

Polarimetric Calibration of Spaceborne SAR Data

in the Presence of the Ionosphere by Means of Azimuth Sub-bands

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Polarimetric System Distortion Model



Polarimetric System Distortion Model

System Tx / Rx Distortion + Propagation (i.e. Faraday Rotation) Distortion :



X-Talk – Faraday Rotation Ambiguity:

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$$Y\begin{bmatrix}1 & \delta_{XH}\\ \delta_{XV} & f_{X}\end{bmatrix}\begin{bmatrix}\cos(\Omega) & \sin(\Omega)\\ -\sin(\Omega) & \cos(\Omega)\end{bmatrix} = \begin{bmatrix}R_{HH}^{\Omega} & R_{HV}^{\Omega}\\ R_{VH}^{\Omega} & R_{VV}^{\Omega}\end{bmatrix}$$
Polar Decomposition of the X-talk matrix:
$$\begin{bmatrix}1 & \delta_{XH}\\ \delta_{XV} & f_{X}\end{bmatrix} = \begin{bmatrix}1 & \beta_{XH}\\ \beta_{XV} & f_{X}\end{bmatrix}\begin{bmatrix}\cos(\Omega_{X}) & \sin(\Omega_{X})\\ -\sin(\Omega_{X}) & \cos(\Omega_{X})\end{bmatrix}$$

$$\begin{bmatrix}R_{HH}^{\Omega} & R_{HV}^{\Omega}\\ R_{VH}^{\Omega} & R_{VV}^{\Omega}\end{bmatrix} = Y\begin{bmatrix}1 & \beta_{XH}\\ \beta_{XV} & f_{X}\end{bmatrix}\begin{bmatrix}\cos(\Omega_{X}) & \sin(\Omega_{X})\\ -\sin(\Omega_{X}) & \cos(\Omega_{X})\end{bmatrix}\begin{bmatrix}\cos(\Omega) & \sin(\Omega)\\ -\sin(\Omega) & \cos(\Omega)\end{bmatrix} = Y\begin{bmatrix}1 & \beta_{XH}\\ \beta_{XV} & f_{X}\end{bmatrix}\begin{bmatrix}\cos(\Omega + \Omega_{X}) & \sin(\Omega + \Omega_{X})\\ -\sin(\Omega + \Omega_{X}) & \cos(\Omega + \Omega_{X})\end{bmatrix}$$
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FR and X-Talk Rotation Ambiguity

Total distortion Matrix:

$$\begin{bmatrix} \mathsf{R}_{\mathsf{H}\mathsf{H}}^{\Omega} & \mathsf{R}_{\mathsf{H}\mathsf{V}}^{\Omega} \\ \mathsf{R}_{\mathsf{V}\mathsf{H}}^{\Omega} & \mathsf{R}_{\mathsf{V}\mathsf{V}}^{\Omega} \end{bmatrix} = \begin{bmatrix} \mathsf{R}_{\mathsf{H}\mathsf{H}} & \mathsf{R}_{\mathsf{H}\mathsf{V}} \\ \mathsf{R}_{\mathsf{V}\mathsf{H}} & \mathsf{R}_{\mathsf{V}\mathsf{V}} \end{bmatrix} \begin{bmatrix} \cos(\Omega) & \sin(\Omega) \\ -\sin(\Omega) & \cos(\Omega) \end{bmatrix} = \begin{bmatrix} \mathsf{1} & \beta_{\mathsf{X}\mathsf{H}} \\ \beta_{\mathsf{X}\mathsf{V}} & \mathsf{f}_{\mathsf{X}} \end{bmatrix} \begin{bmatrix} \cos(\Omega + \Omega_{\mathsf{X}}) & \sin(\Omega + \Omega_{\mathsf{X}}) \\ -\sin(\Omega + \Omega_{\mathsf{X}}) & \cos(\Omega + \Omega_{\mathsf{X}}) \end{bmatrix}$$

... there is an inherent ambiguity between Ω (i.e. FR) and Ω_X (i.e. rotation component of system dist.)



$$\begin{split} & 1 \quad \delta_{\text{EH}} \\ & \delta_{\text{EV}} \quad f_{\text{X}} \end{bmatrix} = k \begin{bmatrix} 1 \quad \delta_{\text{H}} \\ & \delta_{\text{V}} \quad f_{\text{X}} \end{bmatrix} \begin{bmatrix} \cos(\Omega) & -\sin(\Omega) \\ \sin(\Omega) & \cos(\Omega) \end{bmatrix} \\ & = k \begin{bmatrix} \cos(\Omega) + \delta_{\text{H}} \sin(\Omega) & -\sin(\Omega) + \delta_{\text{H}} \cos(\Omega) \\ & \delta_{\text{V}} \cos(\Omega) + f_{\text{X}} \sin(\Omega) & -\delta_{\text{V}} \sin(\Omega) + f_{\text{X}} \cos(\Omega) \end{bmatrix} \end{split}$$

For small FR angles: $cos(\Omega) \approx 1$ and $sin(\Omega) \approx \Omega$

$$\begin{split} \delta_{\mathsf{EH}} &\coloneqq -\sin(\Omega) + \delta_{\mathsf{H}}\cos(\Omega) \approx -\Omega + \delta_{\mathsf{H}}\\ \delta_{\mathsf{EV}} &\coloneqq - f\sin(\Omega) + \delta_{\mathsf{V}}\cos(\Omega) \approx f\Omega + \delta_{\mathsf{V}} \end{split}$$

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Solving the Polarimetric System Calibration Problem cont.

Exploring the $\vec{B} \cdot \vec{\kappa}(\theta_a)$ dependency

Distortion on receive: $\begin{bmatrix} R^{\Omega}_{HH} & R^{\Omega}_{HV} \\ R^{\Omega}_{VH} & R^{\Omega}_{VV} \end{bmatrix} = \begin{bmatrix} R_{HH} & R_{HV} \\ R_{VH} & R_{VV} \end{bmatrix} \begin{bmatrix} \cos(\Omega) & \sin(\Omega) \\ -\sin(\Omega) & \cos(\Omega) \end{bmatrix}$ Distortion on transmit: $\begin{bmatrix} T^{\Omega}_{HH} & T^{\Omega}_{HV} \\ T^{\Omega}_{VH} & T^{\Omega}_{VV} \end{bmatrix} = \begin{bmatrix} \cos(\Omega) & \sin(\Omega) \\ -\sin(\Omega) & \cos(\Omega) \end{bmatrix} \begin{bmatrix} T_{HH} & T_{HV} \\ T_{VH} & T_{VV} \end{bmatrix}$

... by exploring the variation across the synthetic aperture (i.e. across Azimuth "Looks")

Satellite orbit L



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Azimuth Dependency of FR



Separation of FR from X-Talk Rotation Component

2) Exploring the difference in the azimuth dependency of the two components

Distortion on receive:

$$\begin{bmatrix} \mathsf{R}_{\mathsf{HH}}^{\Omega}(\theta_{a}) & \mathsf{R}_{\mathsf{HV}}^{\Omega}(\theta_{a}) \\ \mathsf{R}_{\mathsf{VH}}^{\Omega}(\theta_{a}) & \mathsf{R}_{\mathsf{VV}}^{\Omega}(\theta_{a}) \end{bmatrix} = \begin{bmatrix} \mathsf{R}_{\mathsf{HH}}(\theta_{a}) & \mathsf{R}_{\mathsf{HV}}(\theta_{a}) \\ \mathsf{R}_{\mathsf{VH}}(\theta_{a}) & \mathsf{R}_{\mathsf{VV}}(\theta_{a}) \end{bmatrix} \begin{bmatrix} \cos(\Omega \ (\theta_{a})) & \sin(\Omega \ (\theta_{a})) \\ -\sin(\Omega \ (\theta_{a})) & \cos(\Omega \ (\theta_{a})) \end{bmatrix}$$

Distortion on transmit:

$$\begin{bmatrix} \mathsf{T}_{\mathsf{HH}}^{\Omega}(\theta_{a}) & \mathsf{T}_{\mathsf{HV}}^{\Omega}(\theta_{a}) \\ \mathsf{T}_{\mathsf{VH}}^{\Omega}(\theta_{a}) & \mathsf{T}_{\mathsf{VV}}^{\Omega}(\theta_{a}) \end{bmatrix} = \begin{bmatrix} \cos(\Omega \ (\theta_{a})) & \sin(\Omega \ (\theta_{a})) \\ -\sin(\Omega \ (\theta_{a})) & \cos(\Omega \ (\theta_{a})) \end{bmatrix} \begin{bmatrix} \mathsf{T}_{\mathsf{HH}}(\theta_{a}) & \mathsf{T}_{\mathsf{HV}}(\theta_{a}) \\ \mathsf{T}_{\mathsf{VH}}(\theta_{a}) & \mathsf{T}_{\mathsf{VV}}(\theta_{a}) \end{bmatrix}$$

FR variation across the synthetic aperture (L):

$$\frac{d\Omega}{d(\vec{B}\cdot\hat{\kappa})} = \frac{d\Omega / d\theta_a}{d(\vec{B}\cdot\hat{\kappa}) / d\theta_a} = \frac{\zeta q_e}{c m_e} \frac{1}{f_0^2} TEC$$

 $d\Omega$: Span of az. sub-band FR

 $d(\vec{B} \cdot \hat{\kappa})$: Change of $\vec{B} \cdot \hat{\kappa}$ along the synthetic aperture

 $\hat{\kappa}=\hat{\kappa}(\theta_a)$ (and the piercing point) change with θ_a

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Solving the Polarimetric System Calibration Problem cont.

Separation of FR from X-Talk Rotation by exploring the variation across the aperture (Az):

$$\begin{bmatrix} R_{HH}^{\Omega}(\theta_{a}) & R_{VV}^{\Omega}(\theta_{a}) \\ R_{VH}^{\Omega}(\theta_{a}) & R_{VV}^{\Omega}(\theta_{a}) \end{bmatrix} = \begin{bmatrix} R_{HH}(\theta_{a}) & R_{HV}(\theta_{a}) \\ R_{VH}(\theta_{a}) & R_{VV}^{\Omega}(\theta_{a}) \end{bmatrix} = \begin{bmatrix} R_{HH}(\theta_{a}) & R_{VV}(\theta_{a}) \\ R_{VH}(\theta_{a}) & R_{VV}(\theta_{a}) \end{bmatrix} = \begin{bmatrix} R_{HH}^{I} & R_{HV}^{I} \\ R_{VH}^{I} & R_{VV}^{I} \\ R_{VH}^{I} & R_{A}^{I} \\ R_{VH}^{I}(\theta_{a}) & R_{VV}^{I}(\theta_{a}) \end{bmatrix} = \begin{bmatrix} R_{HH}^{I} & R_{HV}^{I} \\ R_{VH}^{I} & R_{A}^{I} \\ R_{VH}^{I} & R_{A}^{I} \\ R_{VH}^{I}(\theta_{a}) & R_{VV}^{I}(\theta_{a}) \end{bmatrix} = \begin{bmatrix} R_{HH}^{I} & R_{HV}^{I} \\ R_{VH}^{I} & R_{A}^{I} \\ R_{VH}^{I} & R_{A}^{I} \\ R_{VH}^{I}(\theta_{a}) & R_{VV}^{I}(\theta_{a}) \end{bmatrix} = \begin{bmatrix} R_{HH}^{I} & R_{HV}^{I} \\ R_{VH}^{I} & R_{A}^{I} \\ R_{HH}^{I} & R_{A}^{I} \\ R_{A}^{I} & R_{A}^{I} \\ R_{$$

Separation of FR from X-Talk Rotation component cont.

Assumption: Antenna patterns characterise the Az. variable system term:



Test Site: Remningstorp, Sweden (ALOS-1)

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	ALPSRP	DATE
0	01697 2430	06/05/20
	02368 2430	06/07/05
	03039 2430	06/08/20
	03710 2430	06/10/05
T.	ALPSRP	
0	01908 1170	06/06/03
	02579 1170	06/07/19
	03921 1170	06/10/19
	04592 1170	06/12/04

Range

	ALPSRP	DATE
	02295 2640	06/06/30
	02966 2640	06/08/15
	03637 2640	06/09/30
うちし	04308 2640	06/11/15
	04979 2640	06/12/31
	05650 26 <mark>4</mark> 0	07/02/15
	06321 2640	07/04/02
	10347 2640	08/01/03
	11689 2640	08/04/04
	13702 2640	08/08/20

Range

Azimuth

Test Site: Oberpfaffenhofen, Germany, ALOS-1



Test Site: Remningstorp

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	ALPSRP	DATE	Ģ
0	01697 2430	06/05/20	int.
	02368 2430	06/07/05	
	03039 2430	06/08/20	
	03710 2430	06/10/05	
	ALPSRP		
0	ALPSRP 01908-1170	06/06/03	
0	ALPSRP 01908 1170 02579 1170	06/06/03 06/07/19	
0	ALPSRP 01908-1170 02579-1170 03921-1170	06/06/03 06/07/19 06/10/19	
0	ALPSRP 01908 1170 02579 1170 03921 1170 04592 1170	06/06/03 06/07/19 06/10/19 06/12/04	

Range



	02966 2640	06/08/15
and the second s	03637 2640	06/09/30
	04308 2640	06/11/15
	04979 2640	06/12/31
	05650 2640	07/02/15
and the second s	06321 2640	07/04/02
S.	10347 2640	08/01/03
	11689 2640	08/04/04
	13702 2640	08/08/20

Test Site: Oberpfaffenhofen, Germany, ALOS-1



Test Site: Kalimantan (ALOS-2) PRF: 2321 Hz









Test Site: Kyushu (ALOS-2) PRF: 2610 Hz





Test Site: Namibia (ALOS-2) PRF: 2596 Hz





Dependencies on Model Height

→ The squint dependency of FR is a function of (geomagnetic) latitude, and altitude



Dependencies on Height

→ The squint dependency of FR is a function of (geomagnetic) latitude, and altitude



Conclusions

- There is an inherent ambiguity between FR distortion and the rotation component of the system distortion (x-talk);
- The azimuth variation of the FR provides a way to separate the FR distortion from system induced distortion for the calibration of spaceborne polarimetric data
- > Determination of the azimuth dependency of FR relies on mean FR estimates and $\vec{B} \cdot \hat{\kappa}$.
- At low latitudes $\vec{B} \cdot \hat{\kappa}$ becomes too sensitive with respect to the ionospheric height assumption.
- The proposed algorithm relaxes significantly the constrains imposed by conventional polarimetric calibration approaches in the sense that:

1) there are no calibration devices (i.e. reflectors, transponders, etc.) required at the geomagnetic equator but they can still be located in areas where **B**·**k**=**0**;

2) it allows the estimation of X-Talk levels from each single scene and not only where **B**-**k**=**0** is fulfilled.

> Performance analysis (e.g. investigating scene-dependent deviation, etc.) to be done.



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