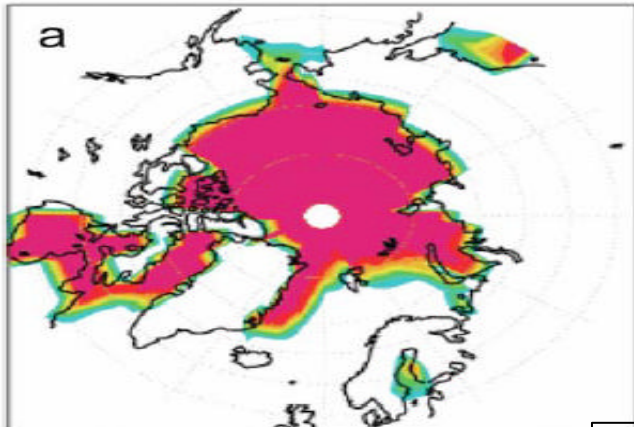
- *define the ice concentration variable  $A$  as the fractional cover; i.e.  $0 < A < 1$ ;*
- *$h$  is the local ice thickness and  $h_I$  is the average thickness over the ice covered region;*
- *ice thickness distribution  $g(h)$ ;*
- *slab models - the vertical structure in the ice is neglected;*
- *ice rheology that parameterize internal ice stresses (plastic, elastic, viscos,  $pev$ ,  $ev$ ,  $pe$ );*
- *fluxes - melt rate on top, freeze rate at ice-ocean interface, freeze rate in open water, rate of frazil ice growth in column;*
- *snow-sea ice system - strong effect on albedo*



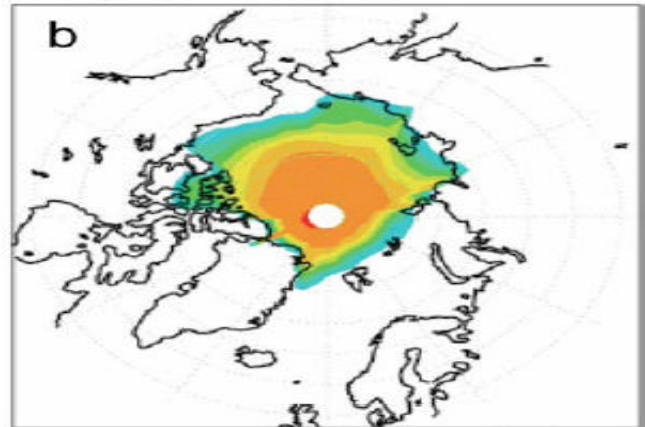
*COURTECY KWOK*

QuickTime™ og en  
GIF-dekomprimerer  
kreves for å se dette bildet.

Mar 2001–2010

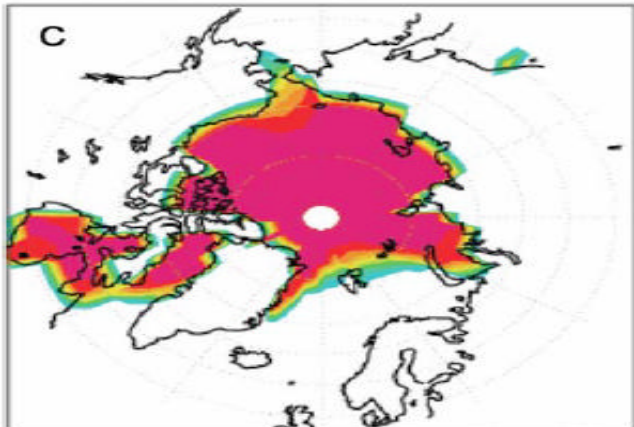


Sep 2001–2010

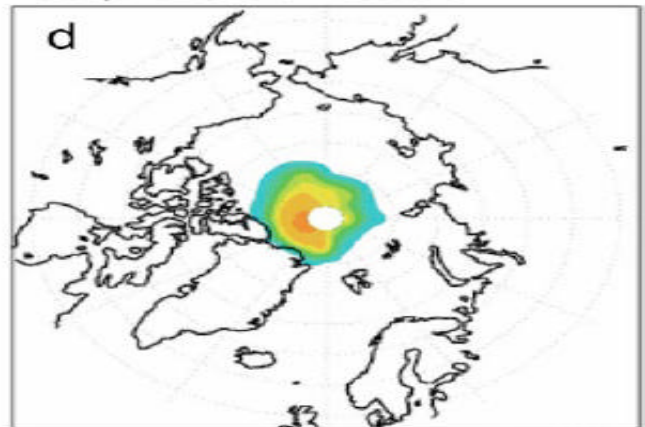


*Echam*

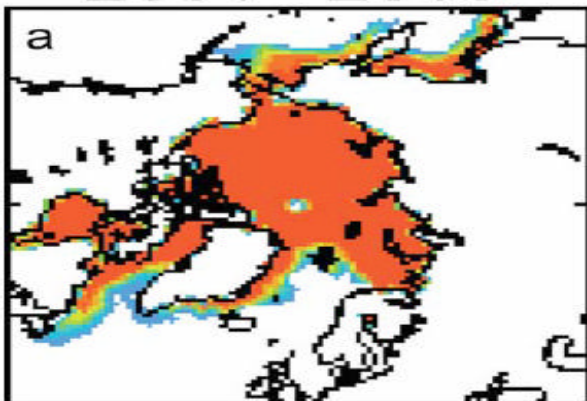
Mar 2081–2090



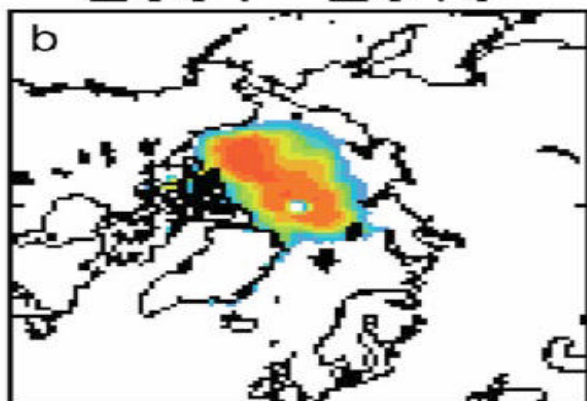
Sep 2081–2090



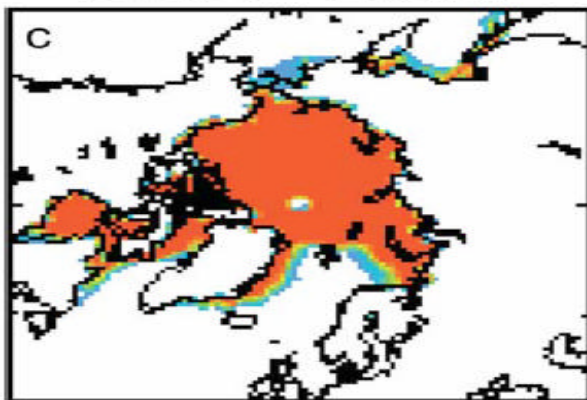
2001-2010



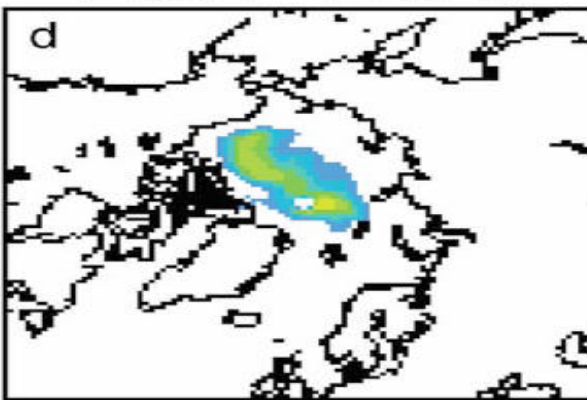
2001-2010



2081-2090



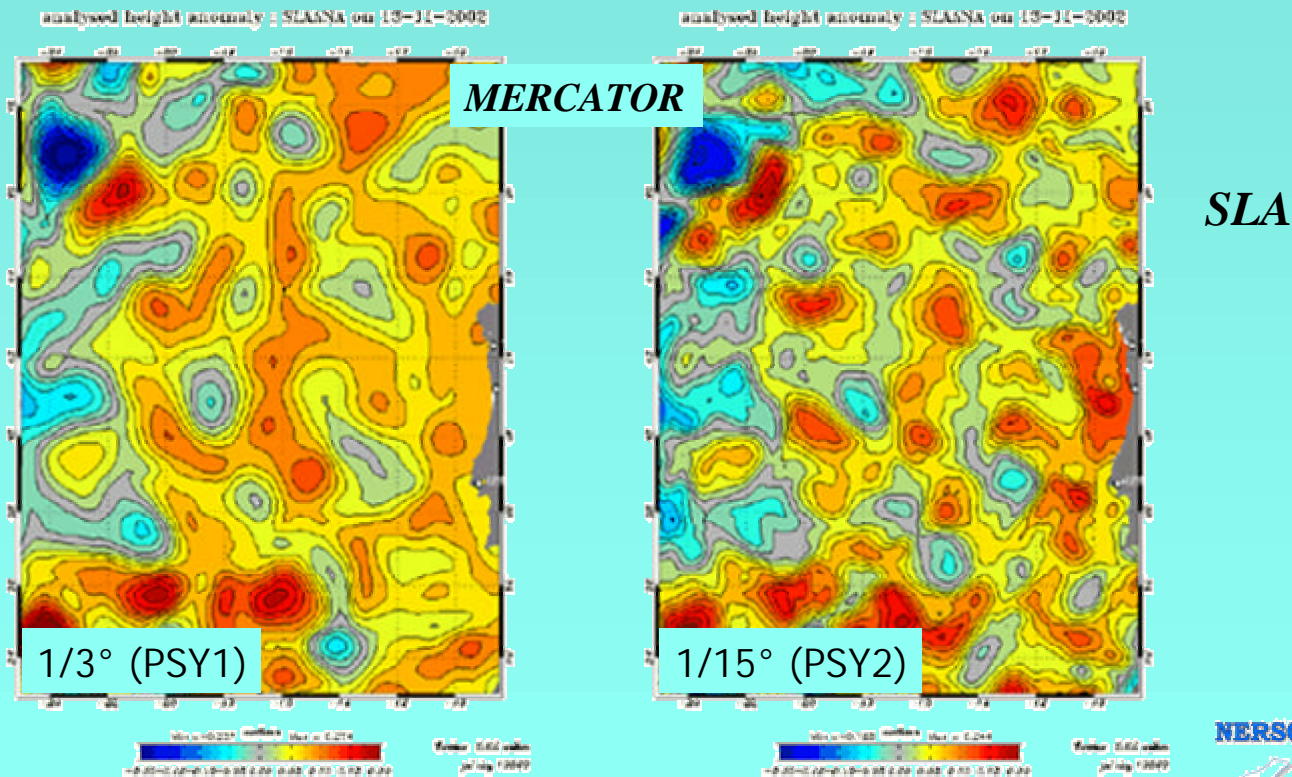
2081-2090



*HadCm*

# Need for improvement

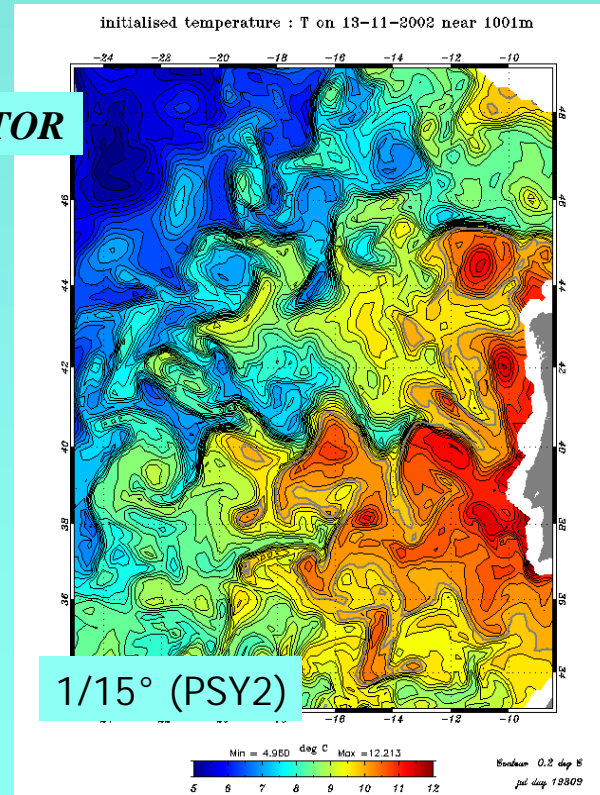
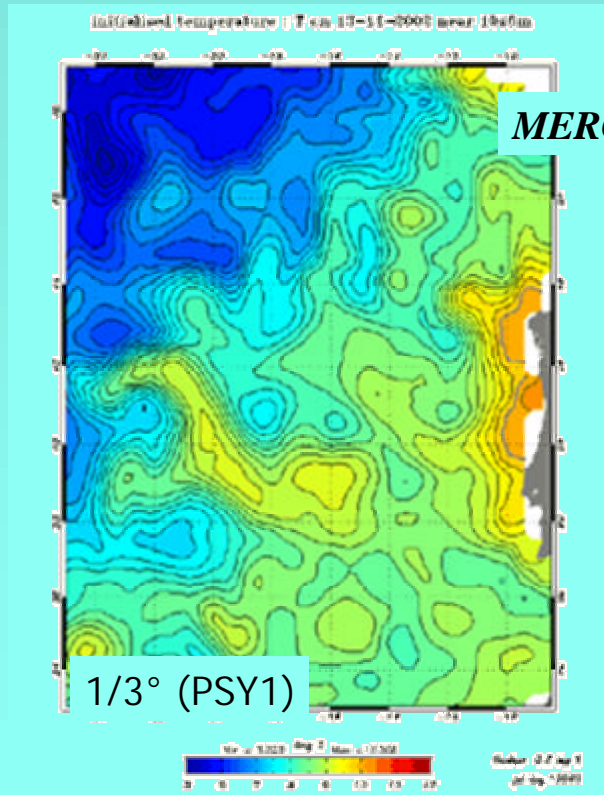
-Model resolution; enhanced resolution in the vertical and horizontal to obtain reliable simulations - global model at 10 km combined with nesting;





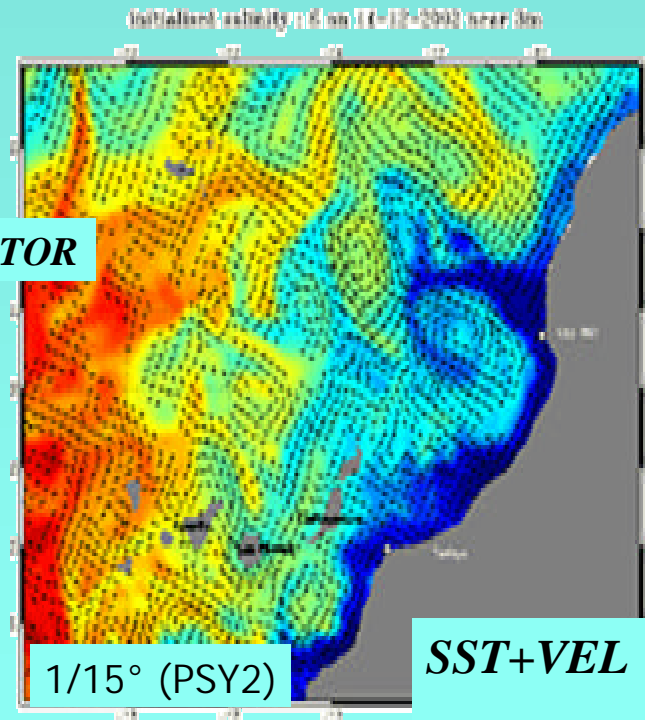
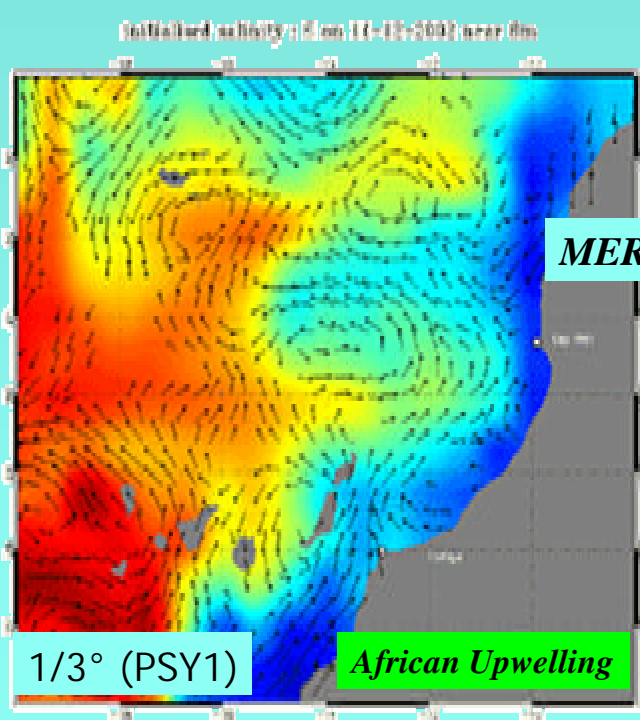
# Need for improvement (cont.)

-Model resolution; enhanced resolution in the vertical and horizontal to obtain reliable simulations - global model at 10 km combined with nesting;



## *Need for improvement (cont.)*

*-Model resolution; enhanced resolution in the vertical and horizontal to obtain reliable simulations - global model at 10 km combined with nesting;*



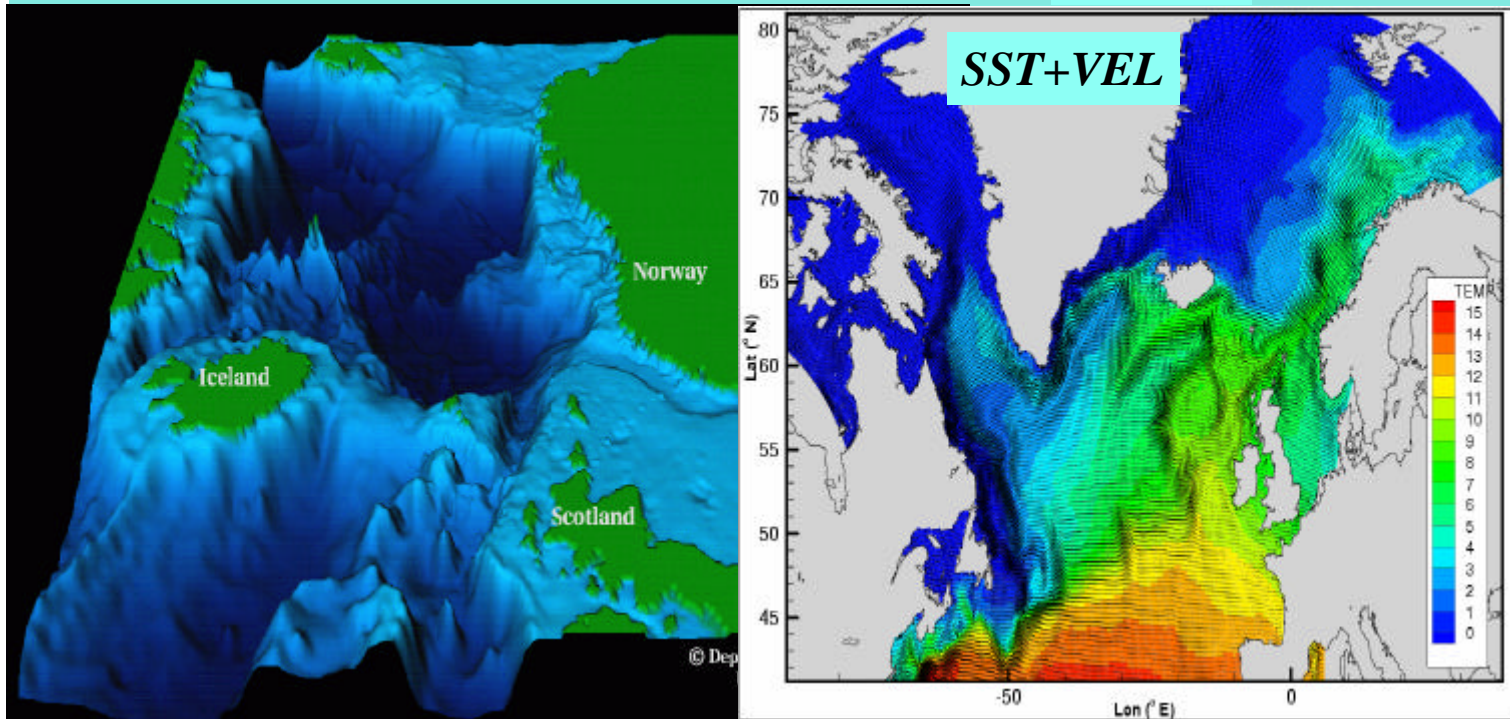
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## *Need for improvement (cont.)*

*-Topography; Improved representation of topographic slopes is critical for simulations of mean and time-varying circulation;*

**MICOM**



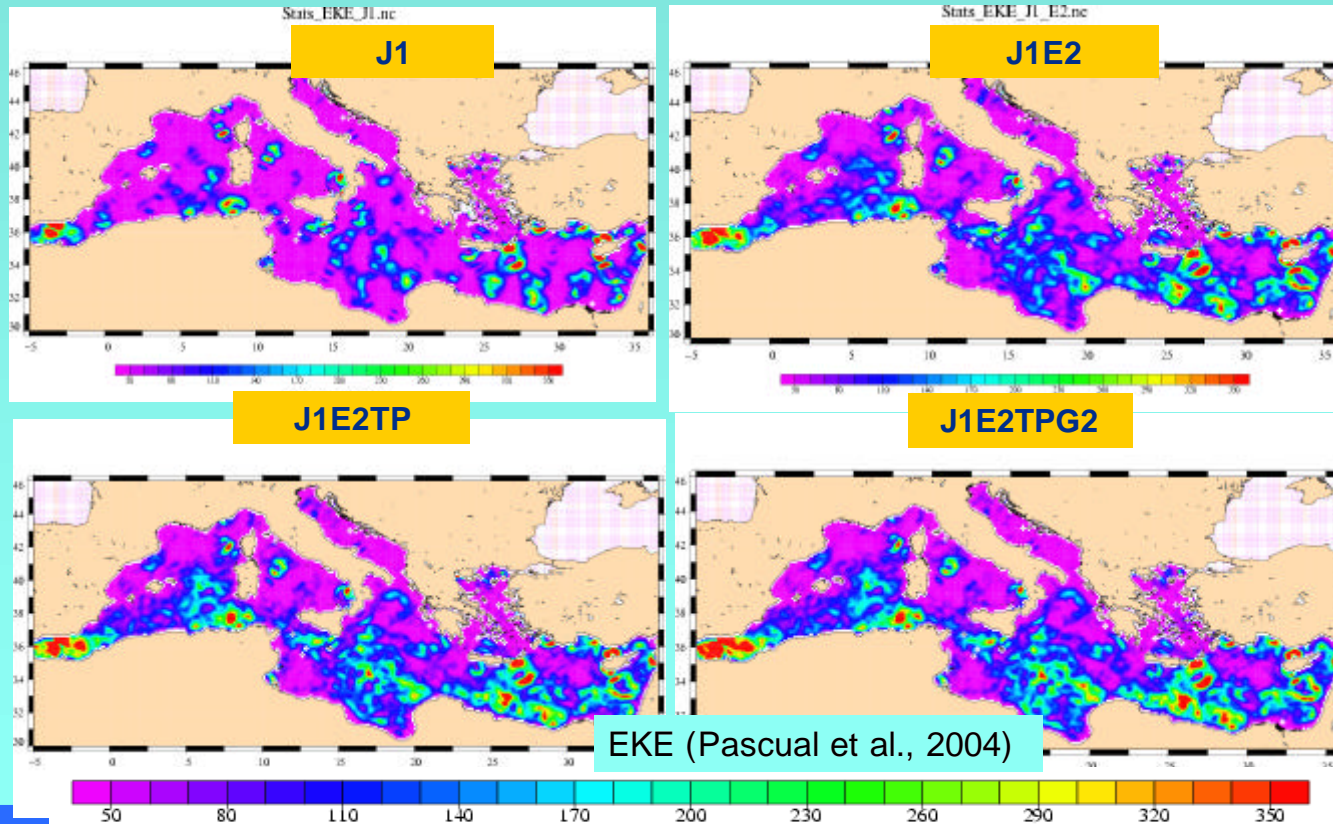
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## *Need for improvement (cont.)*

- *Boundary layer representation; both surface mixed layers and benthic layers near the bottom need to be better simulated*
- *Coupling to ice models; ice models are essential for simulation of horizontal and vertical freshwater fluxes*
- *Mixing processes; mixing across isopycnals need better parameterization*
- *Surface fluxes; the ocean is driven primarily through a combination of buoyancy and momentum fluxes so reliable estimates of surface fluxes of heat, freshwater and momentum*

## *Need for improvement (cont.)*

*- Advance and secure the observing system; integrated observations are needed to provide reliable description of the interior ocean state and to constrain (validate) models.*



# ***RECOMMENDED LITERATURE***

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