

SAR Basic Concepts: Estimation of Vertical Structure Parameters

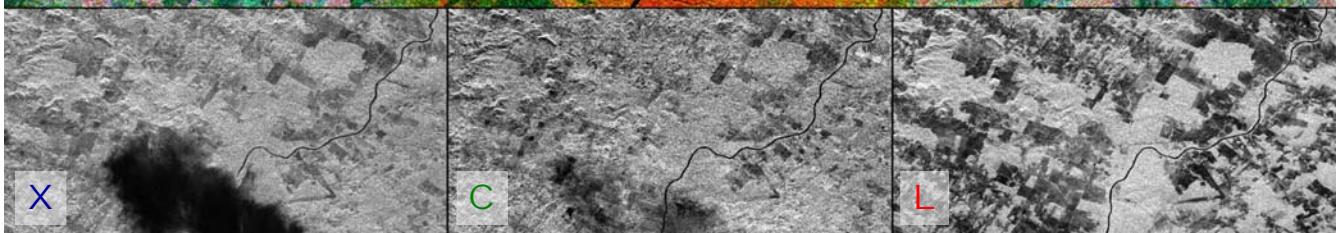
Konstantinos Papathanassiou
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Microwaves and Radar Institute (DLR-HR)
German Aerospace Center (DLR)

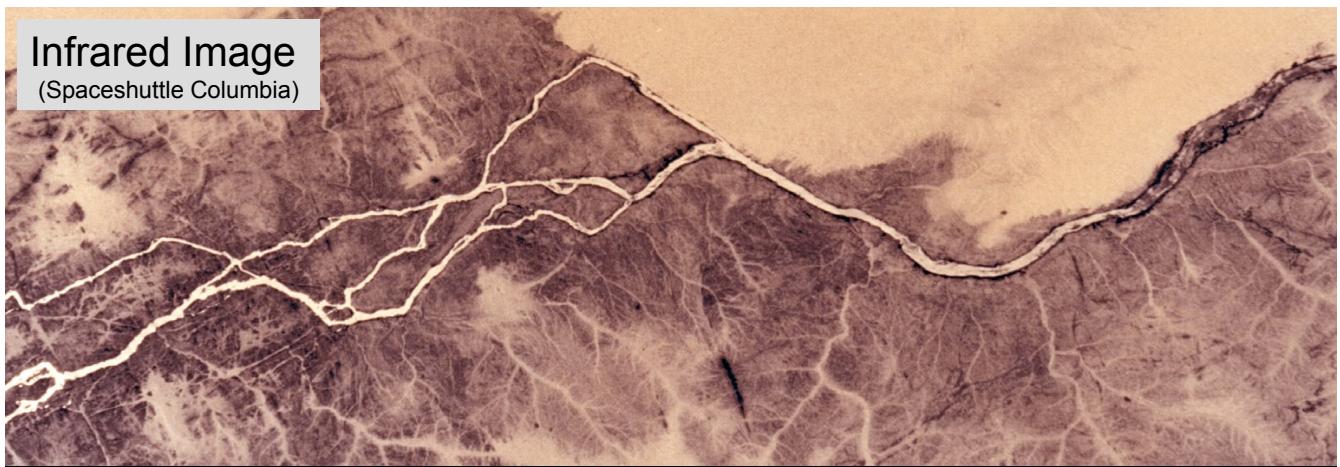
1994: Shuttle Radar Lab SIR-C/X-SAR

35,3 km

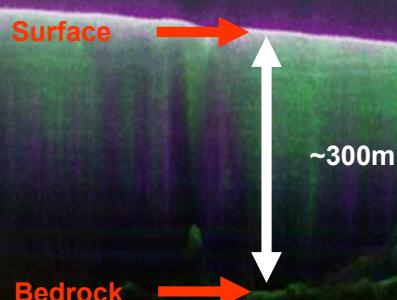
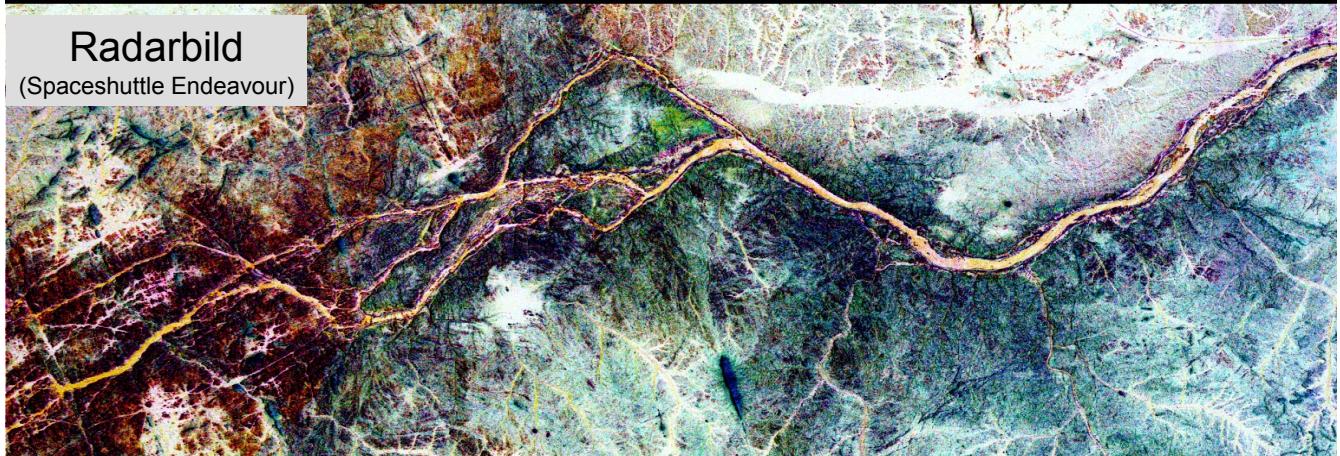
21,3 km



Infrared Image
(Spaceshuttle Columbia)



Radarbild
(Spaceshuttle Endeavour)

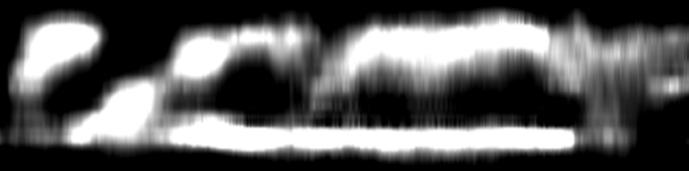


Penetration into Ice

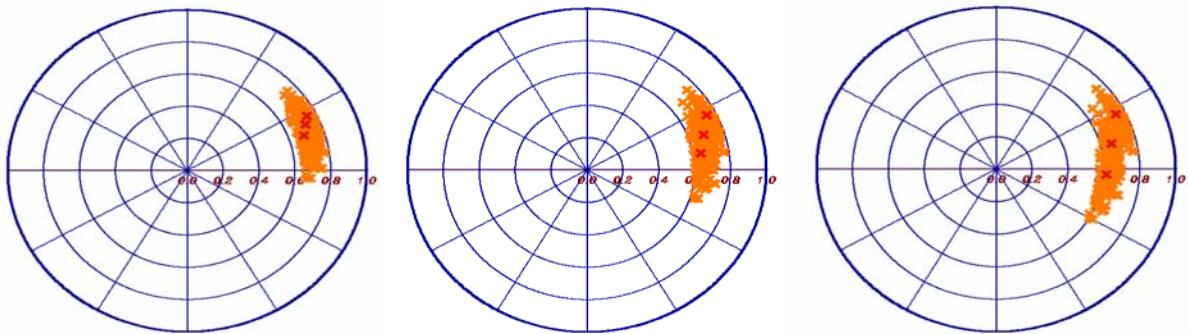
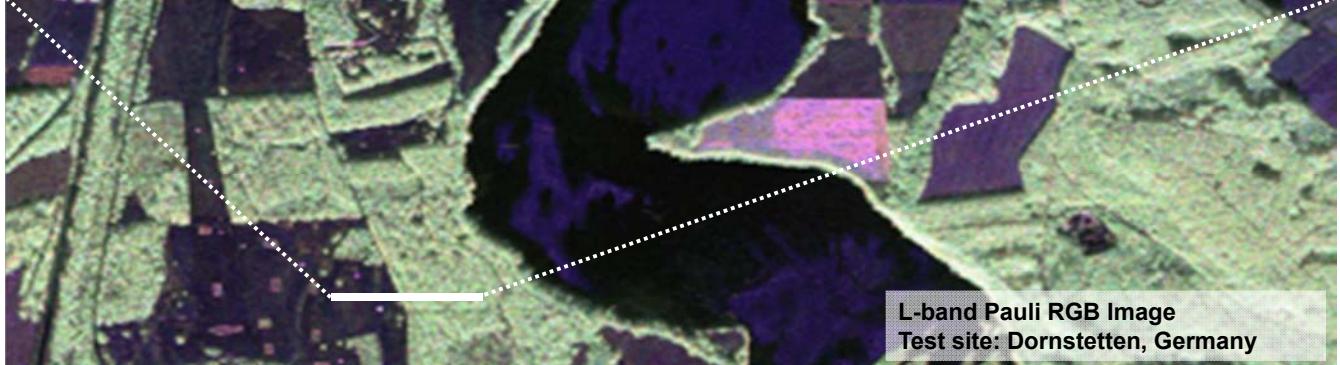
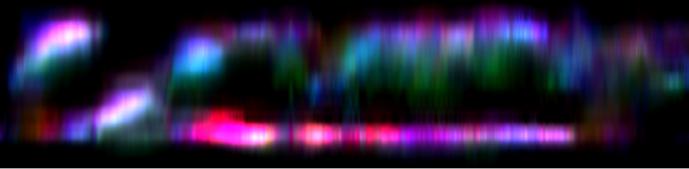
E-SAR / Test Site: Glacier Austfonna, Svalbard

Penetration into Vegetation

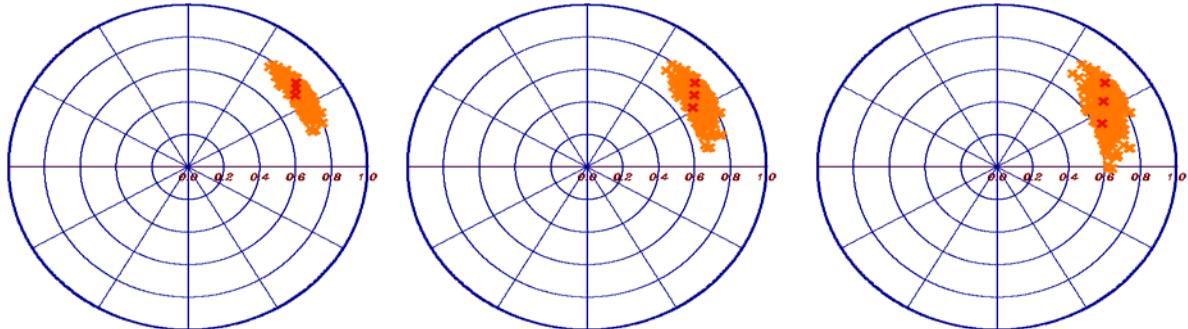
Vertical Reflectivity Profile (HH)



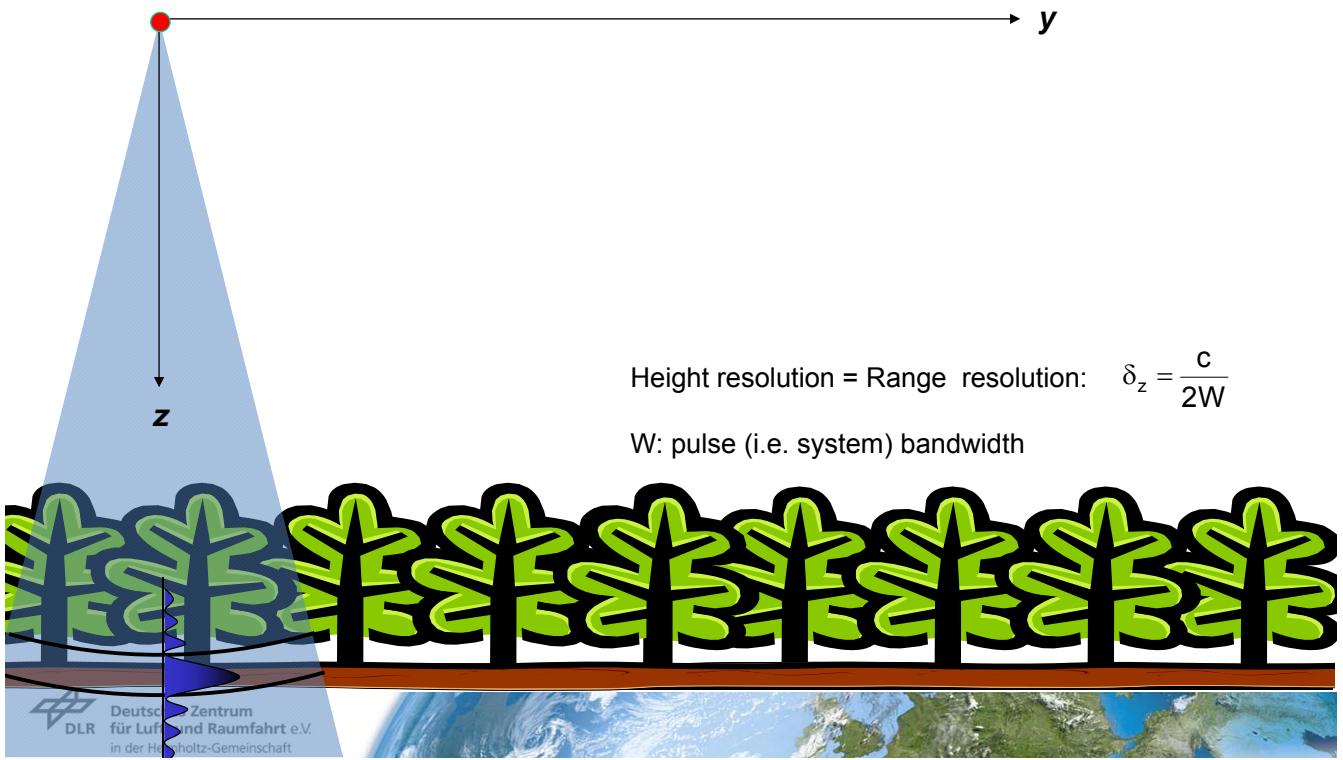
Vertical Reflectivity Profile (Pauli)



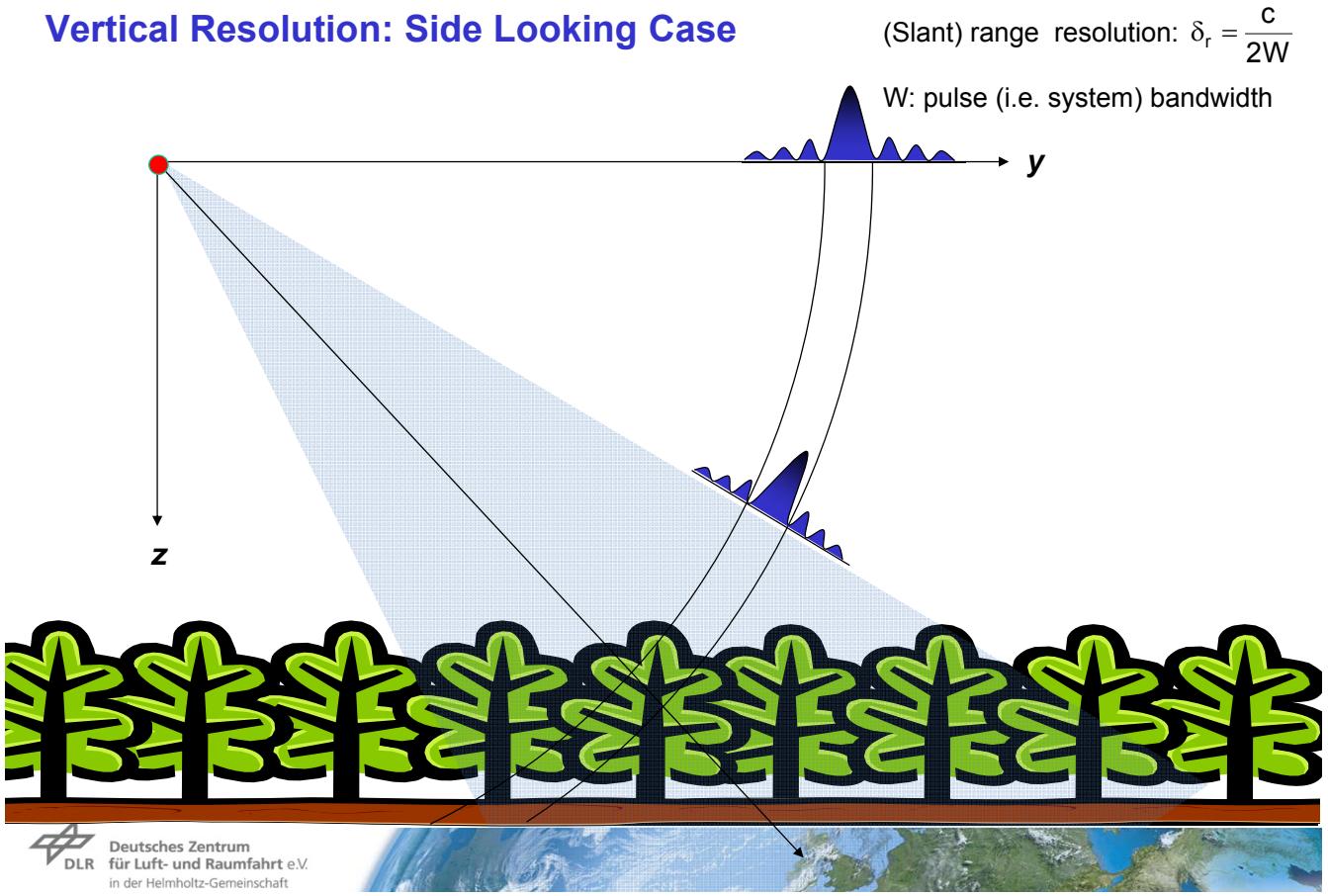
Cross-Range Resolution



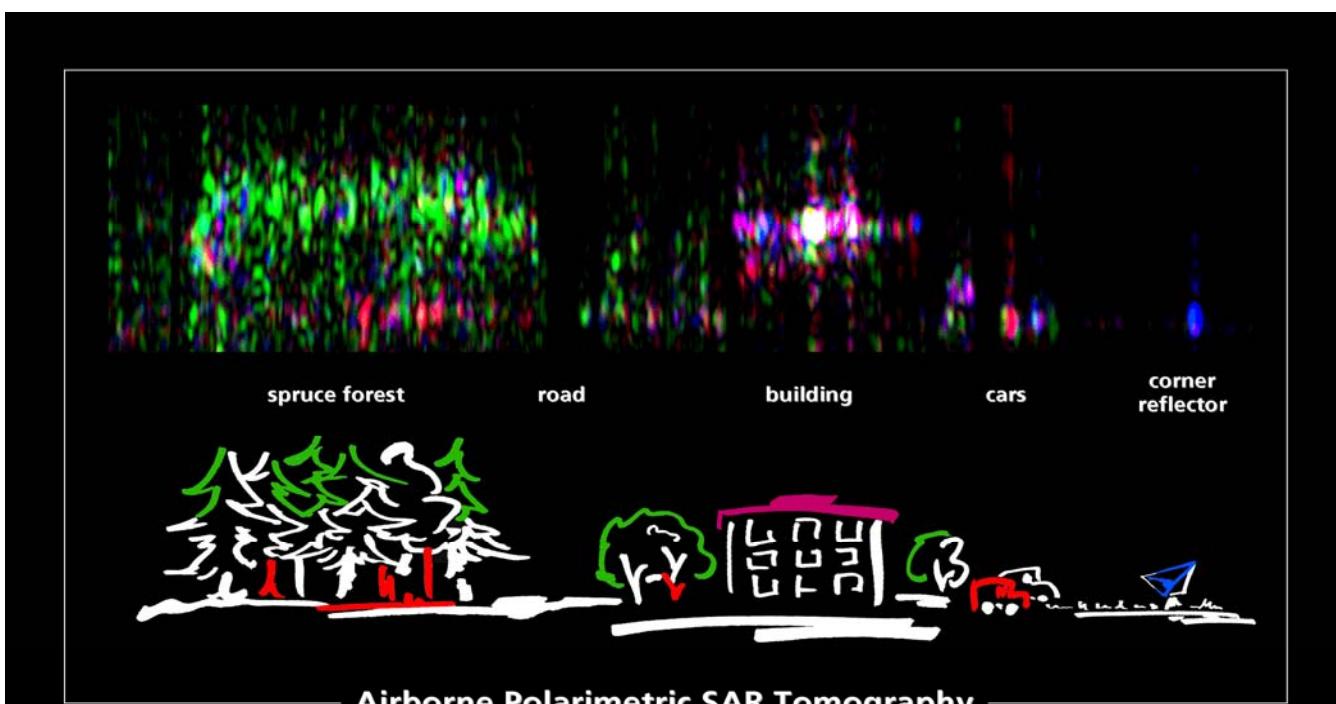
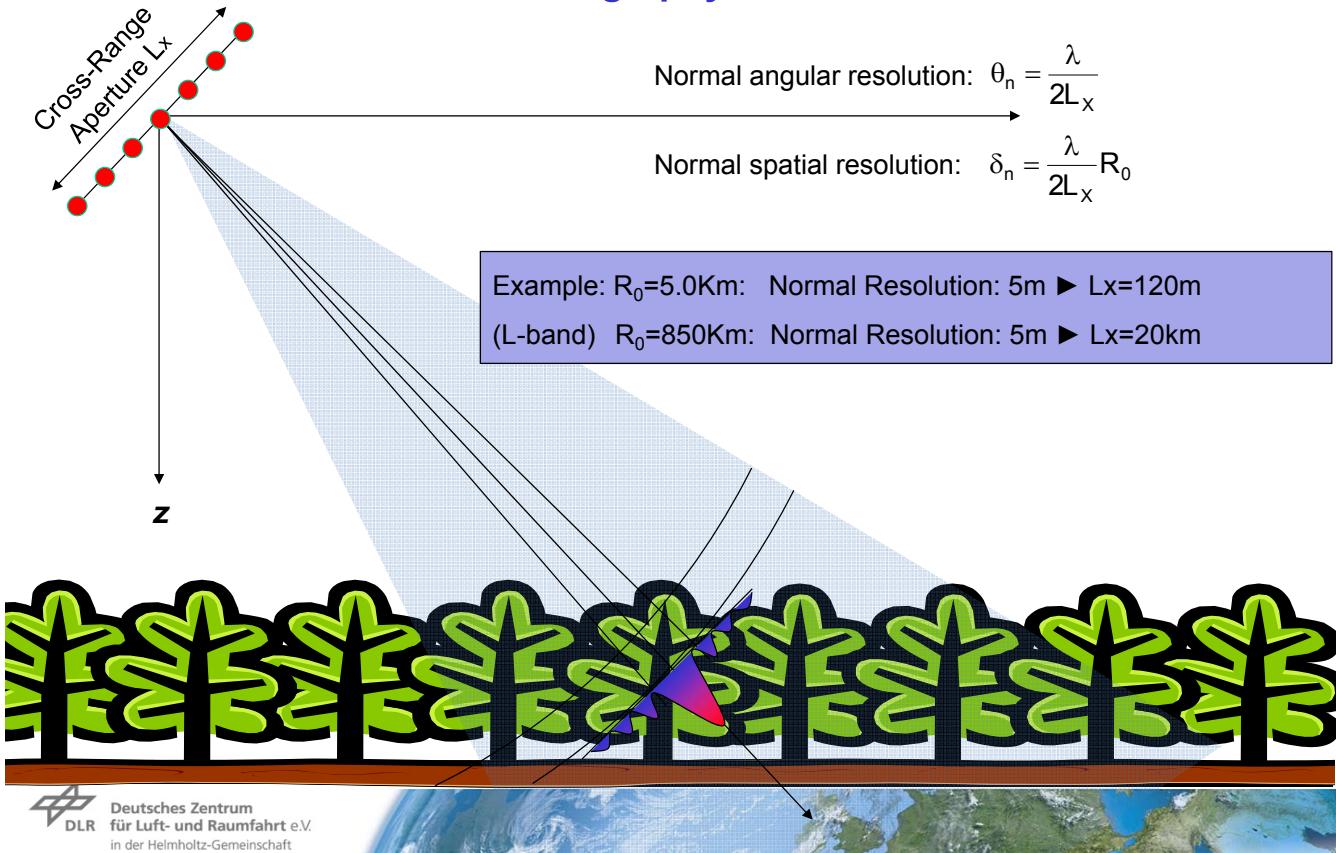
Vertical Resolution: Nadir Looking Case



Vertical Resolution: Side Looking Case

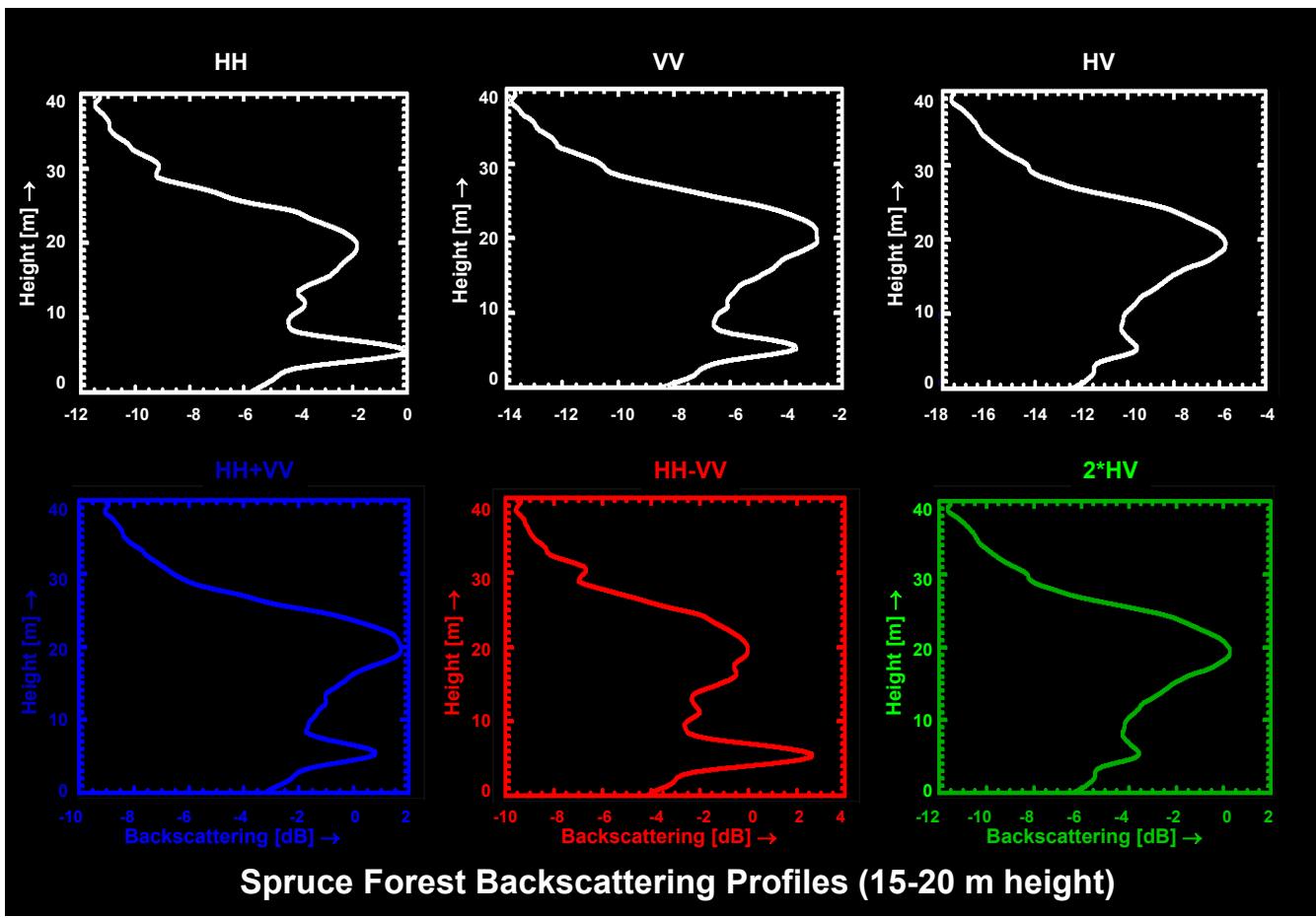
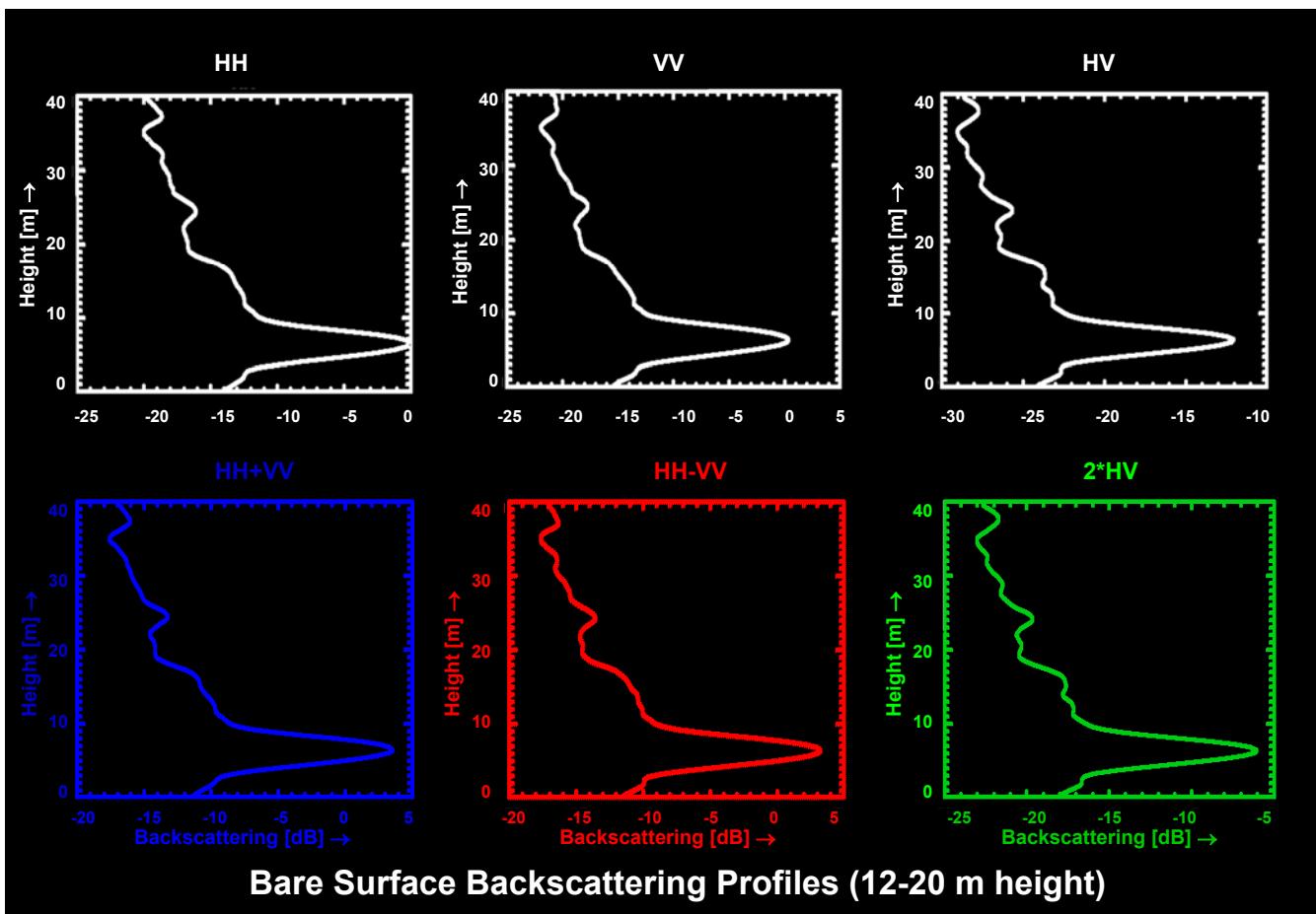


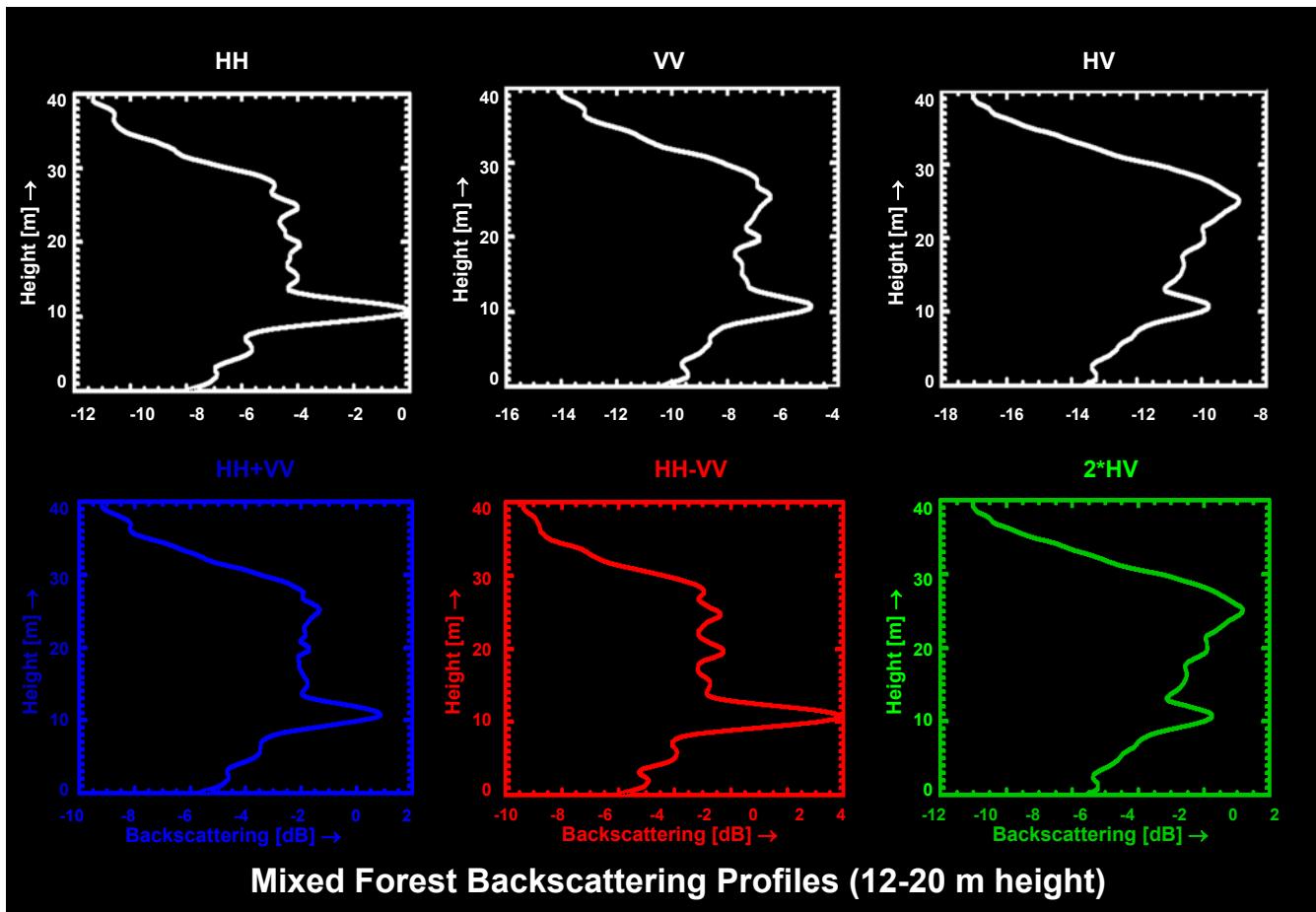
Vertical Resolution: SAR Tomography



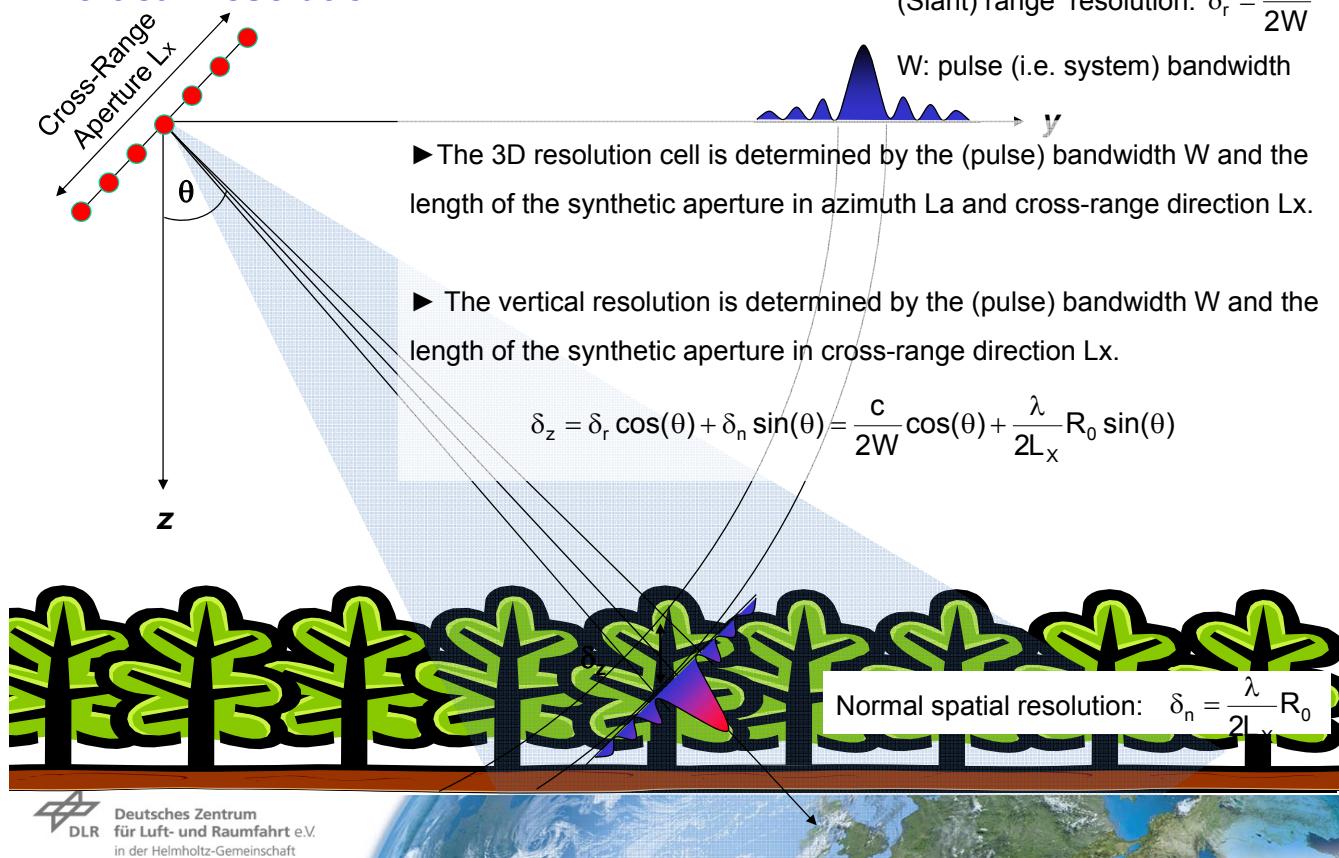
Upper image: Polarimetric color composite (L-band) of a tomographic slice in the height/azimuth-direction
■ HH+VV, ■ HH-VV, ■ 2*HV

Lower image: Schematic view of the imaged area

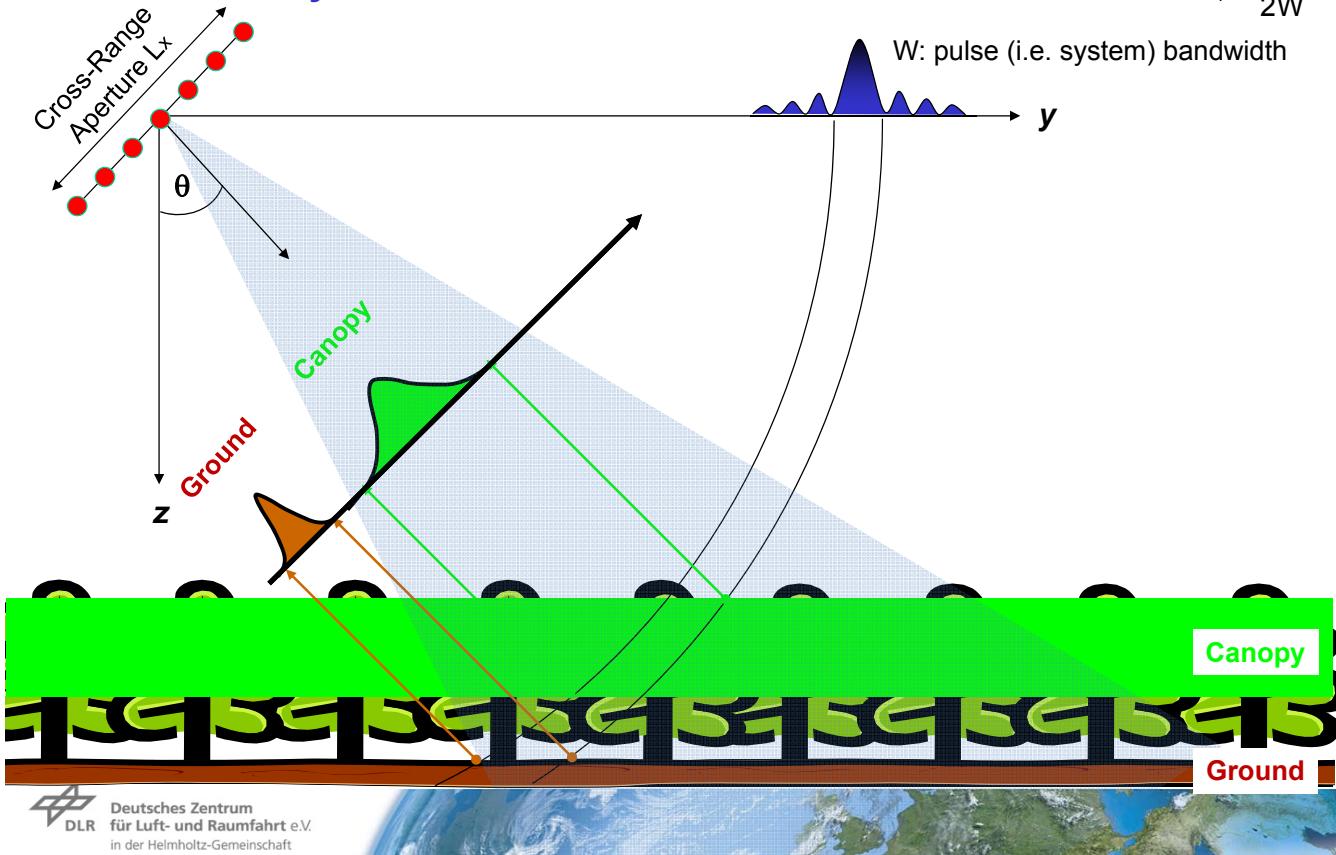




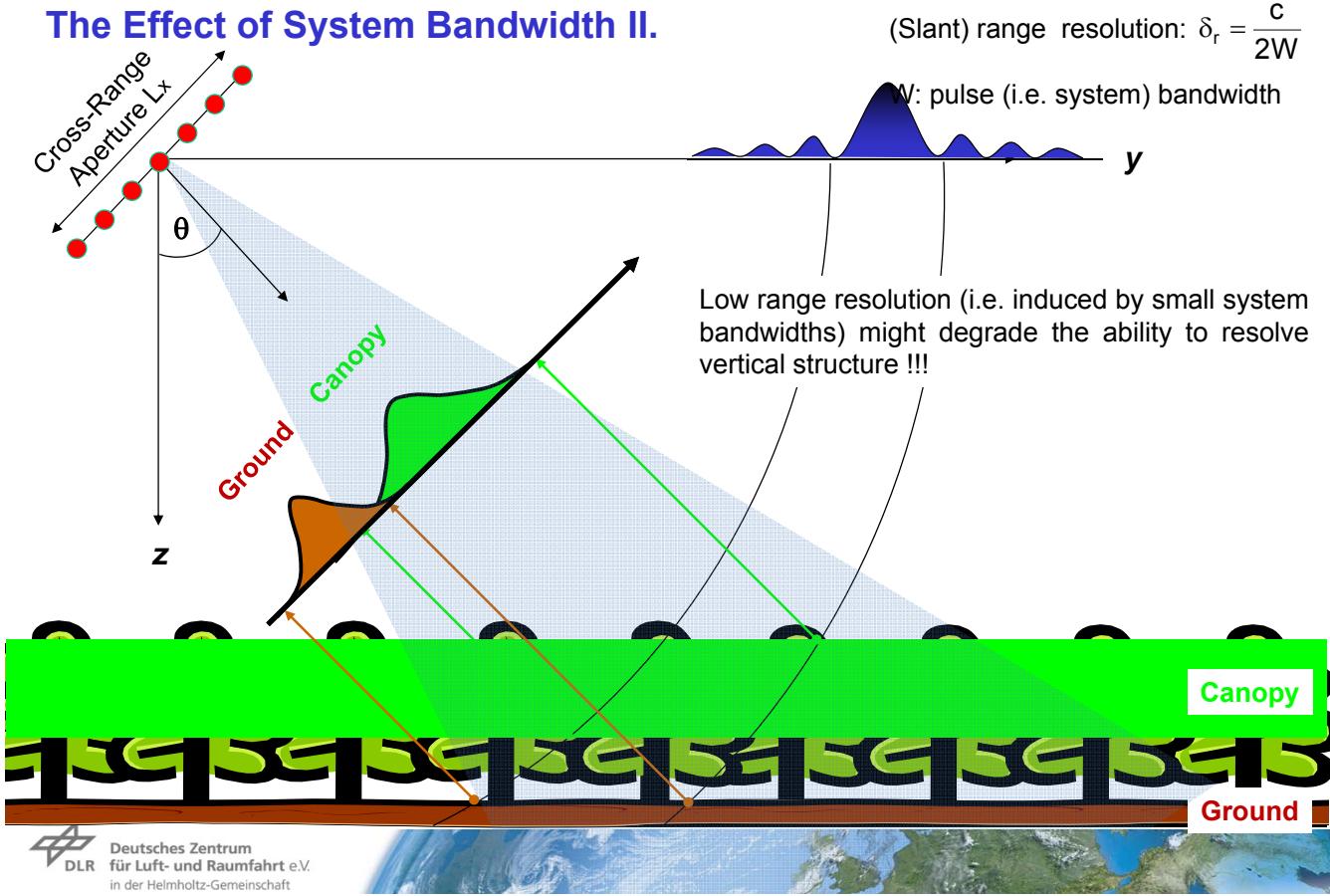
Vertical Resolution



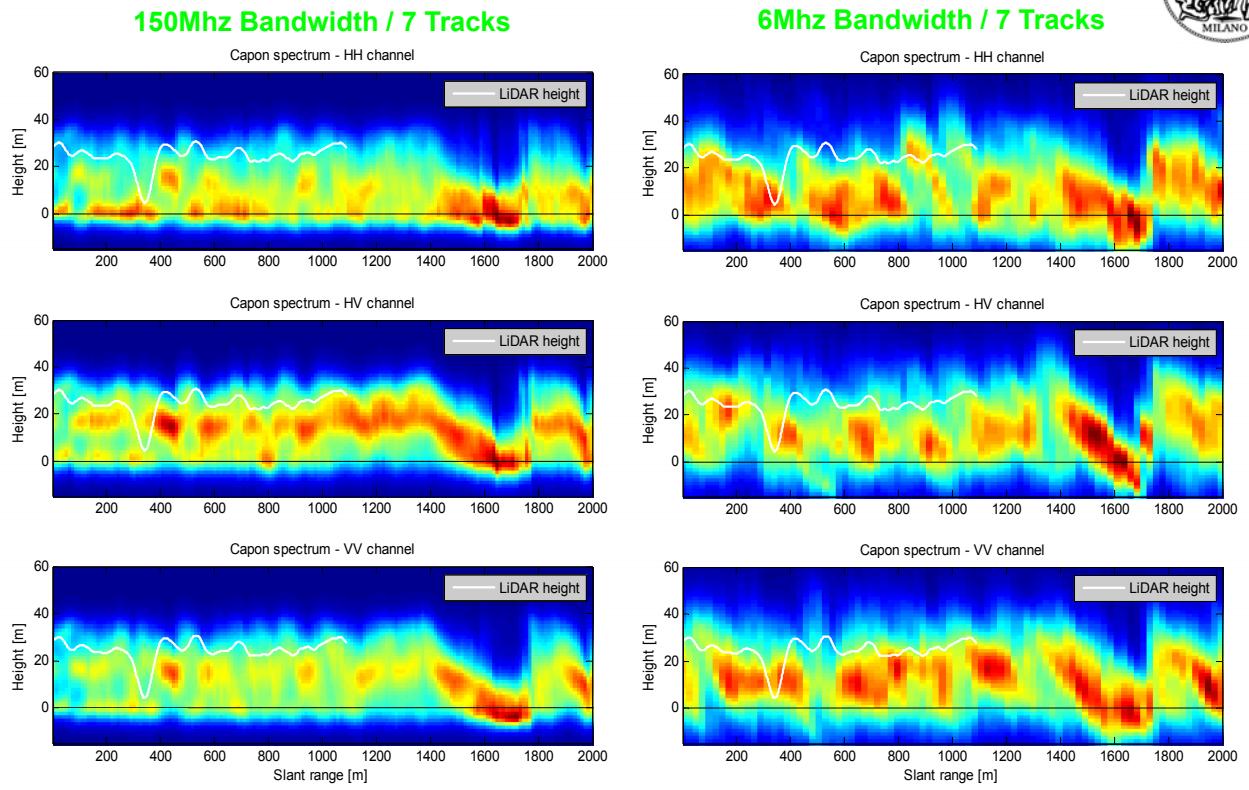
The Effect of System Bandwidth



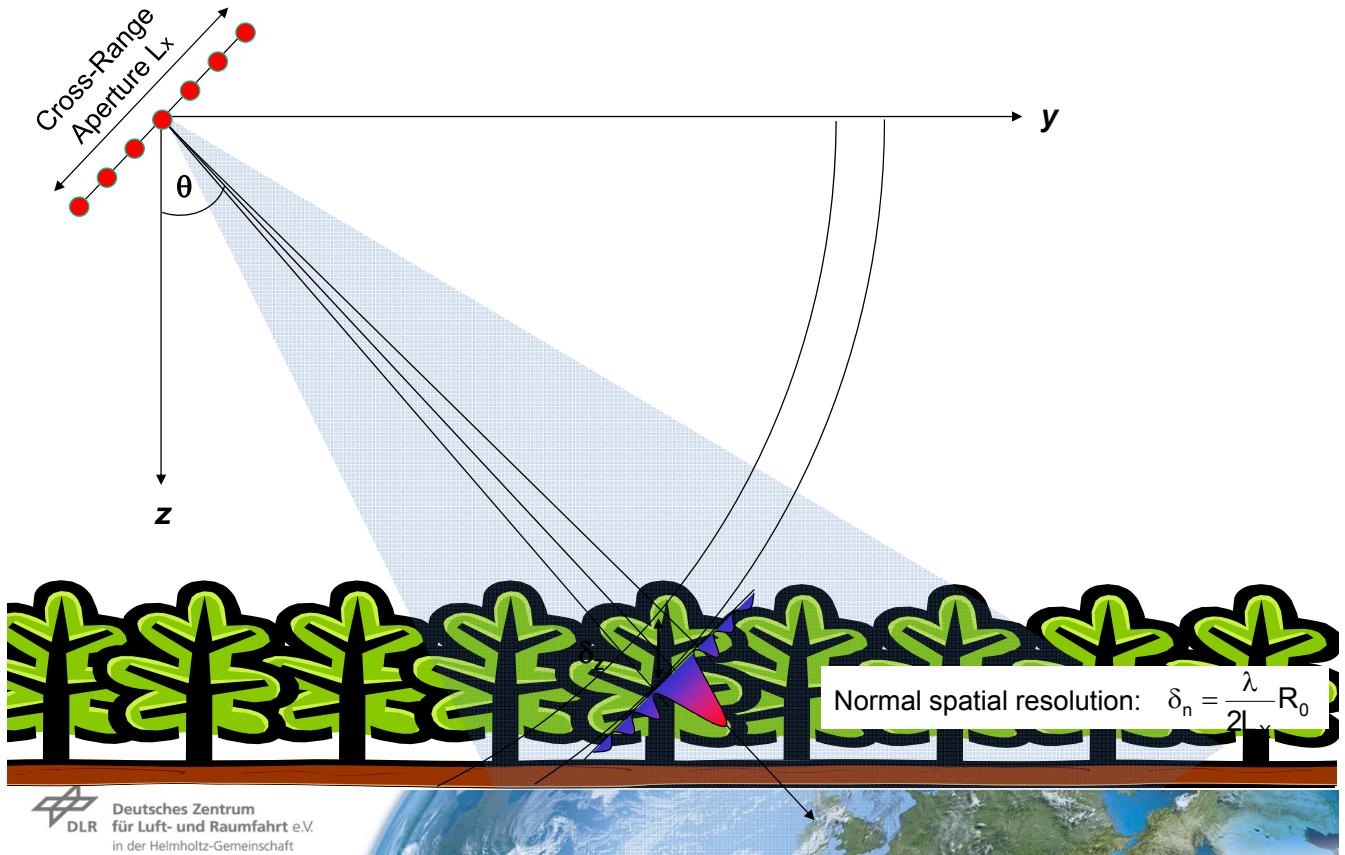
The Effect of System Bandwidth II.



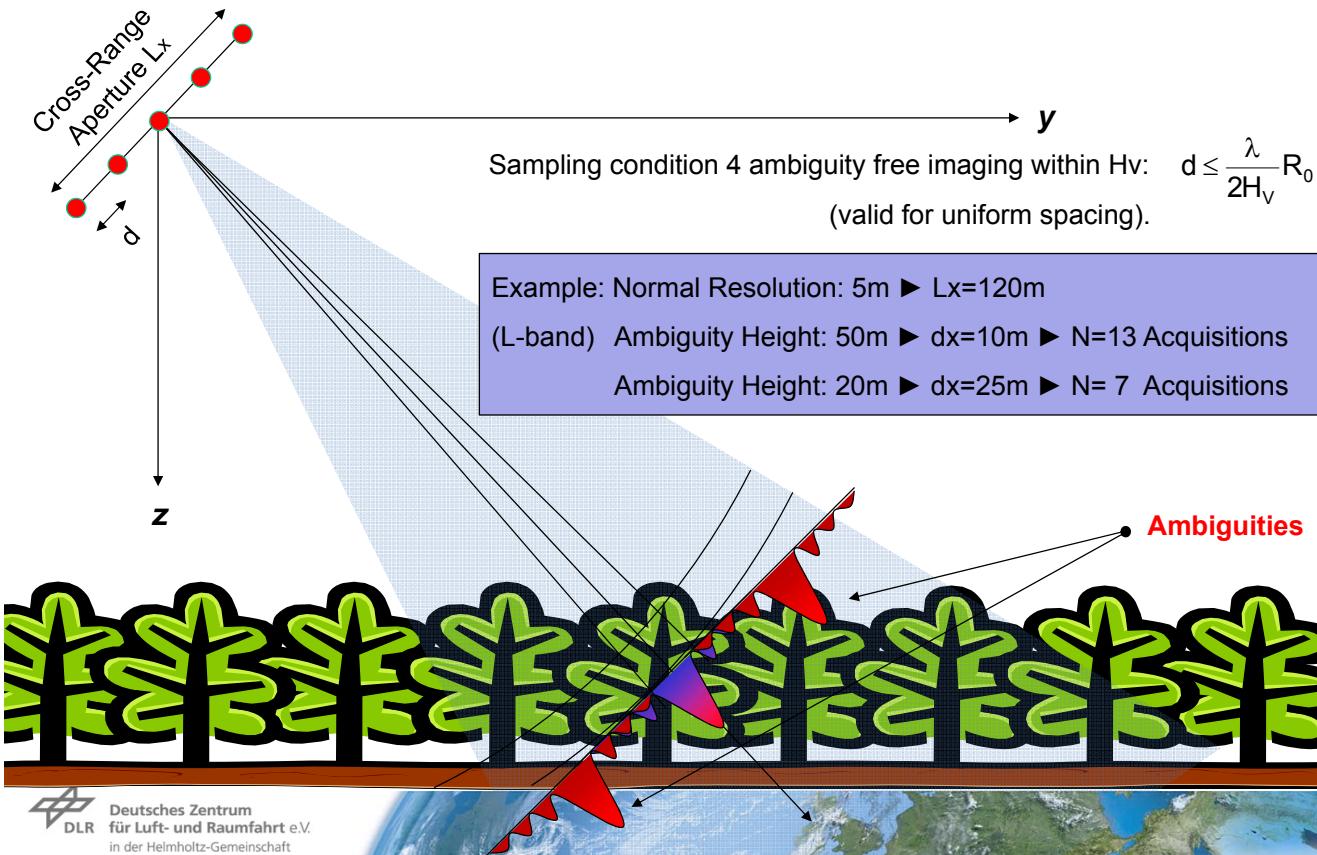
The Effect of System Bandwidth



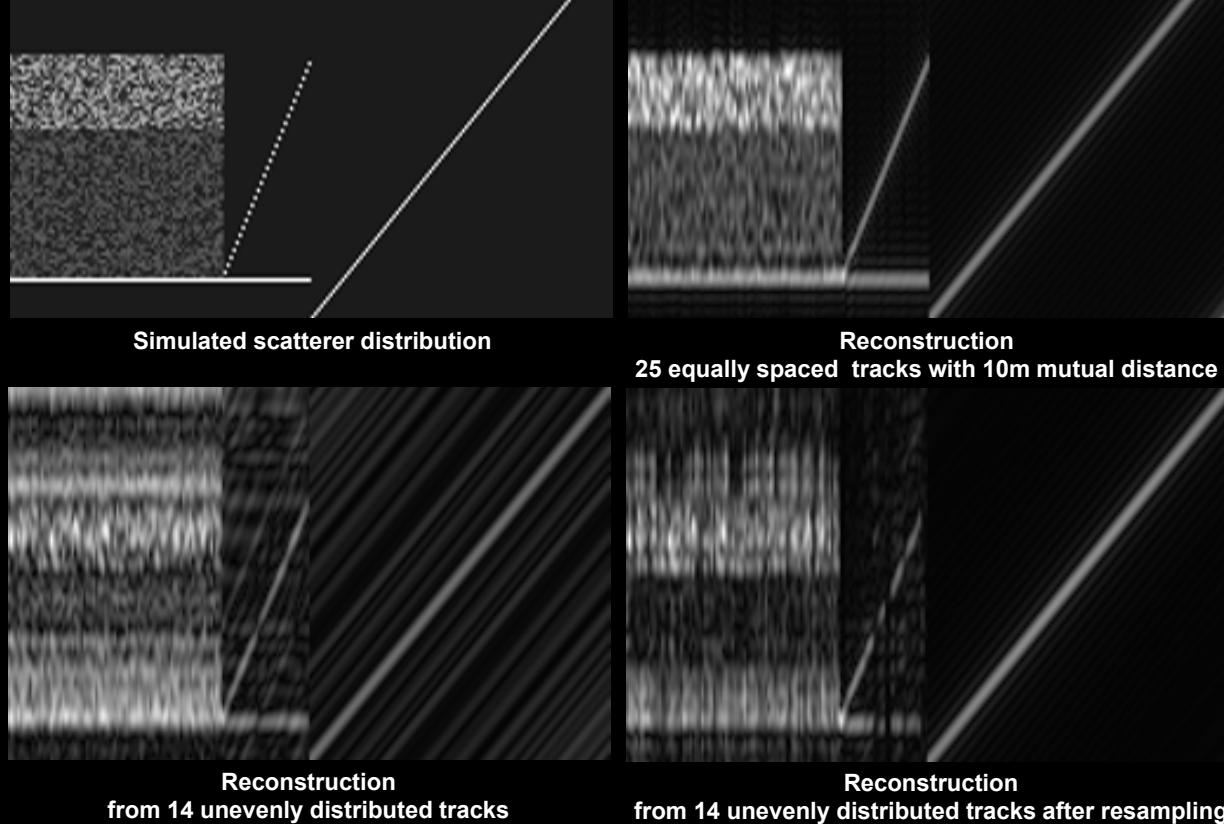
Vertical Resolution



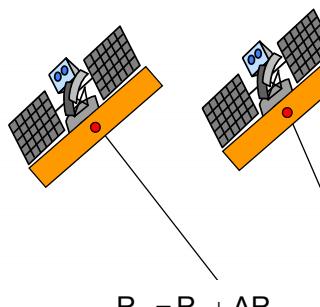
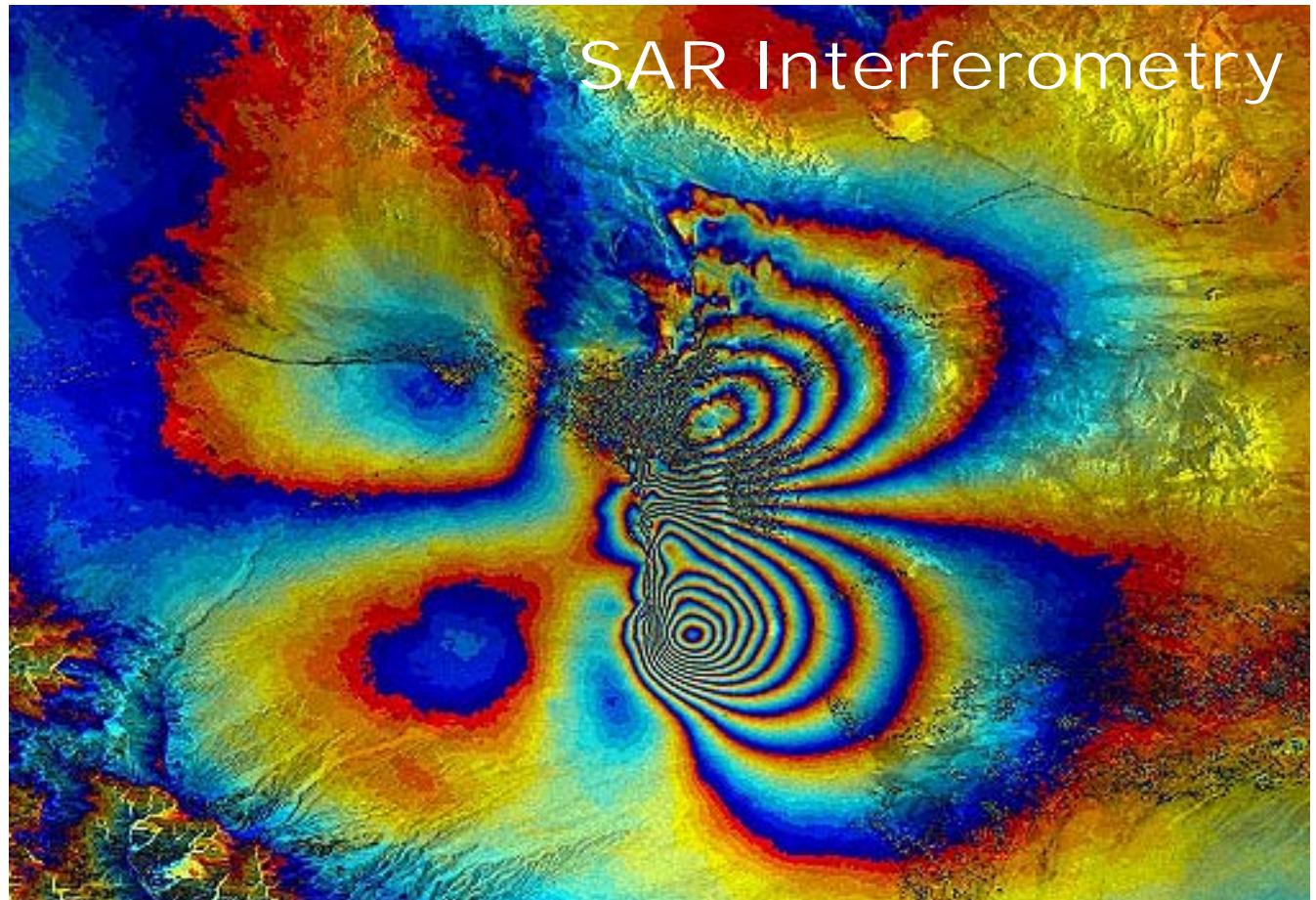
Vertical Resolution



Sidelobe / Ambiguity Suppression



SAR Interferometry



SAR Interferometry



Signal from resolution cell P in Image 1: $i_1 = |i_1| \exp[-i(2\frac{2\pi}{\lambda}R_1) + \phi_{s1}]$

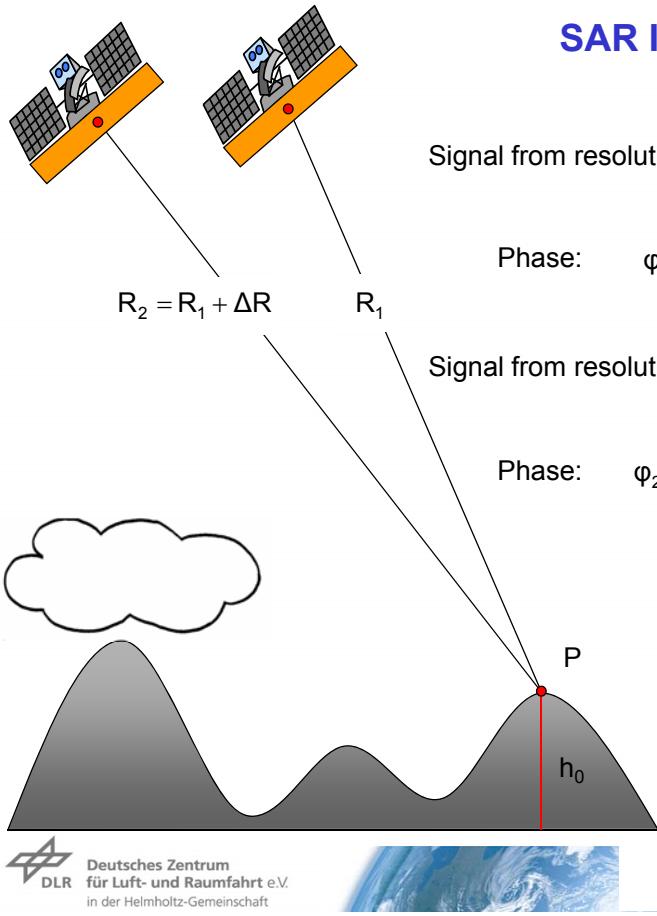
Phase: $\phi_1 = \arg(i_1) = (2\frac{2\pi}{\lambda}R_1) + \phi_{s1}$

Signal from resolution cell P in Image 2: $i_2 = |i_2| \exp[-i(2\frac{2\pi}{\lambda}R_2) + \phi_{s2}]$

Phase: $\phi_2 = \arg(i_2) = (2\frac{2\pi}{\lambda}R_2) + \phi_{s2}$



SAR Interferometry

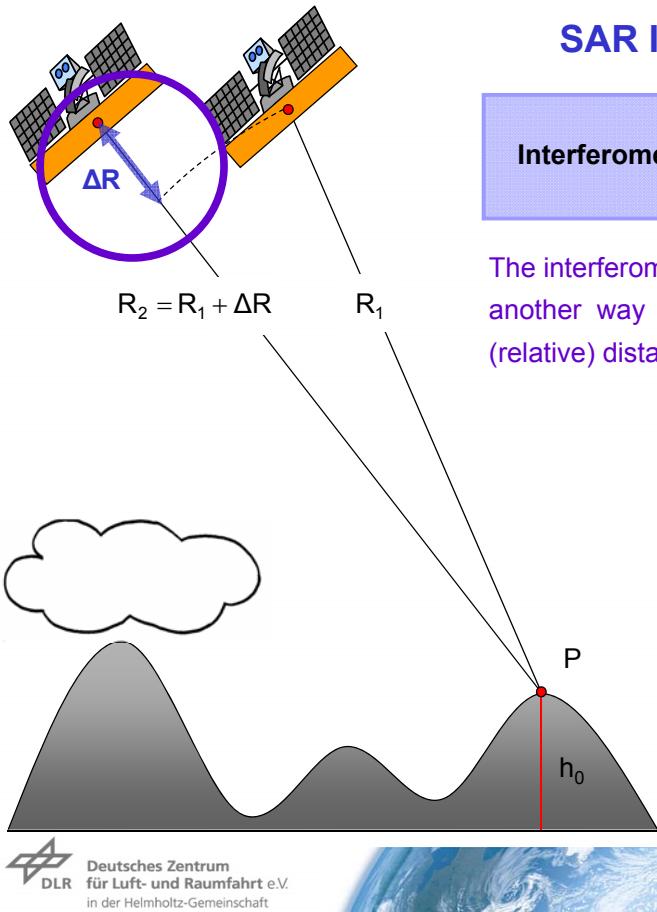


Assuming $\phi_{S1} = \phi_{S2}$!!!

Interferogram: $i_1 i_2^* = |i_1 i_2^*| \exp[-i(2\frac{2\pi}{\lambda} \Delta R)]$

$$\text{Phase: } \phi_{\text{Int}} = \frac{\text{Re}\{i_1 i_2^*\}}{\text{Im}\{i_1 i_2^*\}} = 2\frac{2\pi}{\lambda} \Delta R$$

Deterministic !!!

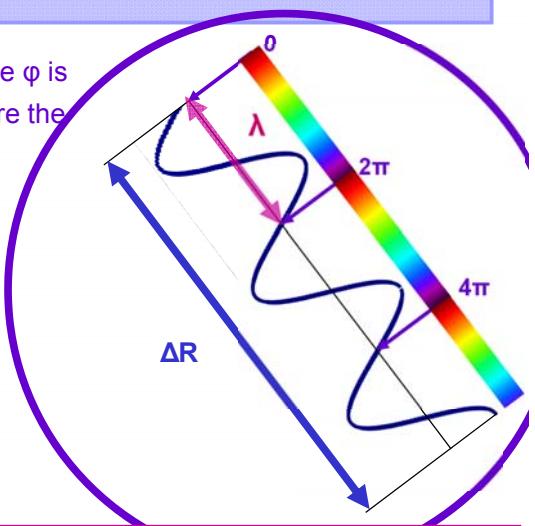


SAR Interferometry



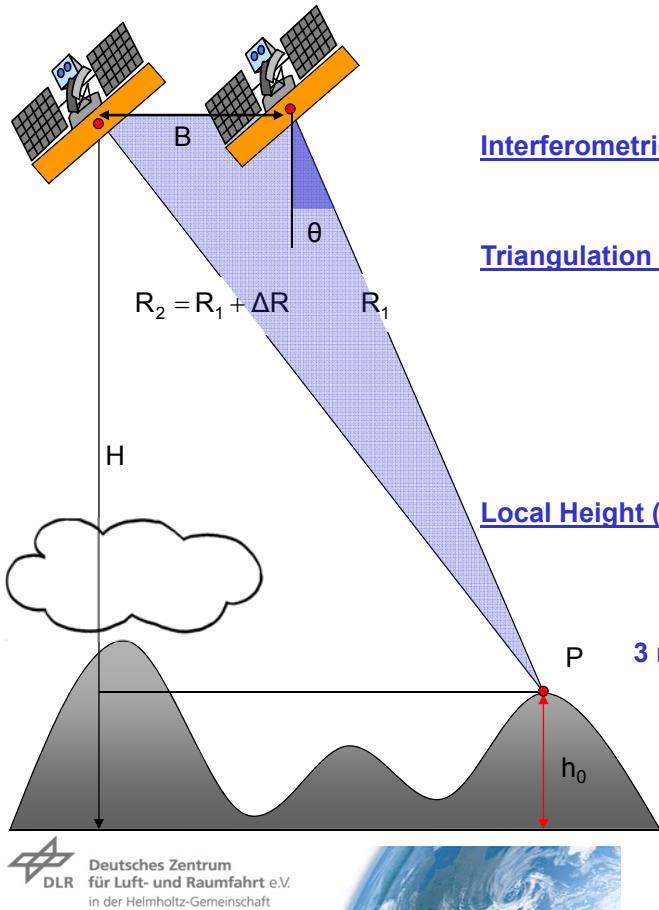
Interferometric Phase: $\phi = 2\frac{2\pi}{\lambda} \Delta R$

The interferometric phase ϕ is another way to measure the (relative) distance ΔR :



Phase measurements in interferometric systems can be made with a degree level accuracy. At radar wavelengths of 1-90cm (Ku to P-band) this corresponds to millimeter accuracy !!!

DEM Generation



$$\text{Interferometric Phase (1): } \varphi = 2\frac{2\pi}{\lambda} \Delta R + 2\pi N \quad N = 0, \pm 1, \pm 2$$

$$\text{Triangulation (2): } (R_1 + \Delta R)^2 = R_1^2 + B^2 - 2R_1 B \cos(\pi/2 + \theta) \rightarrow$$

$$\rightarrow \sin(\theta) = \frac{(R_1 + \Delta R)^2 - R_1^2 - B^2}{2R_1 B}$$

$$\text{Local Height (3): } h_0 = H - (R_1 + \Delta R) \cos(\theta)$$



3 non-linear Equations for 3 Unknowns ($h_0, \theta, \Delta R$)

B ... Spatial baseline and

R_1 ... Range distance in Image 1 are known

Critical is the fact that the interferometric phase φ is initially measured modulo 2π ► Phase Unwrapping

ERS – Bachu / China ~ 100 km × 80 km



Amplitude Image 1



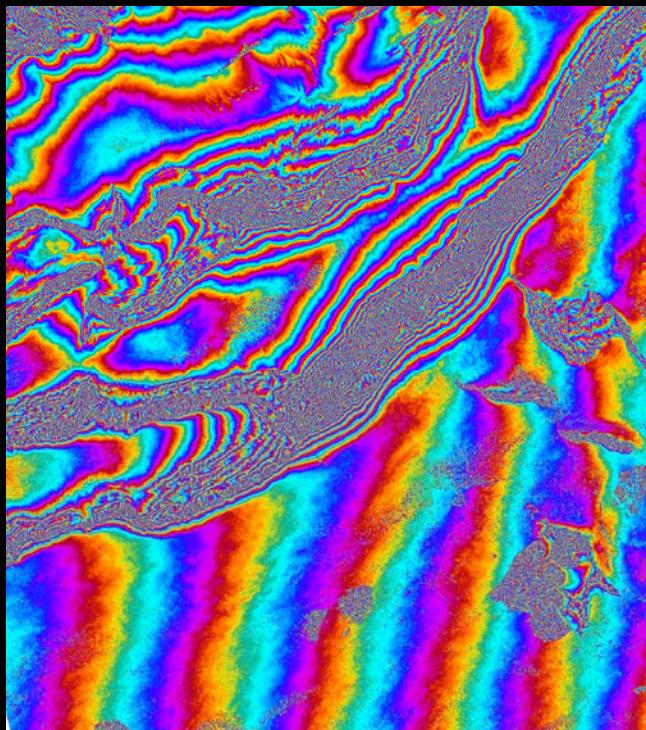
Amplitude Image 2



ERS – Bachu / China ~ 100 km × 80 km



Amplitude Image 1



Interferometric Phase Image



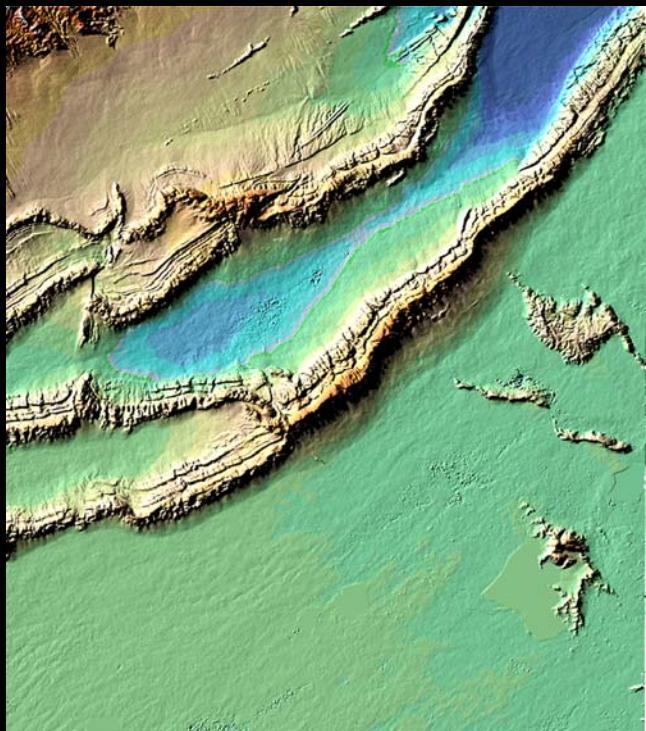
Deutsches Zentrum
für Luft- und Raumfahrt e.V.
in der Helmholtz-Gemeinschaft



ERS – Bachu / China ~ 100 km × 80 km



Amplitude Image

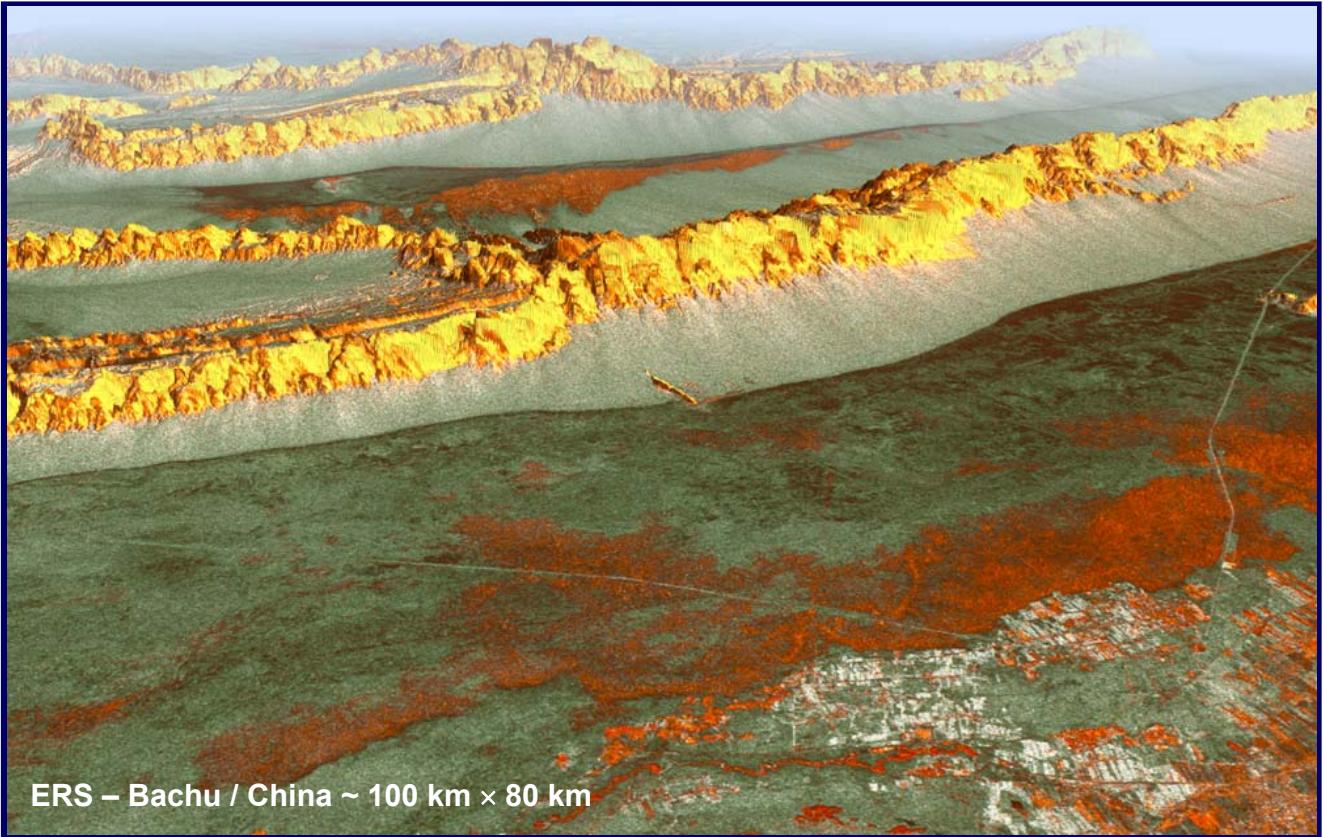


Digital Elevation Model with false colors

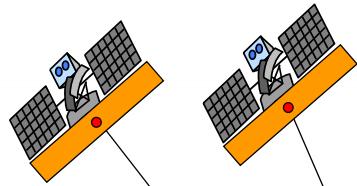


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 Deutsches Zentrum
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in der Helmholtz-Gemeinschaft



Interferometric Coherence

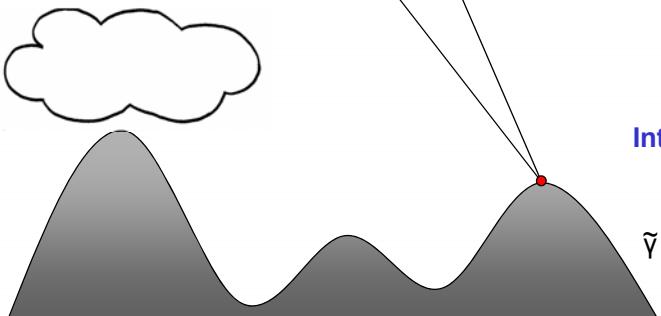


$$\text{Image 1: } i_1 = |i_1| \exp[-i(2\frac{2\pi}{\lambda} R_1) + \phi_{S1}]$$

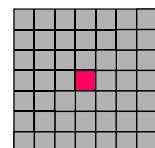
$$\text{Image 2: } i_2 = |i_2| \exp[-i(2\frac{2\pi}{\lambda} R_2) + \phi_{S2}]$$

Interferometric Coherence: Normalised Complex Correlation Coefficient

$$\tilde{\gamma} = \frac{E\{ i_1 i_2^* \}}{\sqrt{E\{ i_1 i_1^* \} E\{ i_2 i_2^* \}}} = \frac{|E\{ i_1 i_2^* \}| \exp(i\varphi)}{\sqrt{E\{ |i_1|^2 \} E\{ |i_2|^2 \}}} \quad 0 \leq |\tilde{\gamma}| \leq 1$$



Interferometric Coherence Estimation:



$$\tilde{\gamma} = \frac{\sum_w i_1[i,j] i_2^*[i,j]}{\sqrt{\sum_w |i_1[i,j]|^2 \sum_w |i_2[i,j]|^2}} = \frac{\langle i_1 i_2^* \rangle}{\sqrt{\langle i_1 i_1^* \rangle \langle i_2 i_2^* \rangle}}$$

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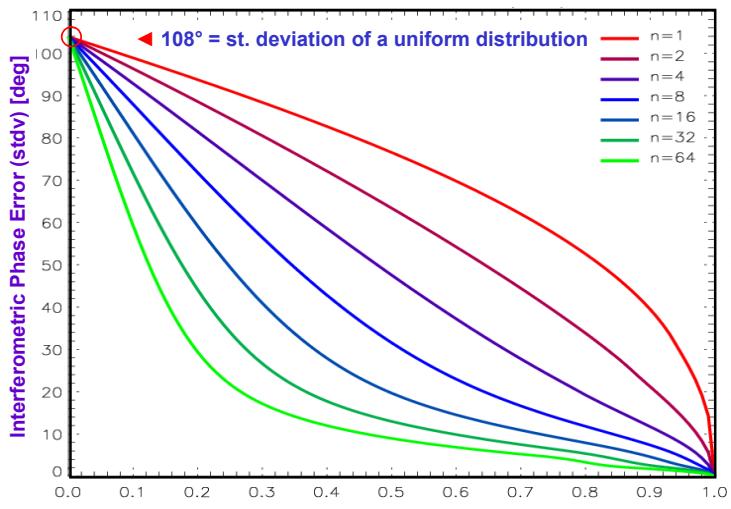
Interferometric coherence

... as a Measure of Interferogram Quality:

Standard Deviation of the InSAR Phase ϕ :

$$\sigma_\phi = \sqrt{\int_{-\pi}^{\pi} \phi^2 \text{pdf}(\phi) \cdot d\phi}$$

- depends on ▶ the underlying coherence &
- ▶ the number of looks N.

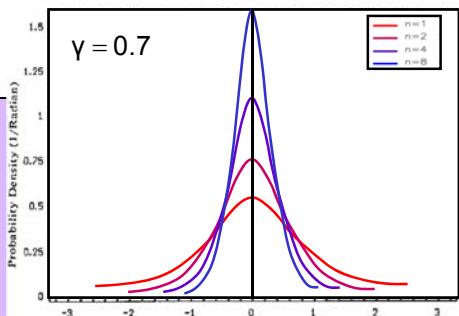


A increase in decorrelation (= loss in coherence) is associated with an increase in the phase variance;

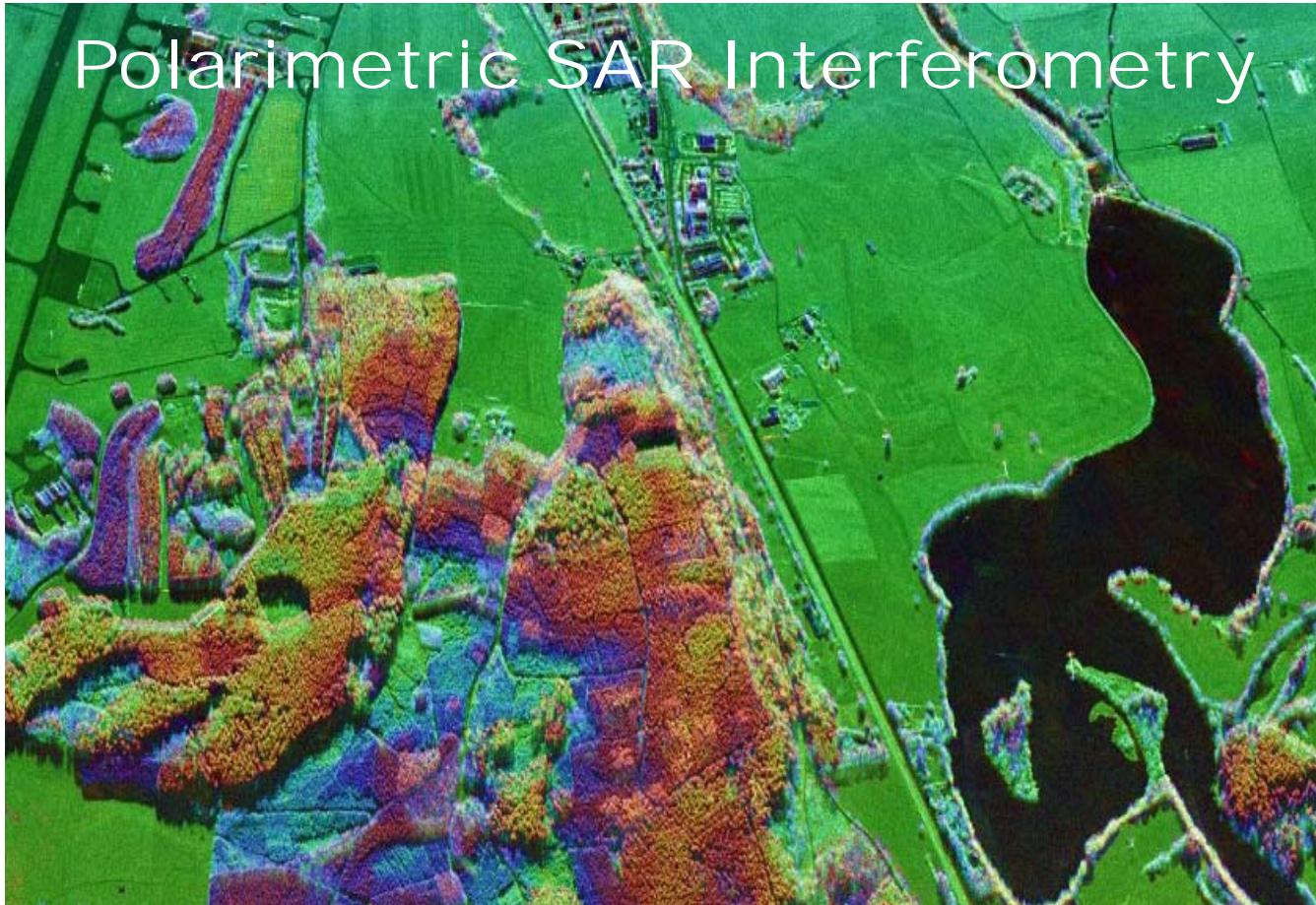
- ▶ Increased phase variance leads to increased height errors.

where: $\text{pdf}(\phi, N) = \frac{\Gamma(N+1/2)(1-|\gamma|^2)^2 \beta}{2\sqrt{\pi}\Gamma(N)(1-\beta^2)^{N+1/2}} + \frac{(1-|\gamma|^2)^N}{2\pi} F(N, 1/2; \beta^2)$

- ▶ F is a Gauss hypergeometric function and $\beta = |\gamma| \cos(\phi - \bar{\phi})$
- ▶ N is the number of Looks



Polarimetric SAR Interferometry





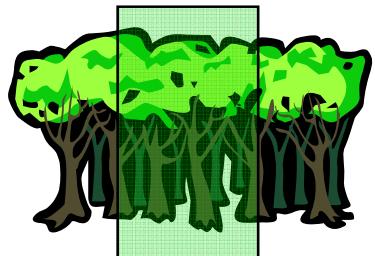
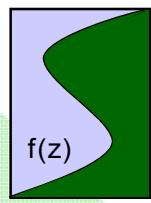
Interferometric Coherence

$$\tilde{\gamma}(S_1 S_2) = \frac{< S_1 S_2^* >}{\sqrt{< S_1 S_1^* > < S_2 S_2^* >}}$$

SAR Interferometry for Volume Structure

Volume Coherence

$$\tilde{\gamma}_{Vol}(f(z)) = e^{ik_z z_o} \frac{\int_{h_v}^{h_v} f(z) e^{ik_z z} dz}{\int_0^{h_v} f(z) dz}$$



$f(z)$... vertical reflectivity function

$$\text{Vertical Wavenumber: } k_z = \frac{\kappa \Delta \theta}{\sin(\theta_0)}$$

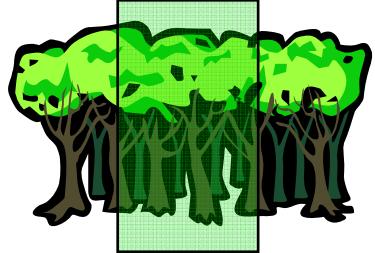
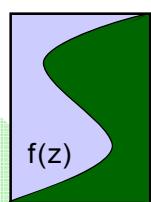
$$\tilde{\gamma} = \tilde{\gamma}_{Temporal} \quad \gamma_{SNR} \quad \tilde{\gamma}_{Volume}$$

- $\tilde{\gamma}_{Temporal}$... temporal decorrelation
- γ_{SNR} ... additive noise decorrelation
- $\tilde{\gamma}_{Volume}$... geometric decorrelation

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in der Helmholtz-Gemeinschaft

Baseline 3

$$\tilde{\gamma}_{Vol}(k_{z3}) = e^{ik_z z_o} \frac{\int_{h_v}^{h_v} f(z) e^{ik_z z} dz}{\int_0^{h_v} f(z) dz}$$



$f(z)$... vertical reflectivity function

$$\text{Vertical Wavenumber: } k_z = \frac{\kappa \Delta \theta}{\sin(\theta_0)}$$

Baseline 2

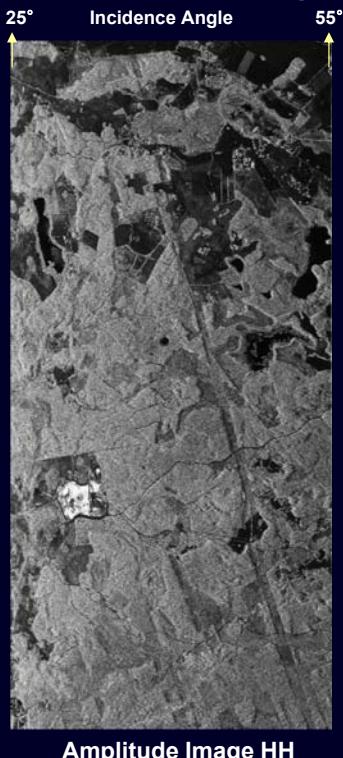
$$\tilde{\gamma}_{Vol}(k_{z1}) = e^{ik_z z_o} \frac{\int_{h_v}^{h_v} f(z) e^{ik_z z} dz}{\int_0^{h_v} f(z) dz}$$



Multibaseline SAR Interferometry

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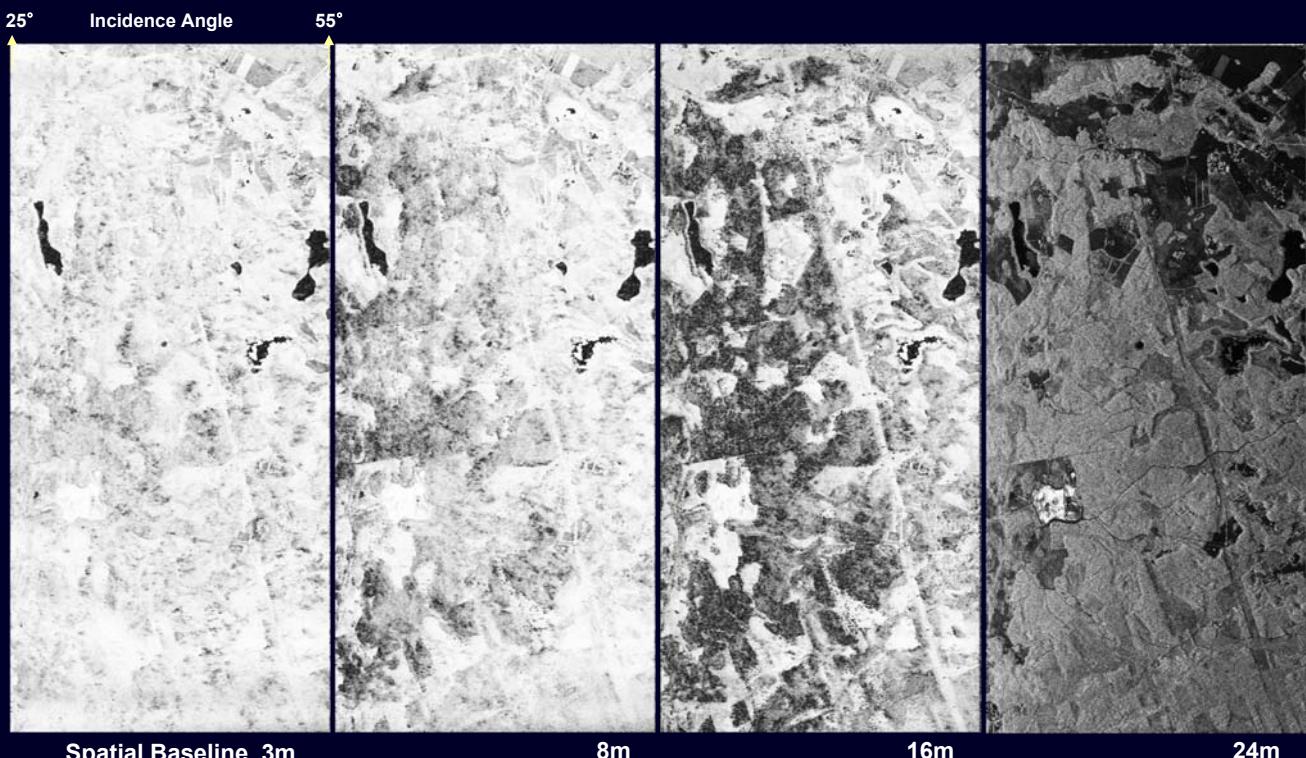
Amplitude Image



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Interferometric Coherence: Volume Decorrelation



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Polarimetric SAR Interferometry

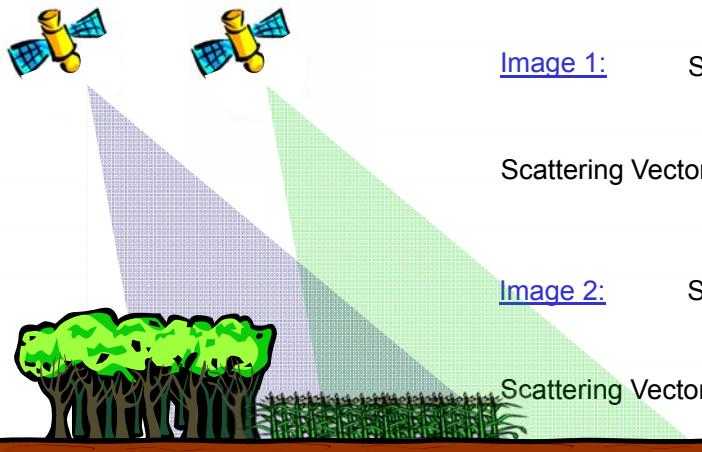


Image 1: Scattering Matrix: $[S_1] = \begin{bmatrix} S_{HH}^1 & S_{HV}^1 \\ S_{VH}^1 & S_{VV}^1 \end{bmatrix}$

$$\text{Scattering Vector: } \vec{k}_1 = \frac{1}{\sqrt{2}} [S_{HH}^1 + S_{VV}^1 \quad S_{HH}^1 - S_{VV}^1 \quad 2S_{HV}^1]^T$$

Image 2: Scattering Matrix: $[S_2] = \begin{bmatrix} S_{HH}^2 & S_{HV}^2 \\ S_{VH}^2 & S_{VV}^2 \end{bmatrix}$

$$\text{Scattering Vector: } \vec{k}_2 = \frac{1}{\sqrt{2}} [S_{HH}^2 + S_{VV}^2 \quad S_{HH}^2 - S_{VV}^2 \quad 2S_{HV}^2]^T$$

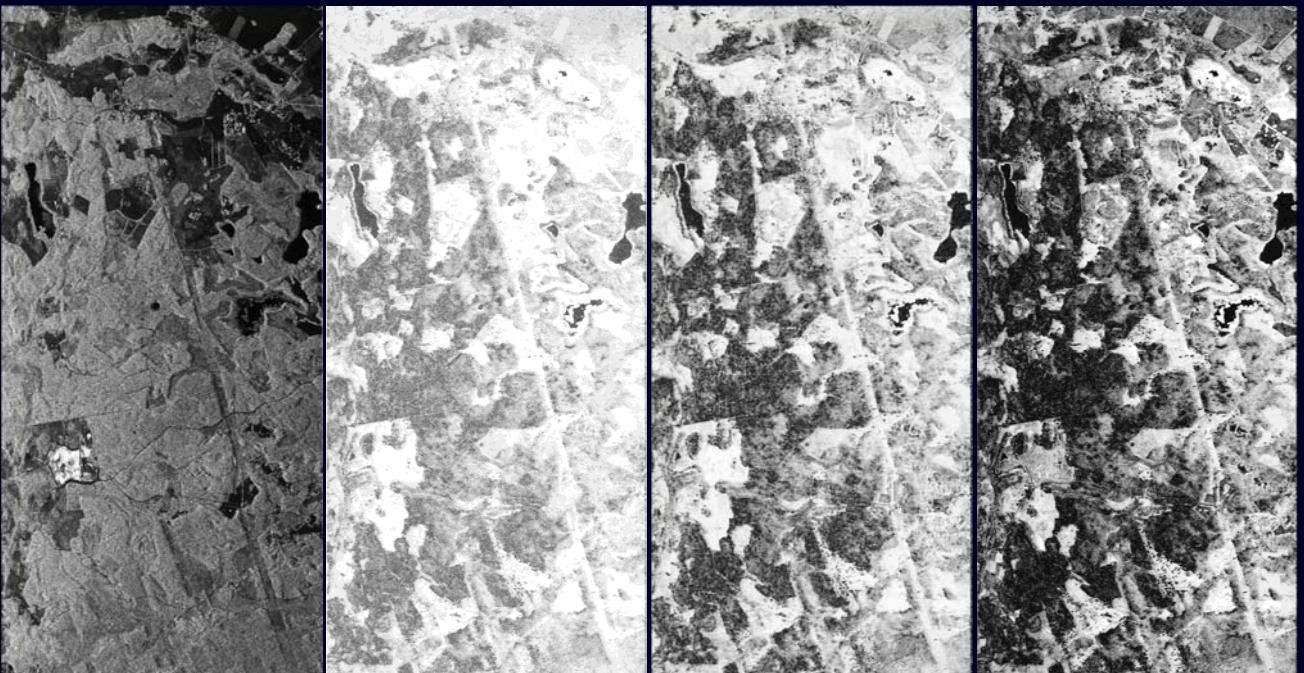
Image formation: $i_1 = \vec{w}_1^+ \cdot \vec{k}_1$ and $i_2 = \vec{w}_2^+ \cdot \vec{k}_2$ where \vec{w}_i are complex unitary vectors

Interferogram formation: $i_1 i_2^* = (\vec{w}_1^+ \cdot \vec{k}_1)(\vec{w}_2^+ \cdot \vec{k}_2)^* = \vec{w}_1^+ (\vec{k}_1 \cdot \vec{k}_2^+) \vec{w}_2 = \vec{w}_1^+ [\Omega] \vec{w}_2$

$$\text{Interferometric Coherence: } \tilde{\gamma}(\vec{w}_1, \vec{w}_2) = \frac{\langle i_1 i_2^* \rangle}{\sqrt{\langle i_1 i_1^* \rangle \langle i_2 i_2^* \rangle}} = \frac{\langle \vec{w}_1^+ [\Omega] \vec{w}_2 \rangle}{\sqrt{\langle (\vec{w}_1^+ [\Omega] \vec{w}_1) \rangle \langle (\vec{w}_2^+ [\Omega] \vec{w}_2) \rangle}}$$



Interferometric Coherence: Volume Decorrelation



Amplitude Image HH

Sp. Baseline 16m

Opt 1

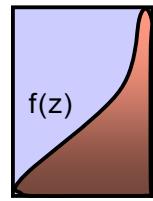
HH

Opt 3



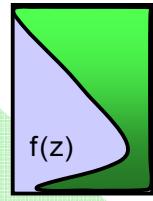
Polarisation 3

$$\tilde{Y}_{Vol}(f(z)) = e^{ik_z z_0} \frac{\int_{h_v}^{h_v} f(z) e^{ik_z z} dz}{\int_0^{h_v} f(z) dz}$$



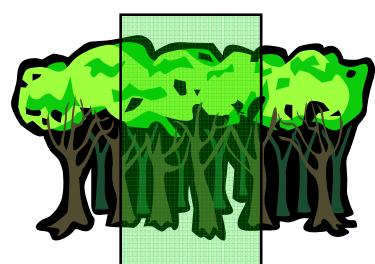
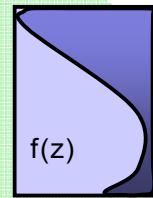
Polarisation 1

$$\tilde{Y}_{Vol}(f(z)) = e^{ik_z z_0} \frac{\int_0^{h_v} f(z) e^{ik_z z} dz}{\int_0^{h_v} f(z) dz}$$



Polarisation 2

$$\tilde{Y}_{Vol}(f(z)) = e^{ik_z z_0} \frac{\int_0^{h_v} f(z) e^{ik_z z} dz}{\int_0^{h_v} f(z) dz}$$

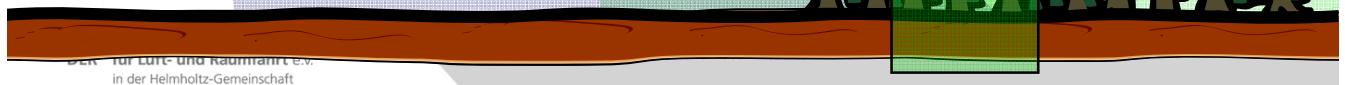


Vertical reflectivity function

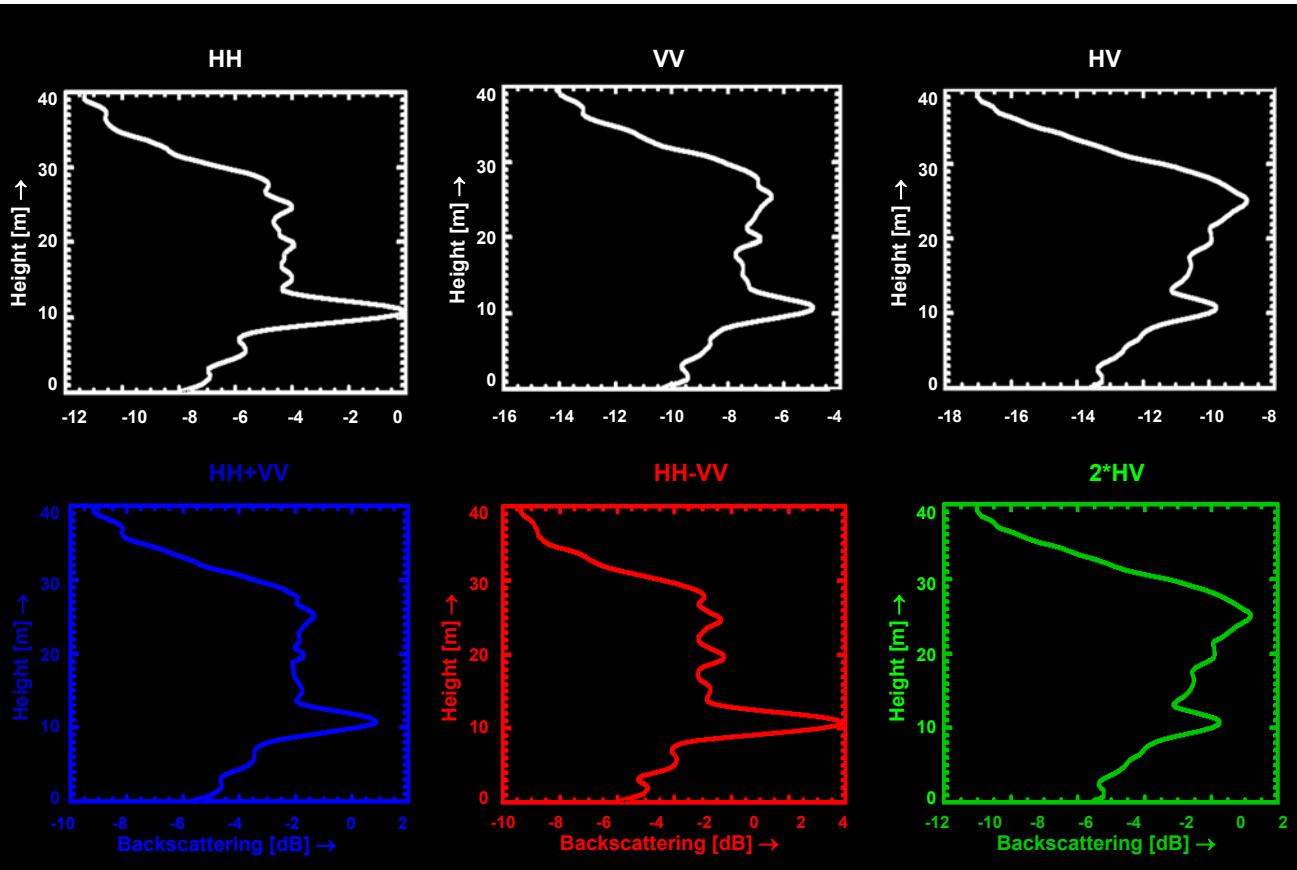
Wavenumber: $\kappa_z = \frac{\kappa \Delta \theta}{\sin(\theta_0)}$

$f(z)$... vertical reflectivity function

Polarimetric SAR Interferometry



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Structure Parameters & Applications

Forest

- Forest Height
- Forest (Vertical) Structure
- Forest Biomass
- Underlying Topography

- Forest Ecology
- Forest Management
- Ecosystem Modeling
- Climate Change

Agriculture

- Underlying Soil Moisture
- Moisture of Vegetation Layer
- Height of Vegetation Layer
- Soil Roughness

- Farming Management
- Ecosystem Modeling
- Water Cycle / CC
- Desertification

Snow & Ice

- Ice Layer Structure
- Penetration Depth (Ice)
- Snow Layer Thickness
- Snow Water Equivalent

- Ecosystem Change
- Water Cycle
- Water Management



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Essential Climate Variables

Pol-InSAR In Orbit

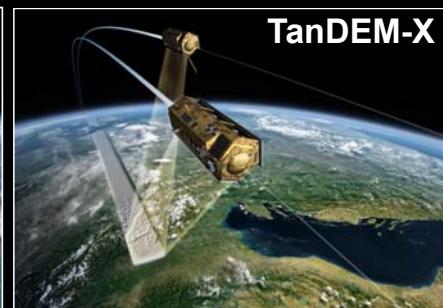
ALOS-PalSAR



RadarSAT 2



TanDEM-X



ALOS-2



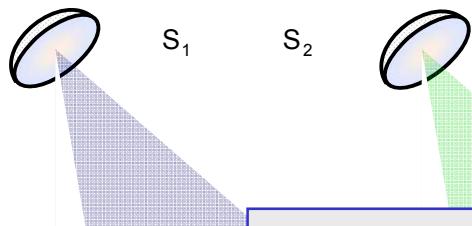
biomass



Tandem-L



Deutsches Zentrum
für Luft- und Raumfahrt e.V.
in der Helmholtz-Gemeinschaft

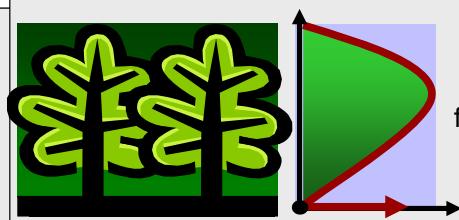
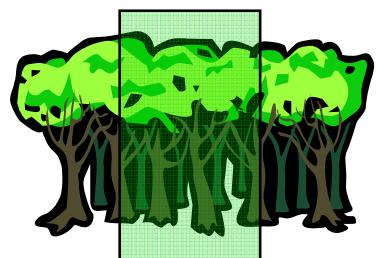
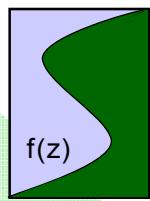


Interferometric Coherence

$$\tilde{\gamma}(S_1 S_2) = \frac{< S_1 S_2^* >}{\sqrt{< S_1 S_1^* > < S_2 S_2^* >}}$$

Volume Coherence

$$\tilde{\gamma}_{Vol}(f(z)) = e^{ik_z z_0} \frac{\int_{-h_v}^{h_v} f(z) e^{ik_z z} dz}{\int_{-h_v}^{h_v} f(z) dz}$$



$$f(z) = f_0 e^{\left(\frac{2 \sigma(z) z}{\cos \theta_0}\right)} + m'_G \delta(z - z_0)$$

2 Layer Inversion Model

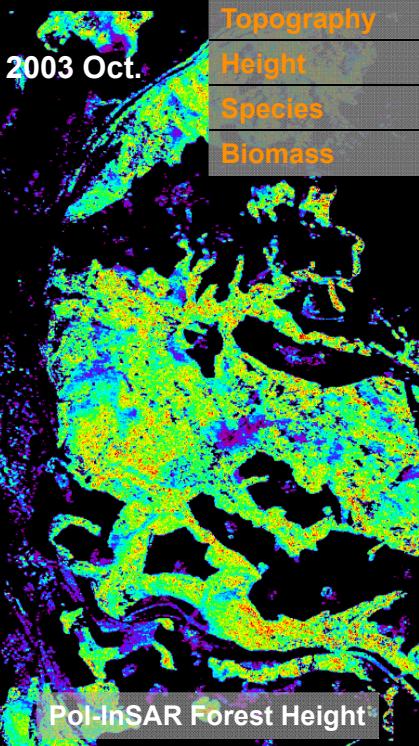
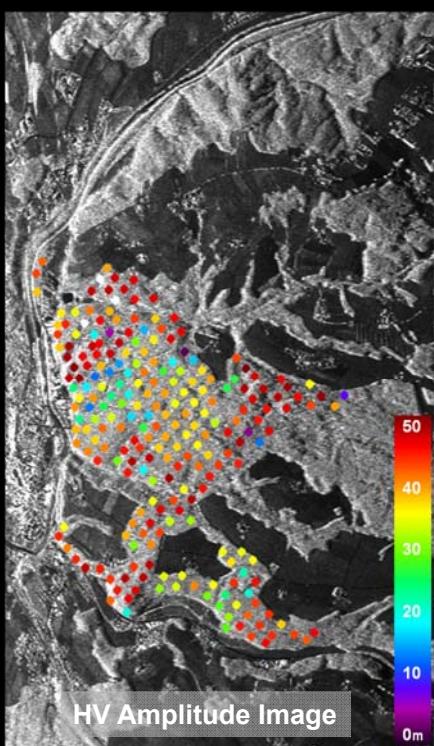
$$\tilde{\gamma}_{Vol}(\bar{w}) = \exp(i\varphi_0) \frac{\tilde{\gamma}_V + m(\bar{w})}{1 + m(\bar{w})}$$

Volume Coherence

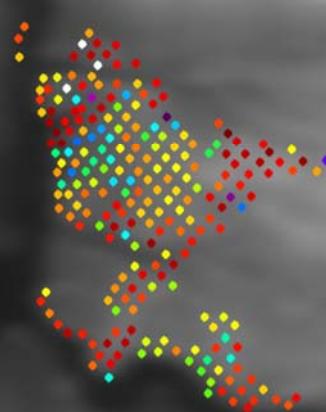
$$\tilde{\gamma}_V = \frac{I}{I_0} \left\{ \begin{array}{l} I = \int_0^{h_v} \exp(i\kappa_z z') \exp\left(\frac{2 \sigma(z) z'}{\cos \theta_0}\right) dz' \\ I_0 = \int_0^{h_v} \exp\left(\frac{2 \sigma(z) z'}{\cos \theta_0}\right) dz' \end{array} \right. \quad m(\bar{w}) = \frac{m_G(\bar{w})}{m_V(\bar{w}) I_0} \quad \kappa_z = \frac{\kappa \Delta \theta}{\sin(\theta_0)}$$

$\sigma(z)$ has to be parameterised
Volume Height h_v
Topography φ_0
G/V Ratio $m(\bar{w})$

Traunstein Test Site

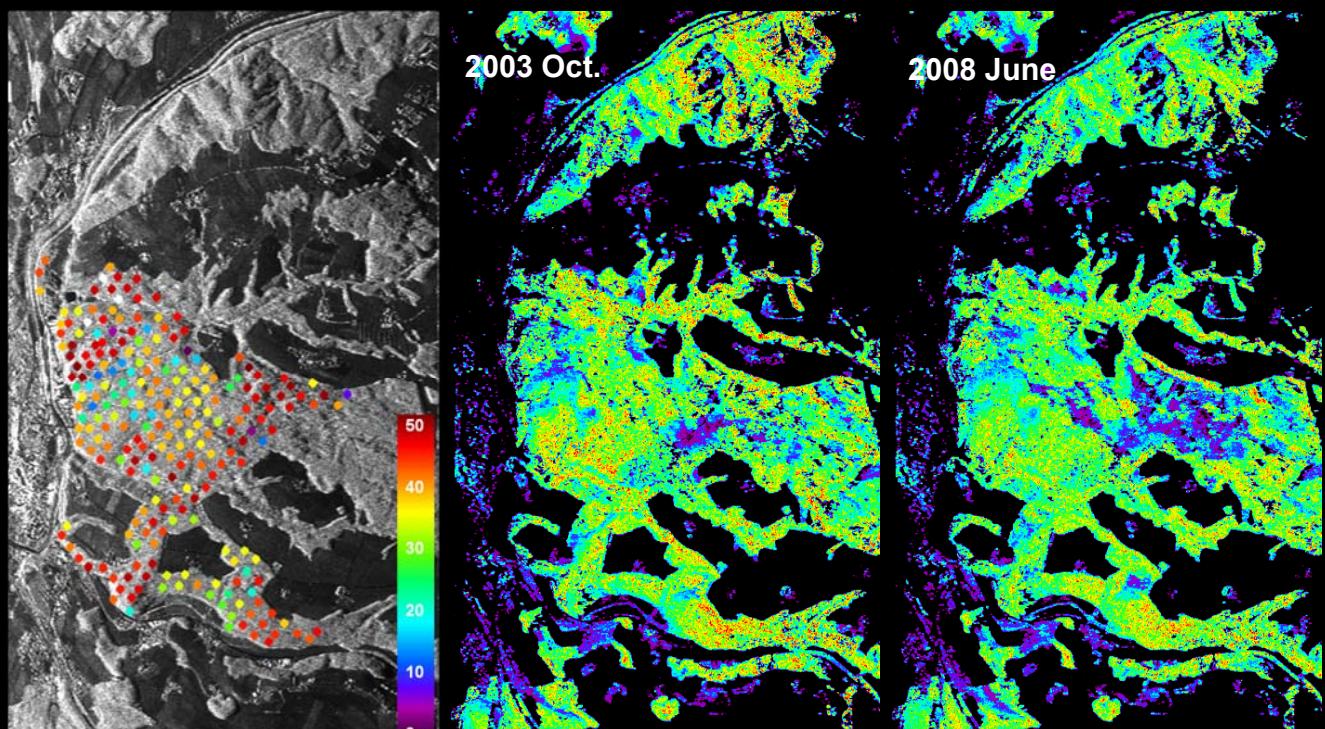


Forest type	Temperate
Topography	Moderate slopes
Height	25 ~ 35m
Species	N. Spruce, E. Beech, White Fir
Biomass	40 ~ 450 t/ha



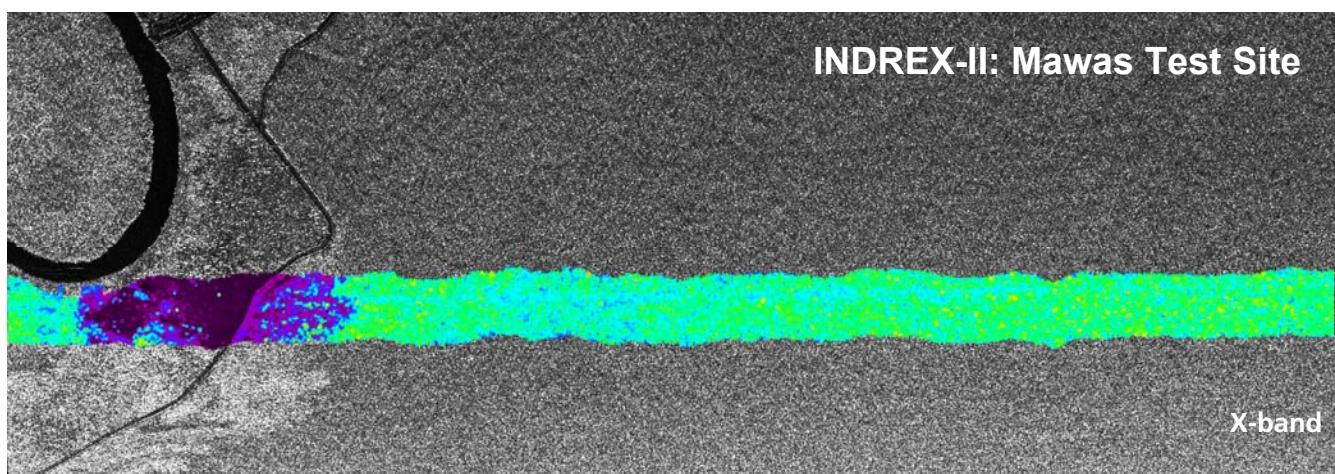
Elevation Model

Traunstein Test Site

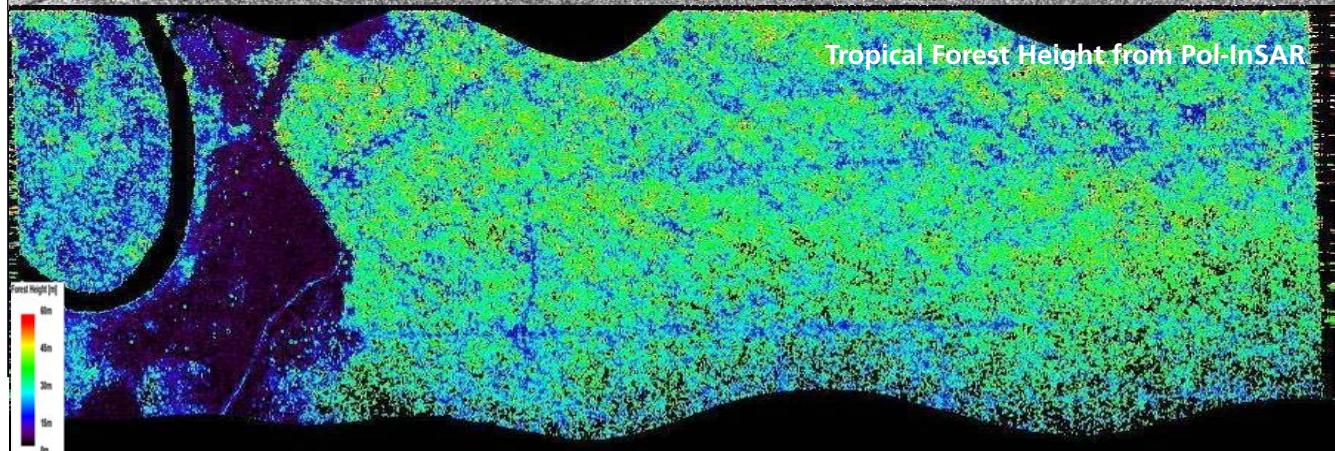


Deutsches Zentrum
für Luft- und Raumfahrt e.V.
in der Helmholtz-Gemeinschaft

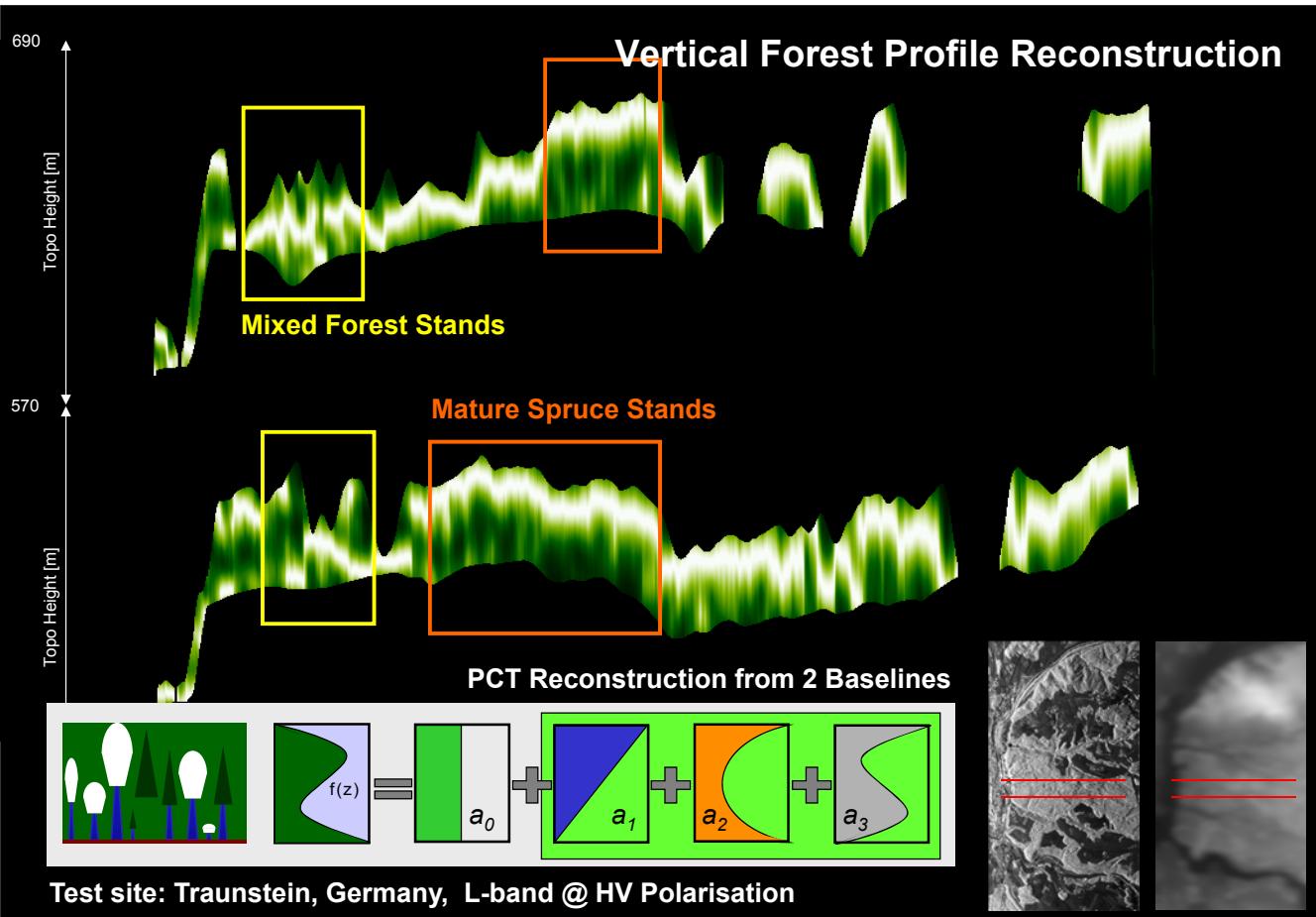
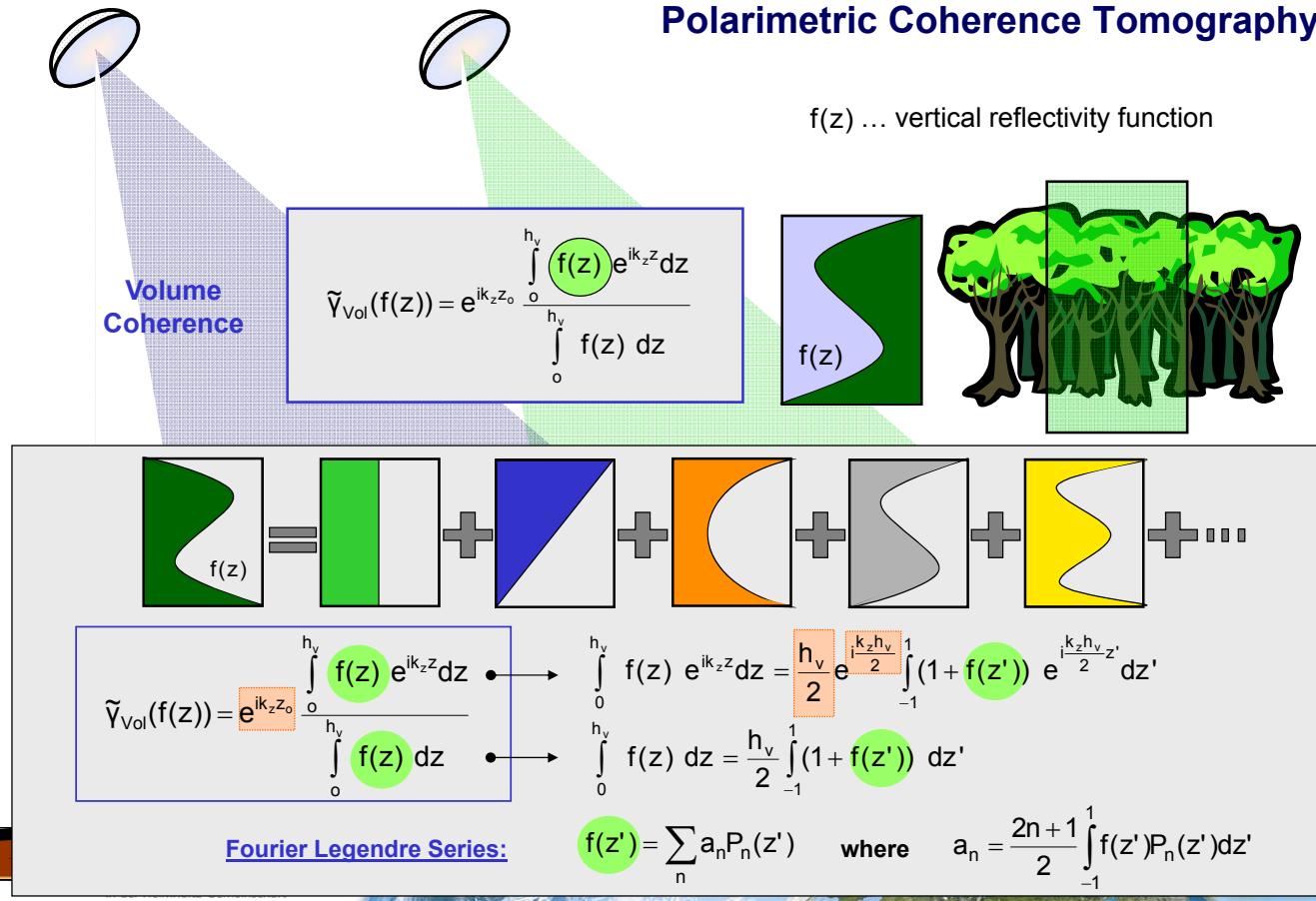
VU 48 > Autor Name



X-band

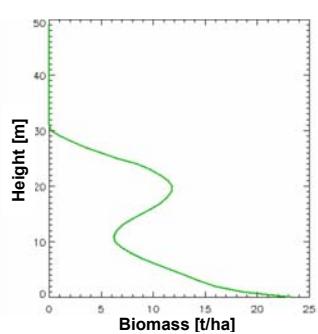


Polarimetric Coherence Tomography

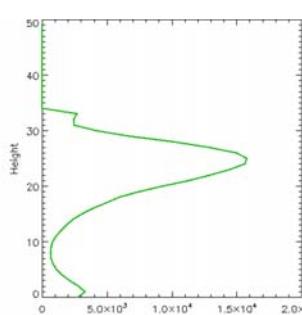


What do we measure ?

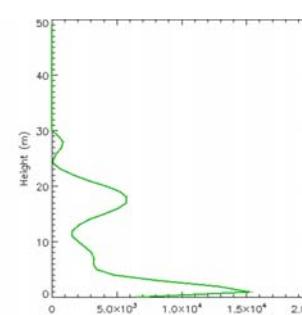
Biomass Profile



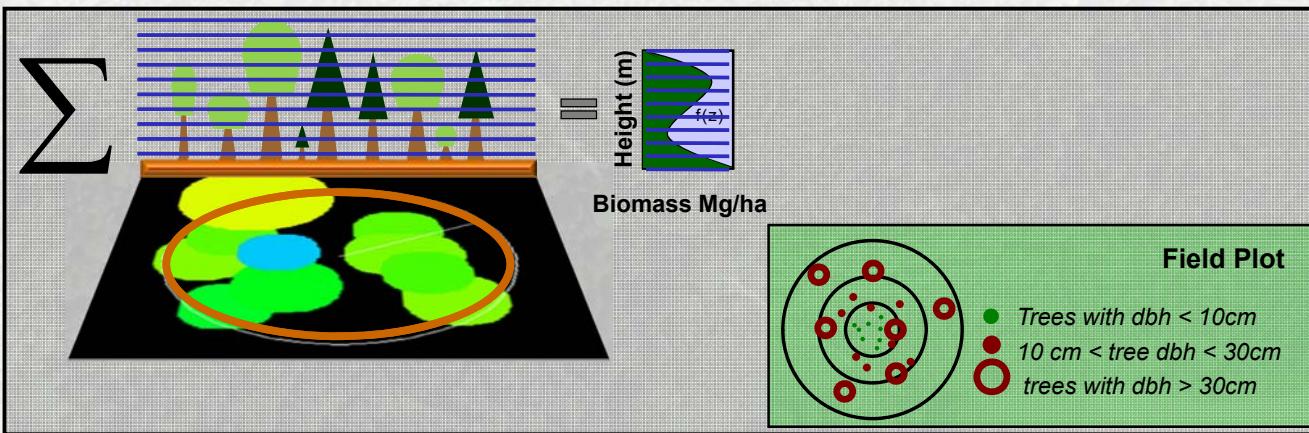
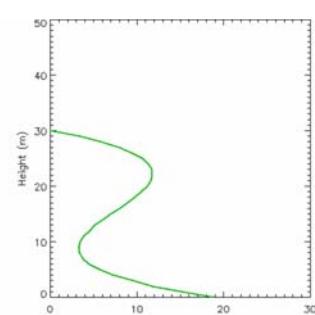
Airborne Lidar Profile



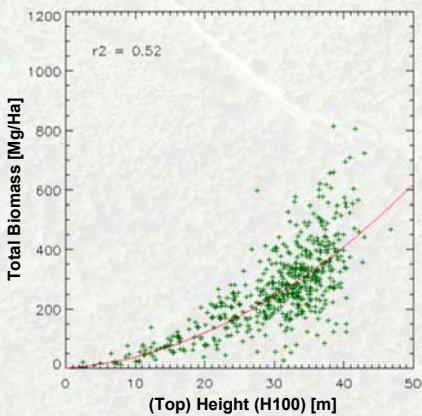
Terrestrial Lidar Profile



L-band Profile

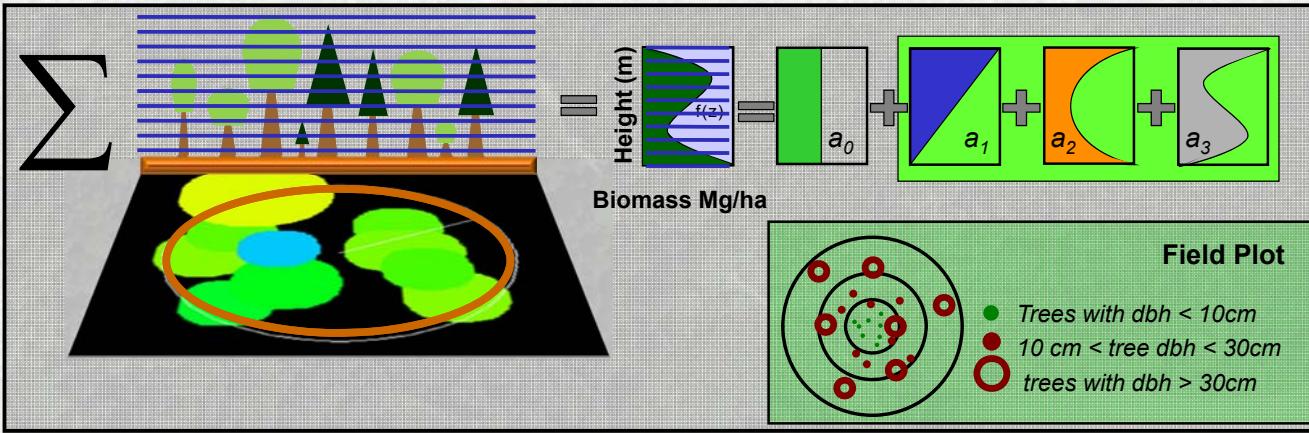
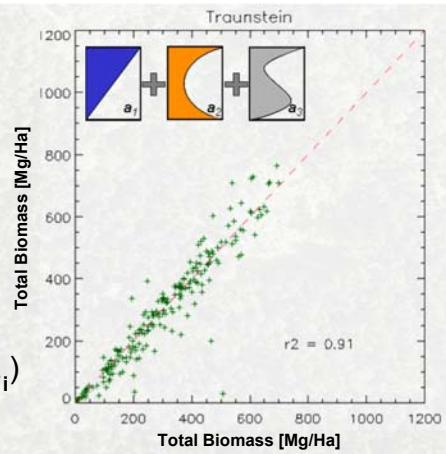


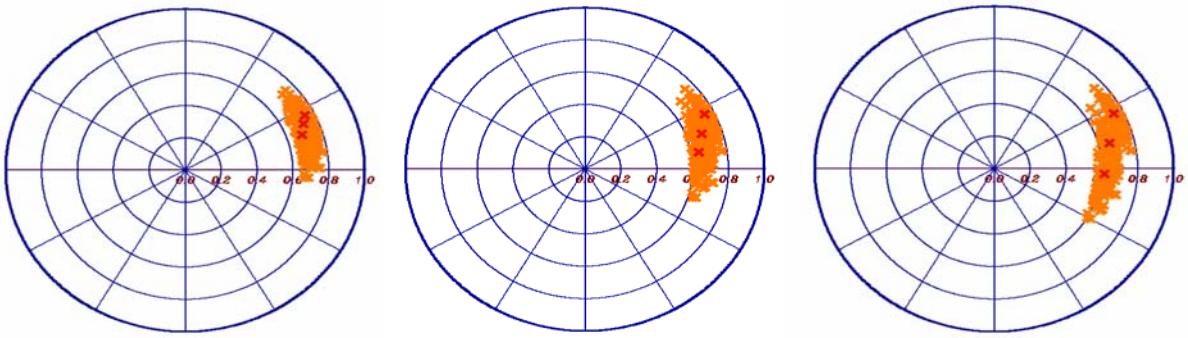
Structure-to-Biomass Allometry



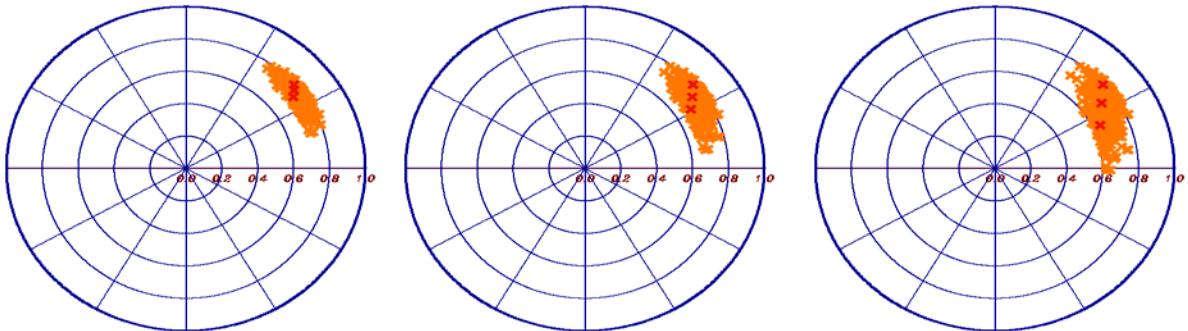
$$B = la * 1.66 H^{1.50}$$

$$B = 3.11 * \sum_{i=0}^H \sum_{j=1}^3 a_j * P_j(z_i)$$

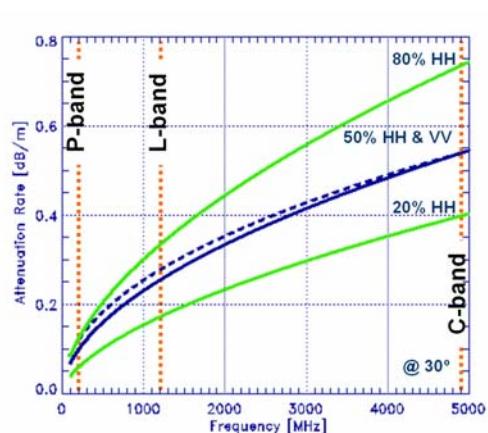




Frequency Effects



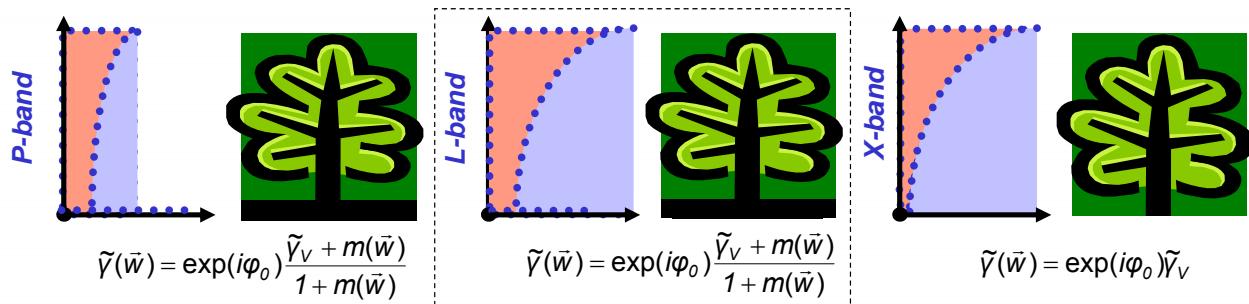
Deutsches Zentrum
für Luft- und Raumfahrt e.V.
in der Helmholtz-Gemeinschaft



RVoG Model – Frequency Dependency

With degreasing frequency:

- The attenuation through the vegetation degreases;
- The Ground to Volume Scattering Ratio increases;
- The relative importance of the volume decreases;
- The relative importance of the ground increases;
- The effective scatterers change.

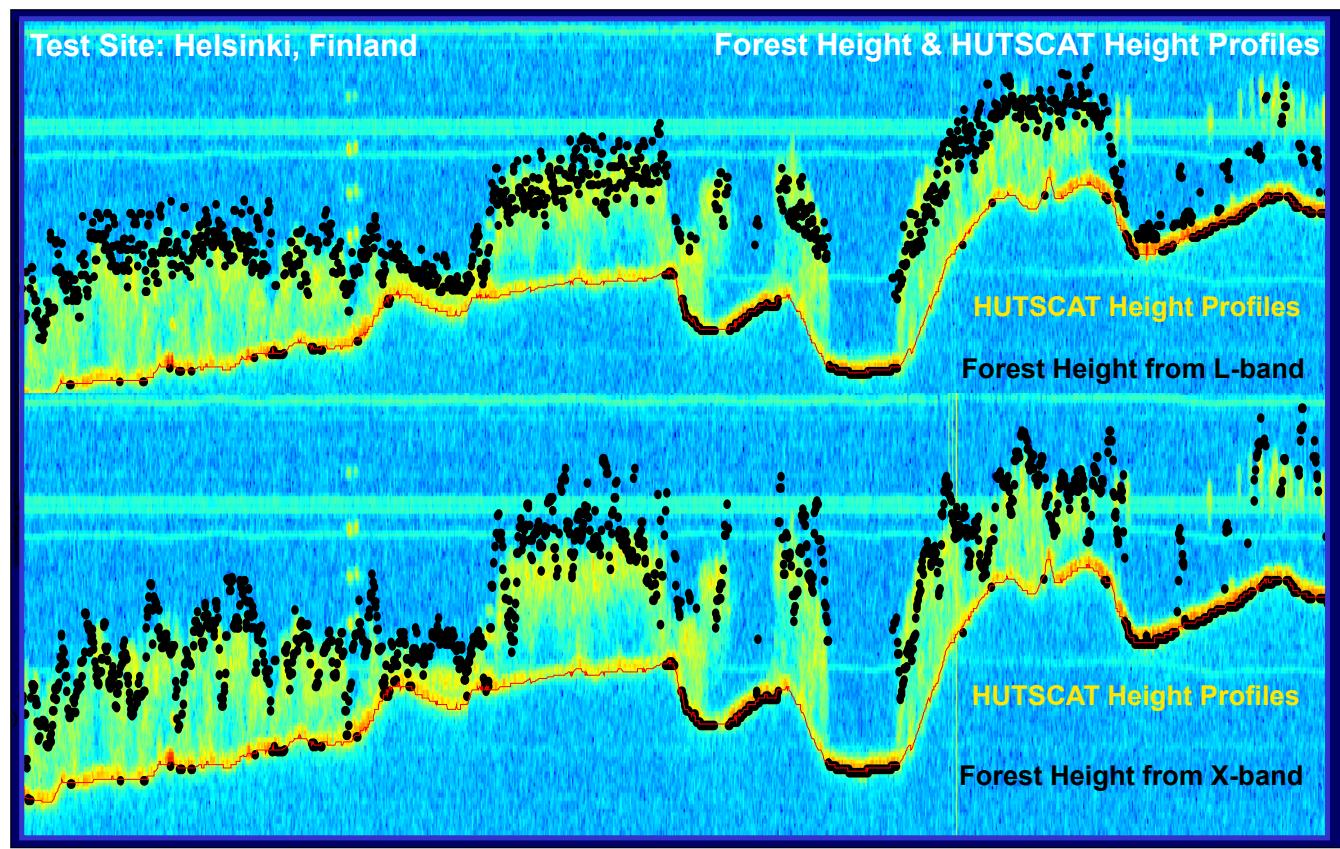
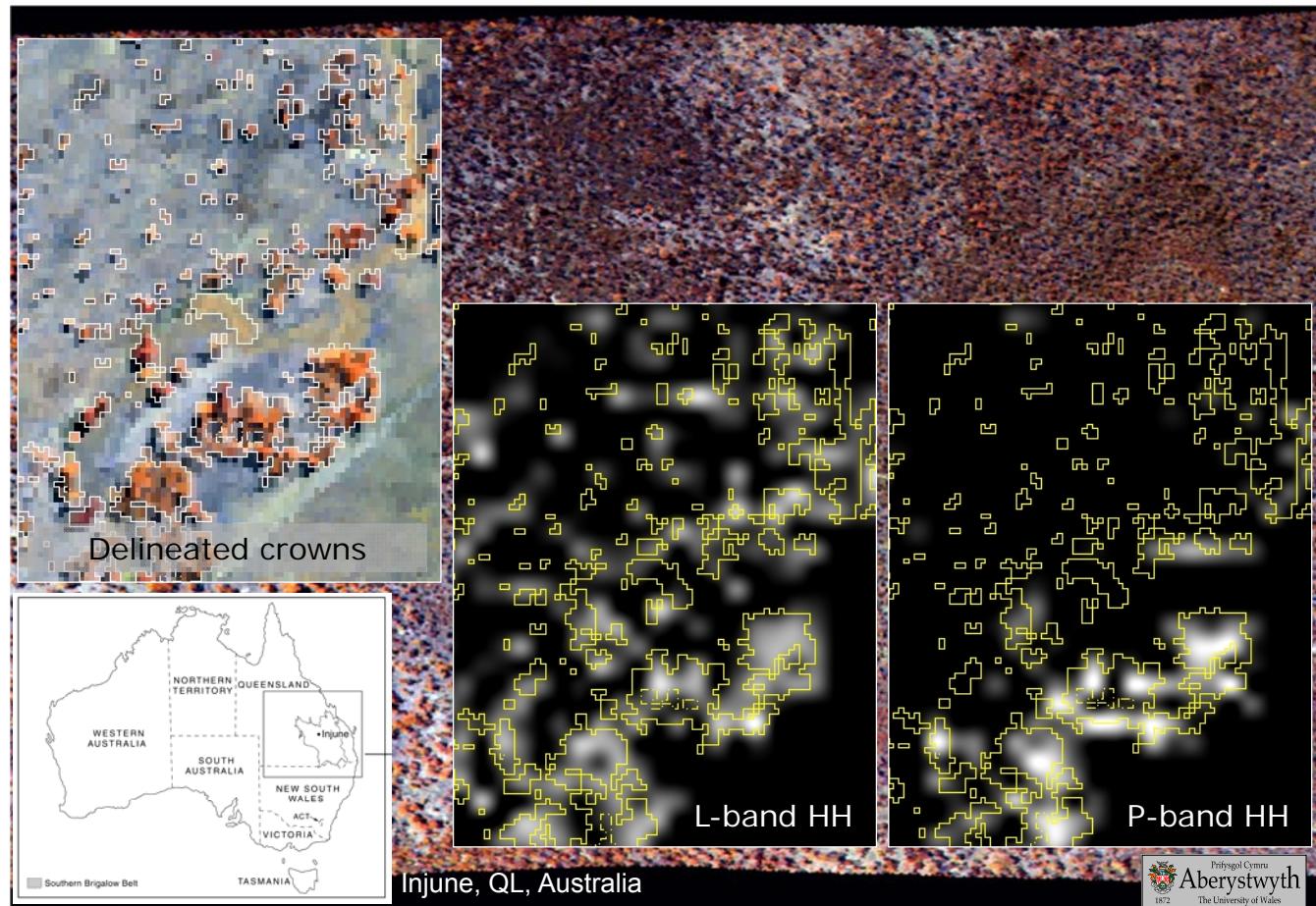


L.Bessette, S.Ayasli "Ultra Wide Band P-3 and Carabas II Foliage Attenuation and Backscatter Analysis", Proceedings of IEEE Radar Conference, 2001.



Deutsches Zentrum
für Luft- und Raumfahrt e.V.
in der Helmholtz-Gemeinschaft

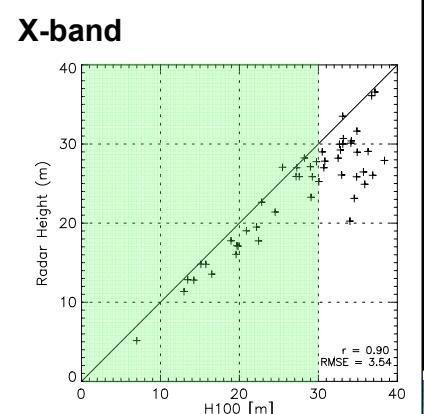
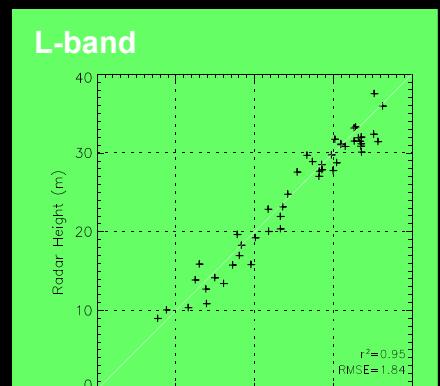
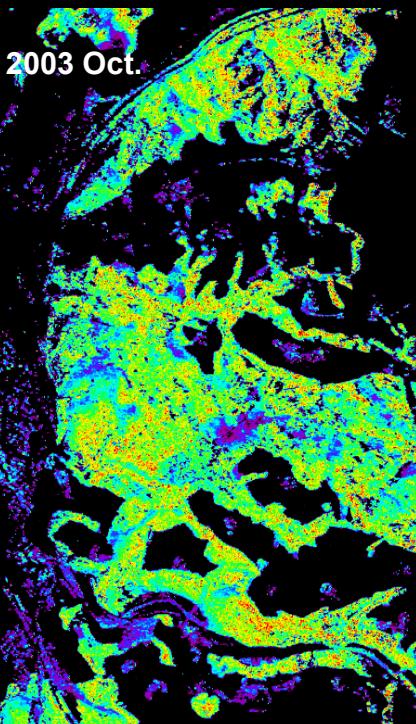
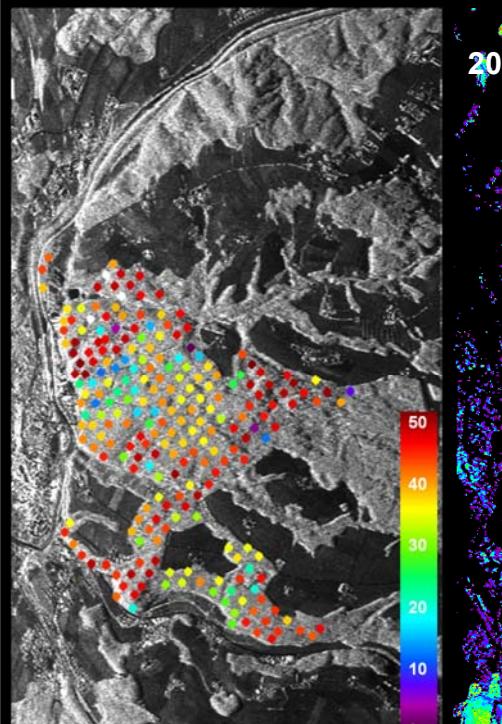




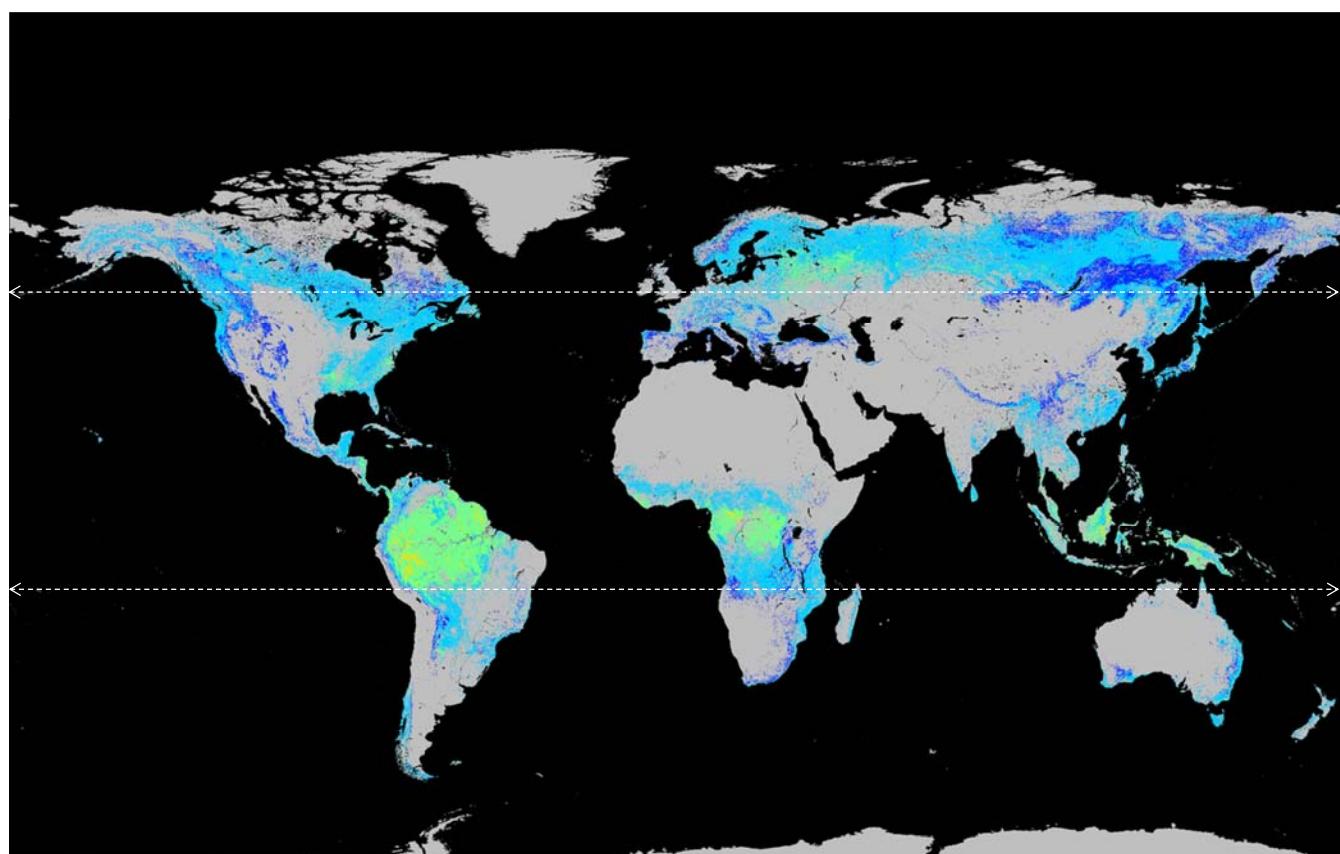
Deutsches Zentrum
für Luft- und Raumfahrt e.V.
in der Helmholtz-Gemeinschaft



Traunstein Test Site



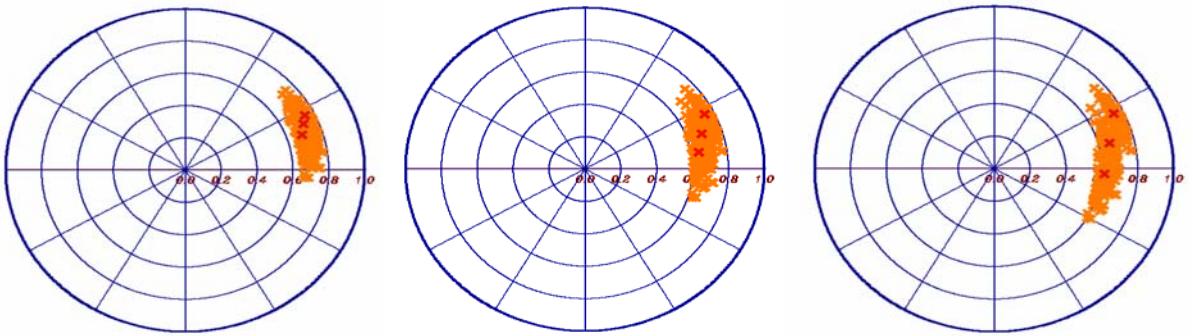
Deutsches Zentrum
für Luft- und Raumfahrt e.V.
in der Helmholtz-Gemeinschaft



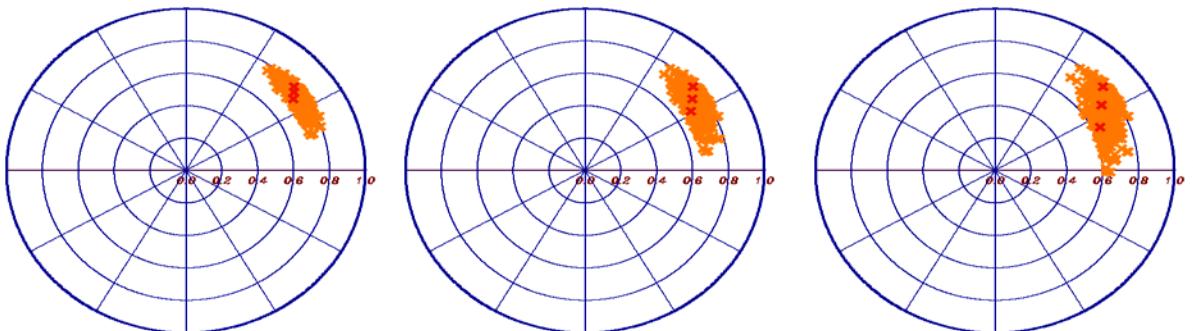
Source: Marc Simard, JPL, NASA



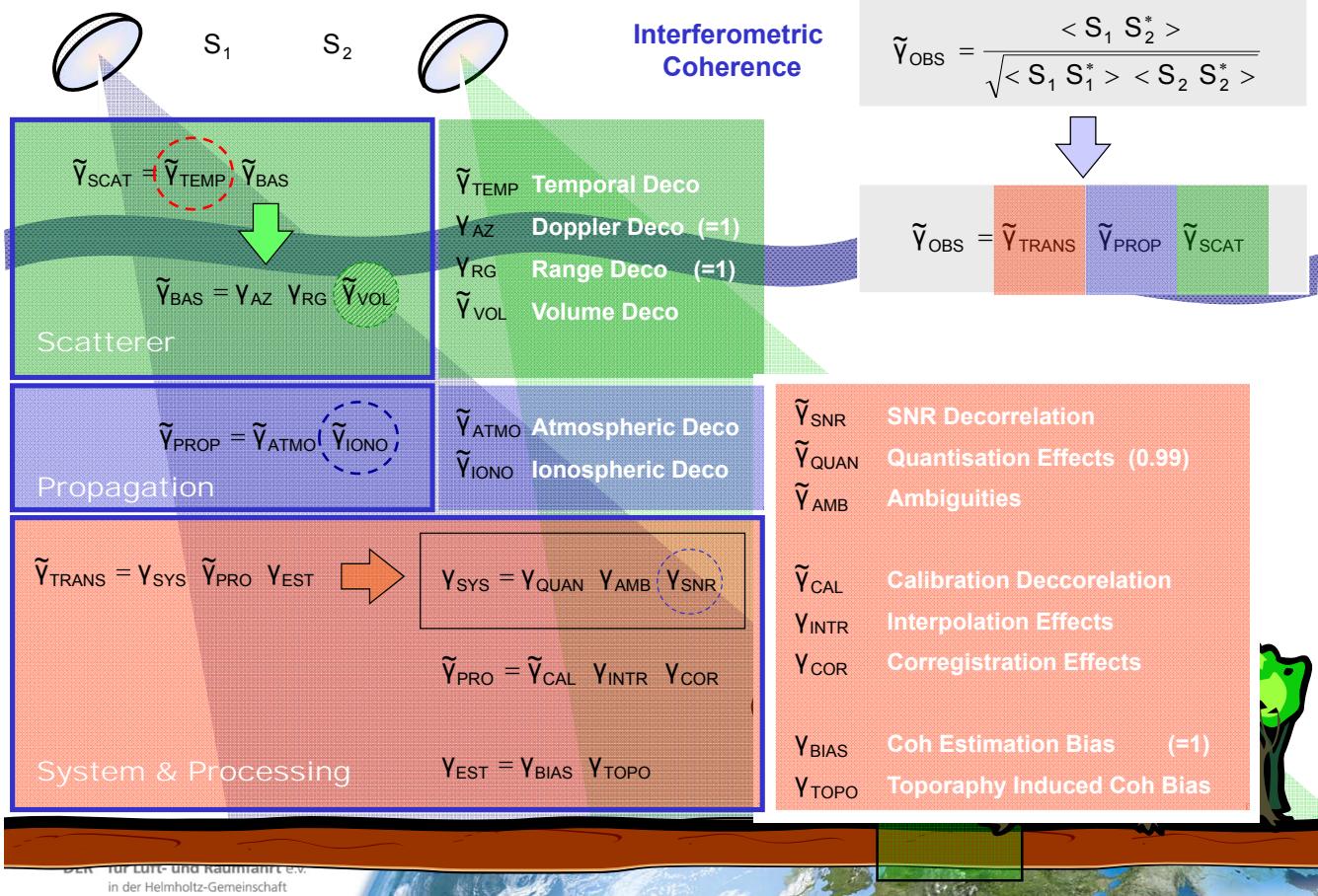
0 10 20 30 40 50 [m]



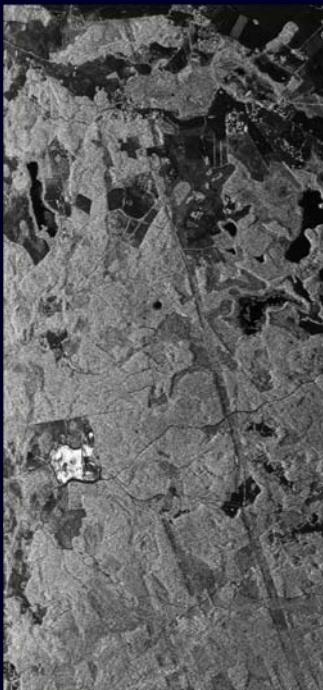
Non-Volumetric Decorrelation Effects



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Amplitude Image



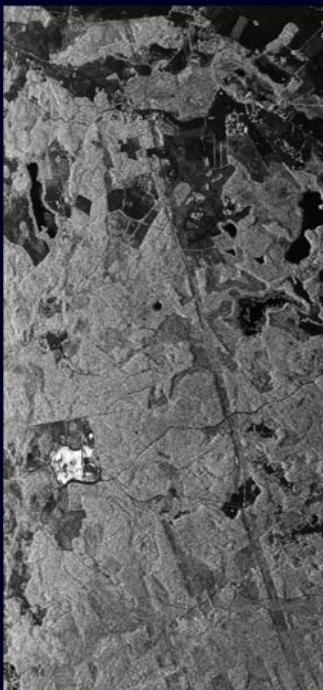
Amplitude Image HH



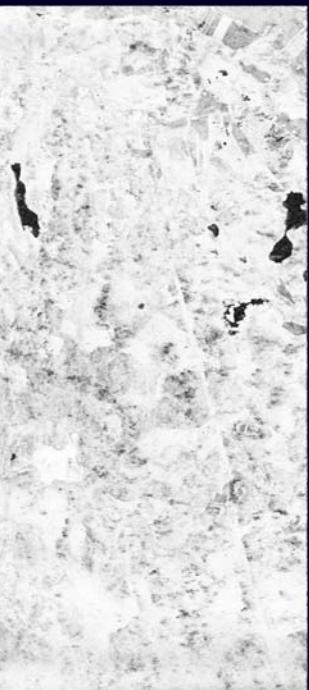
Deutsches Zentrum
für Luft- und Raumfahrt e.V.
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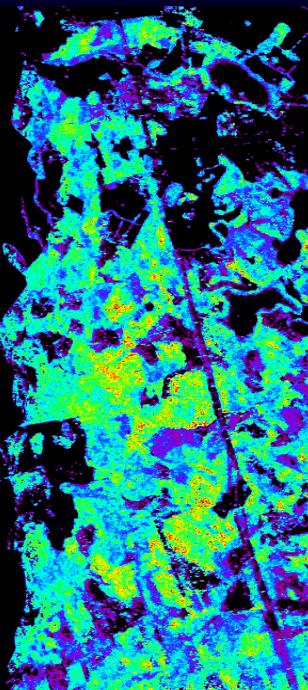
Interferometric Coherence: Volume vs Temporal Decorrelation



Amplitude Image HH



Volume Coherence



Forest Height Map



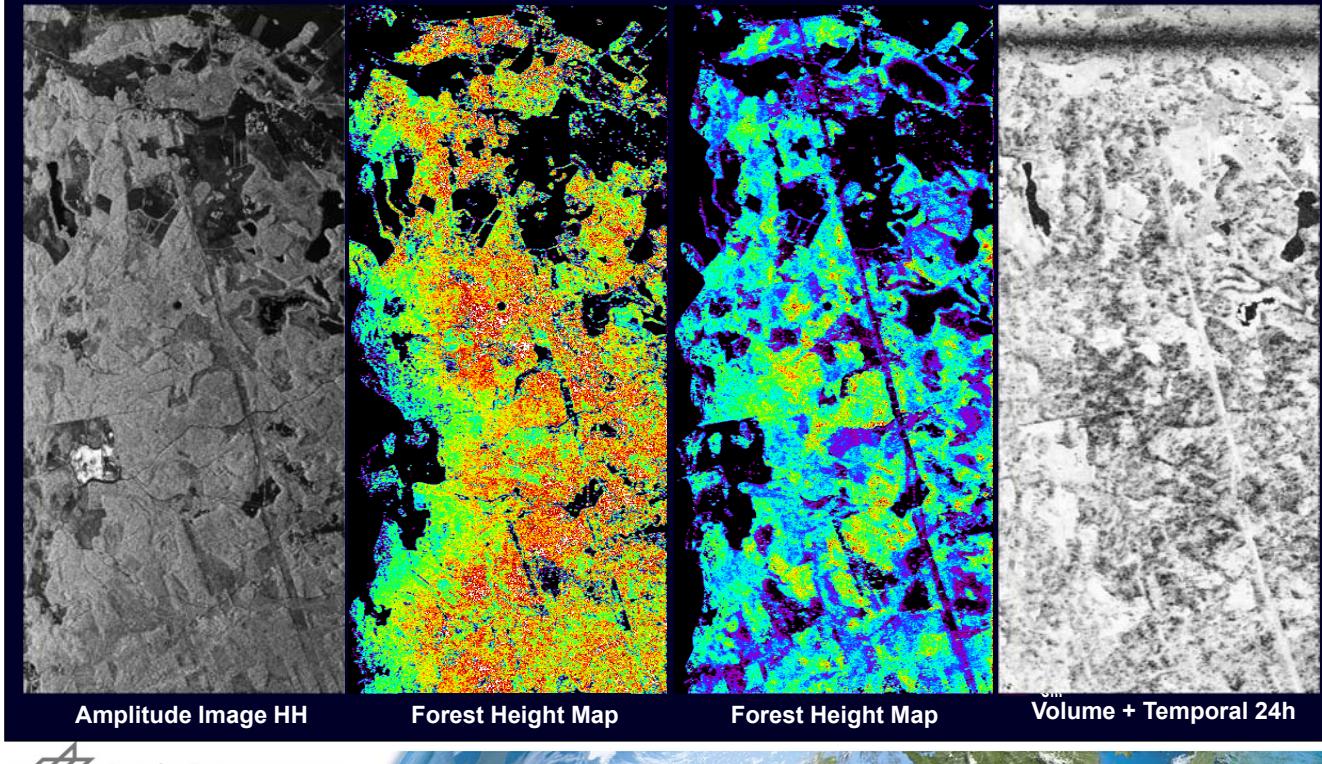
Volume + Temporal 24h



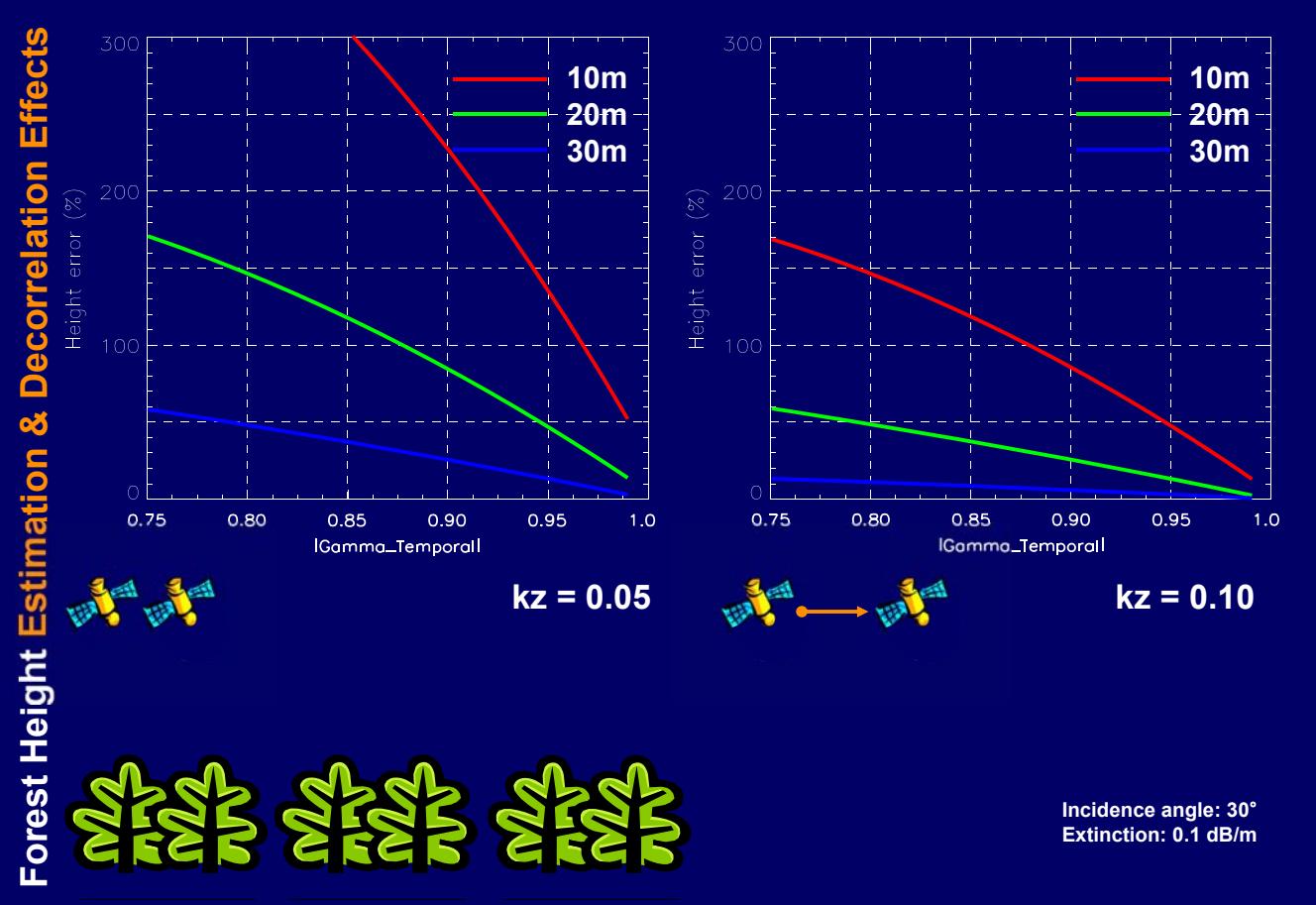
Deutsches Zentrum
für Luft- und Raumfahrt e.V.
in der Helmholtz-Gemeinschaft



Interferometric Coherence: Volume vs Temporal Decorrelation



Deutsches Zentrum
für Luft- und Raumfahrt e.V.
in der Helmholtz-Gemeinschaft



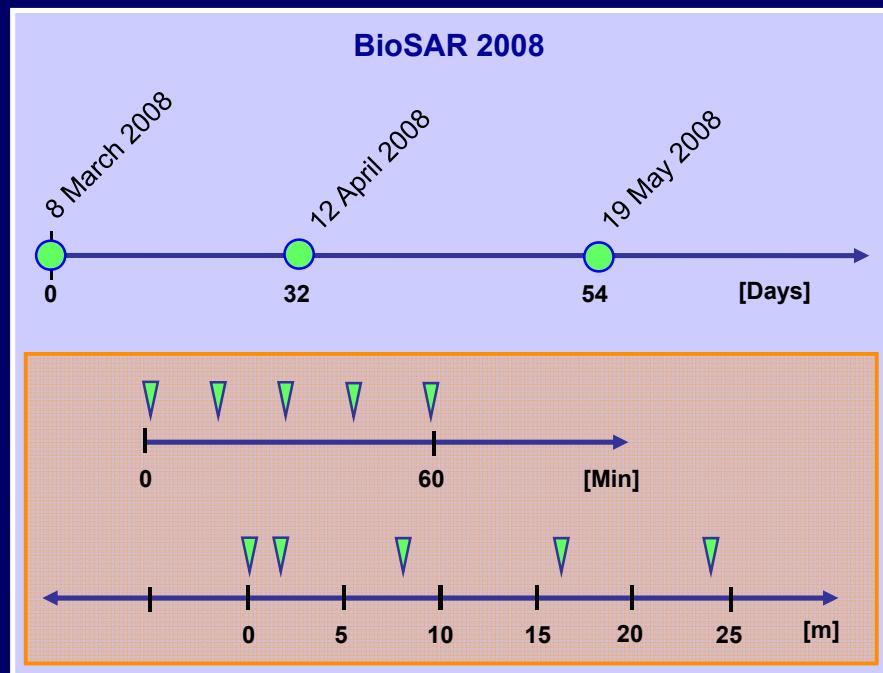
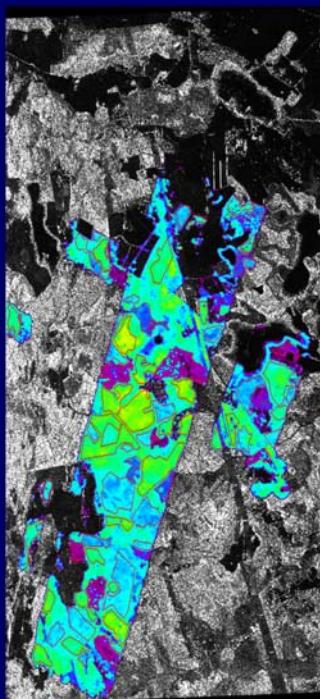
BIOSAR: Remnningstorp Test Site

- Forest Heights: up to 25 -30m
- Predominantly Spruce but also Pine and Mixed stands.
- Homogenous and Managed.
- Biomass Level: up to 300t/ha
- Flat Topography



eesa

Remnningstorp Test Site: The BIOSAR-I Campaign



Amplitude Image HH

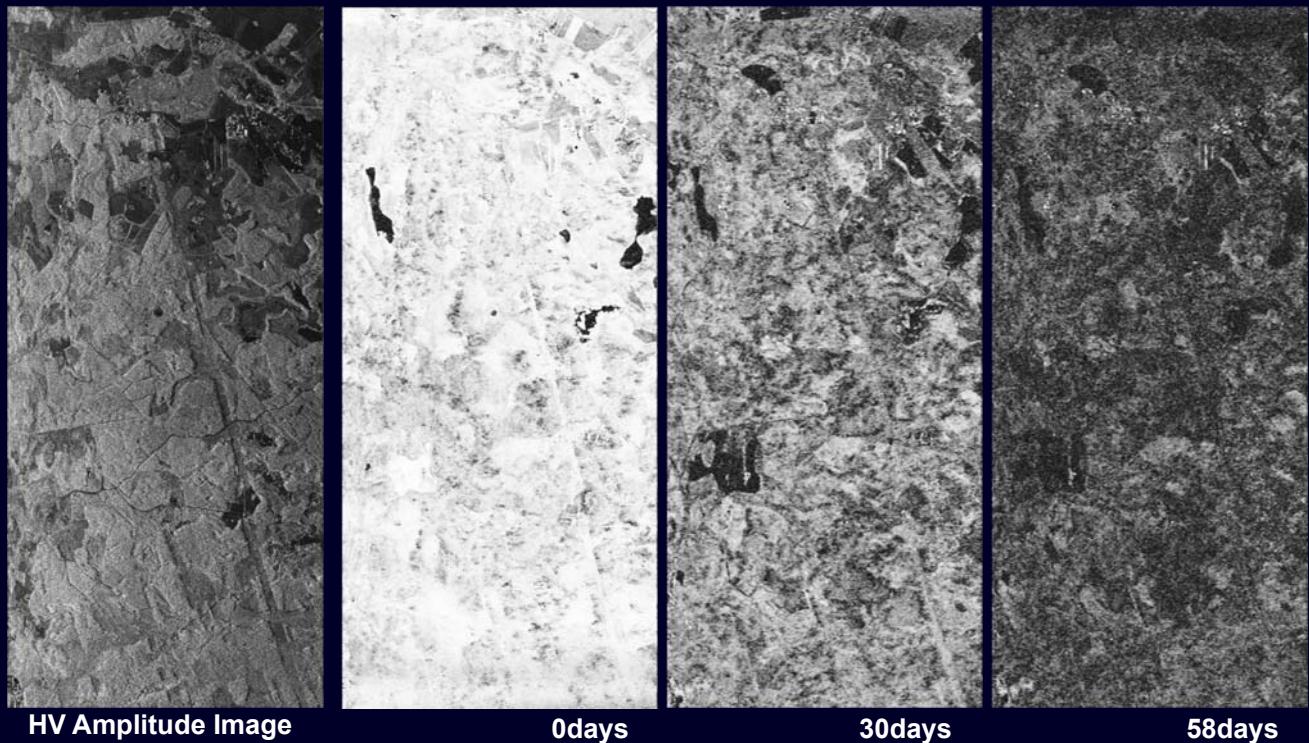


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für Luft- und Raumfahrt e.V.
in der Helmholtz-Gemeinschaft

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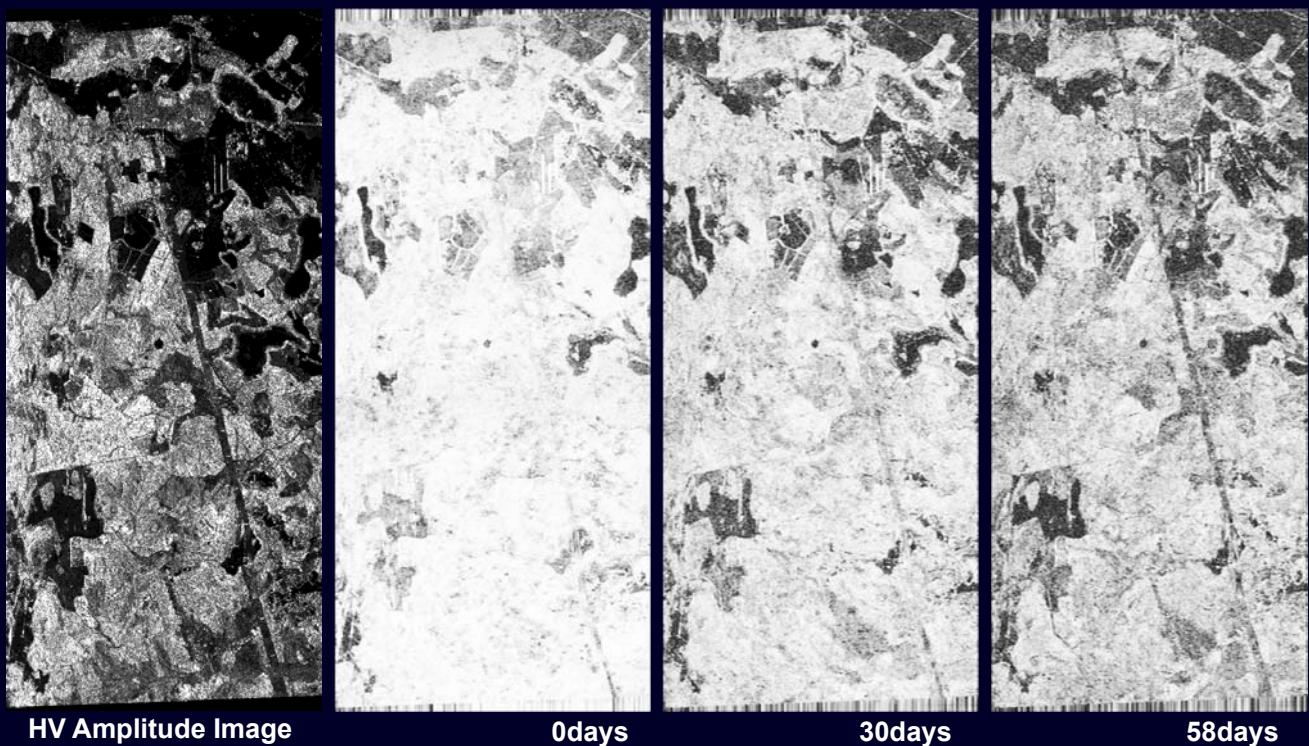
Remningstorp Test Site: Temporal Decorrelation: L-band



Deutsches Zentrum
für Luft- und Raumfahrt e.V.
in der Helmholtz-Gemeinschaft



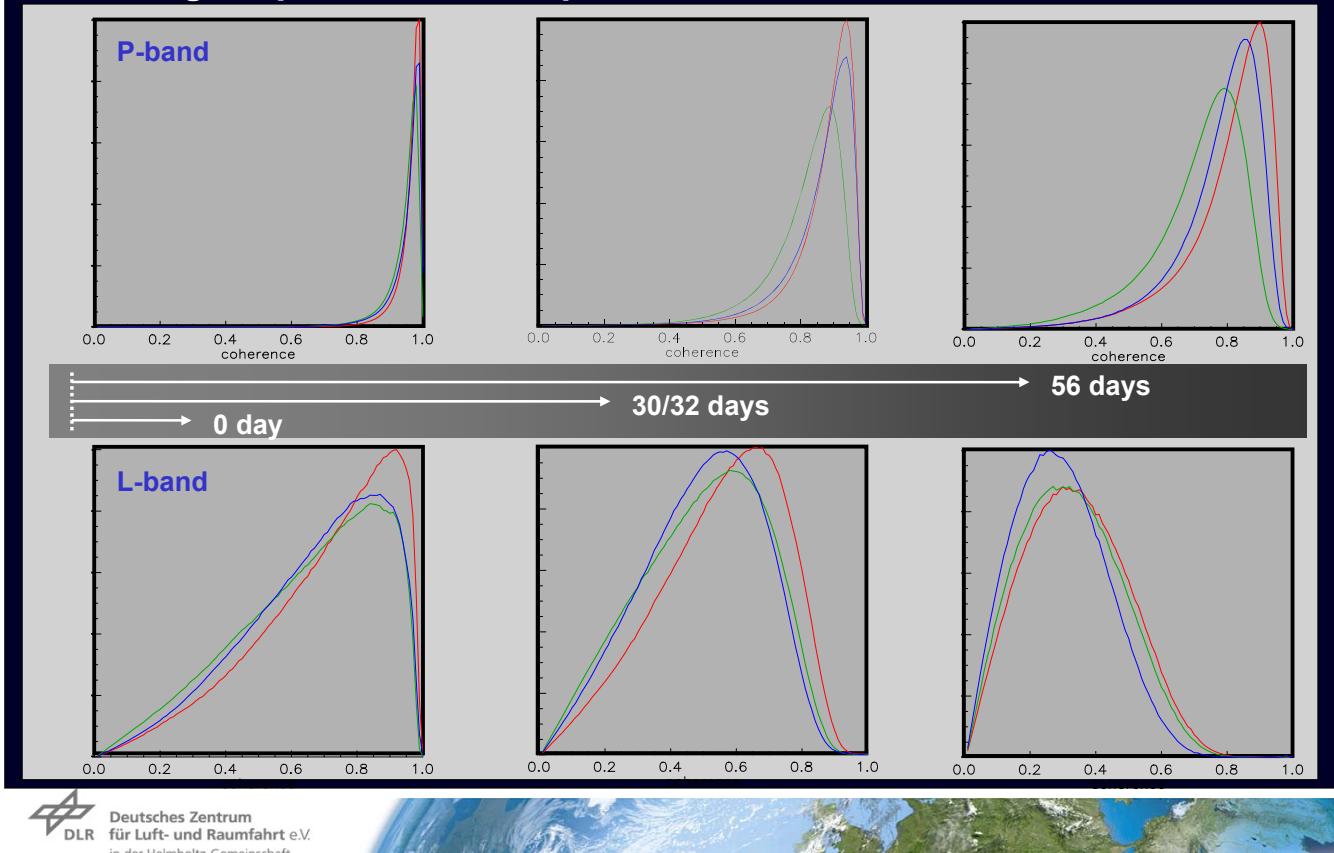
Remningstorp Test Site: Temporal Decorrelation: P-Band



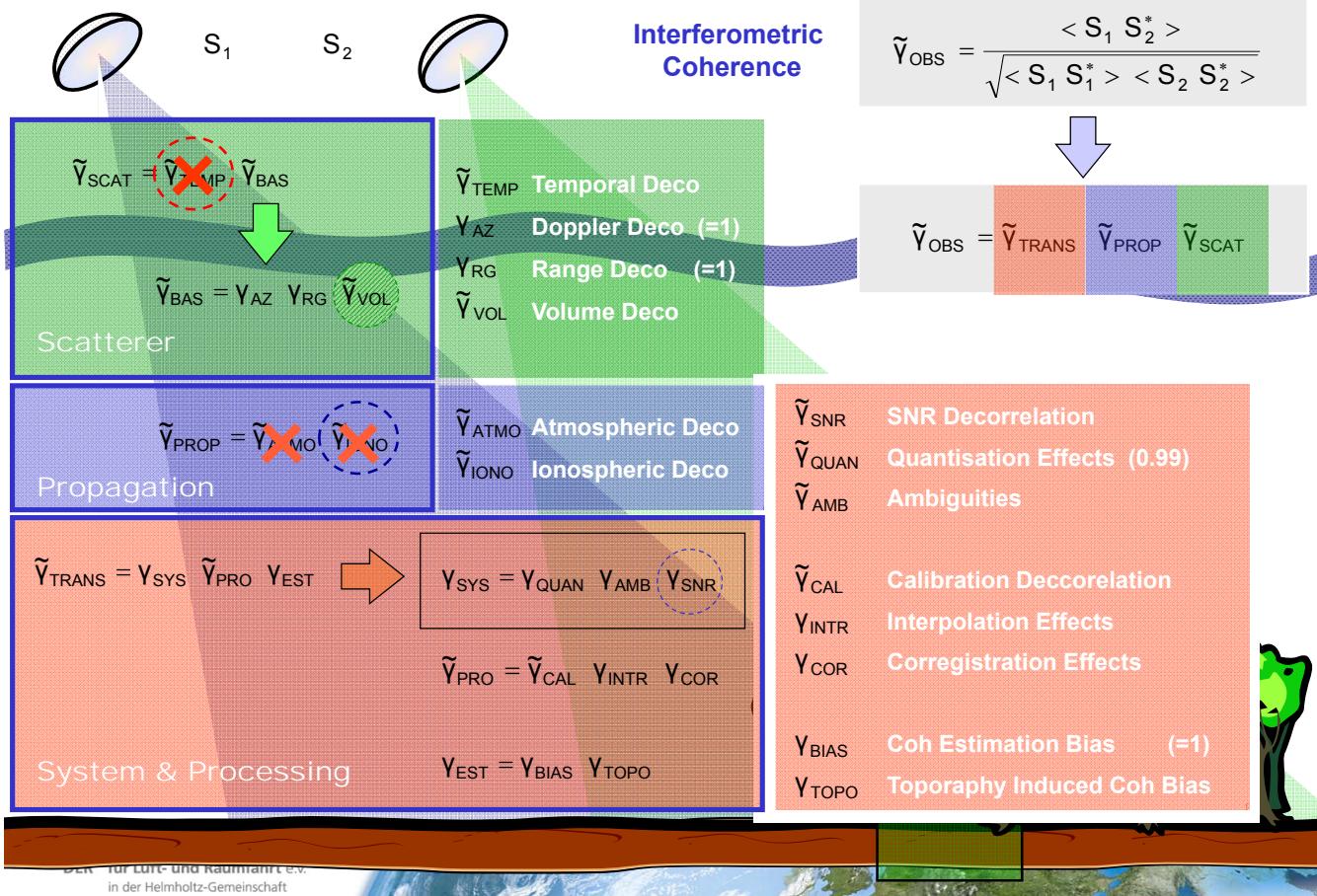
Deutsches Zentrum
für Luft- und Raumfahrt e.V.
in der Helmholtz-Gemeinschaft



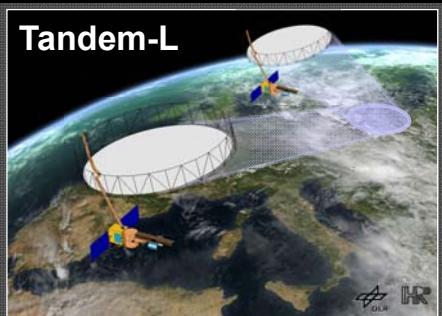
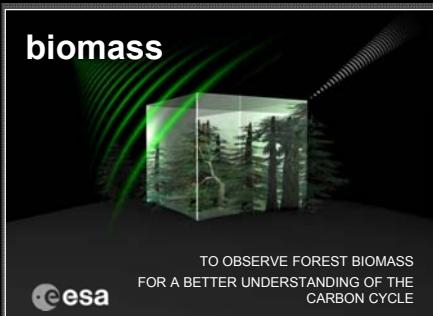
Remningstorp Test Site: Temporal Decorrelation: P-Band



Deutsches Zentrum
für Luft- und Raumfahrt e.V.
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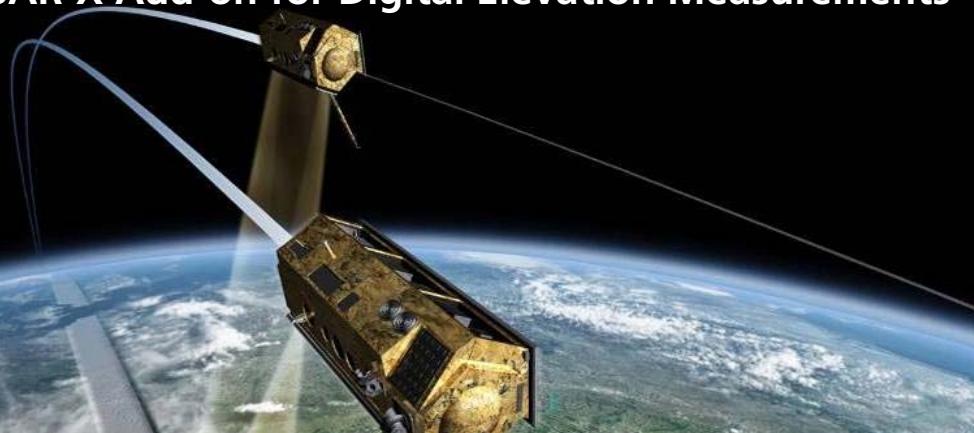
Pol-InSAR In Orbit



Deutsches Zentrum
für Luft- und Raumfahrt e.V.
in der Helmholtz-Gemeinschaft

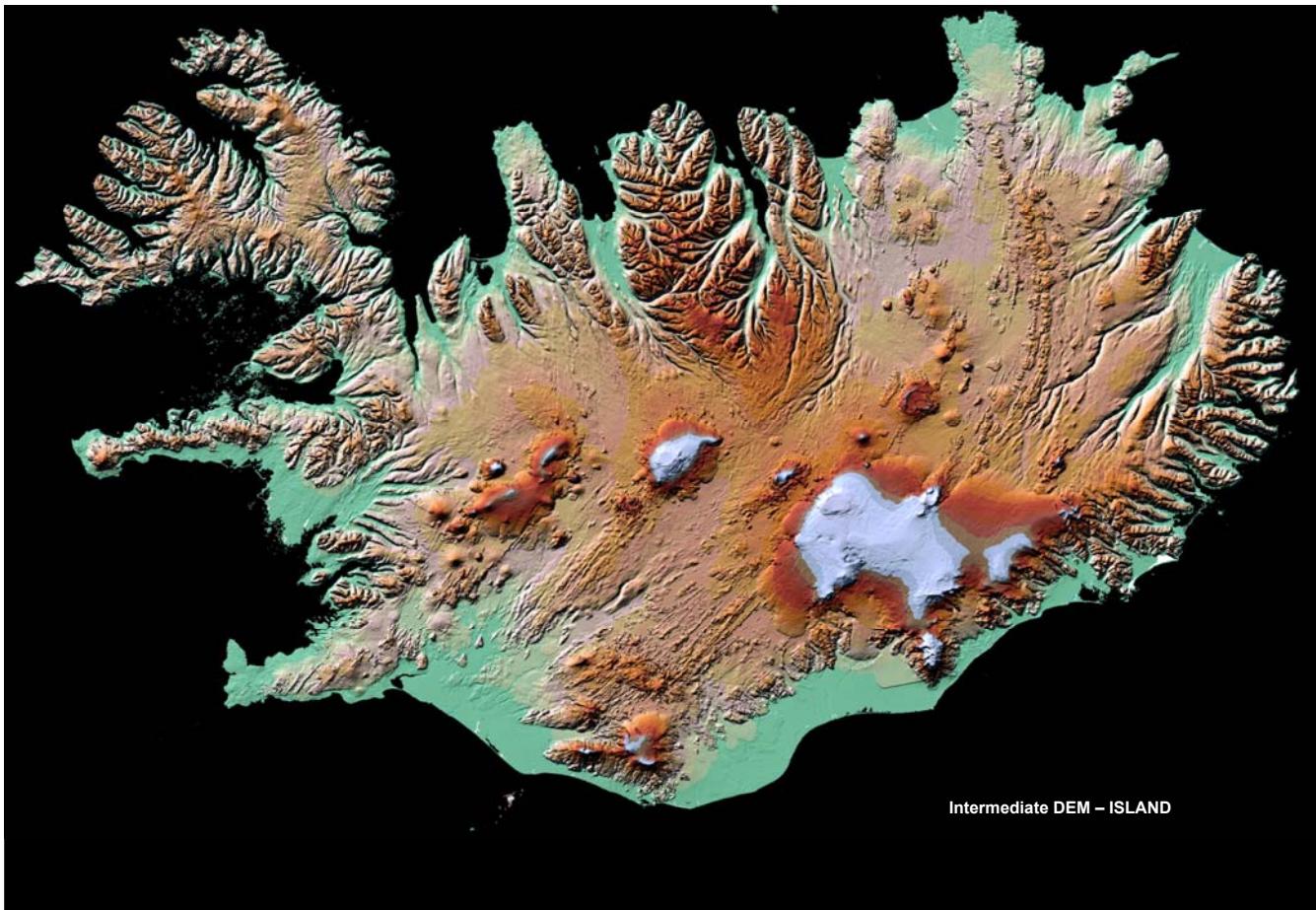


TanDEM-X: TerraSAR-X Add-on for Digital Elevation Measurements

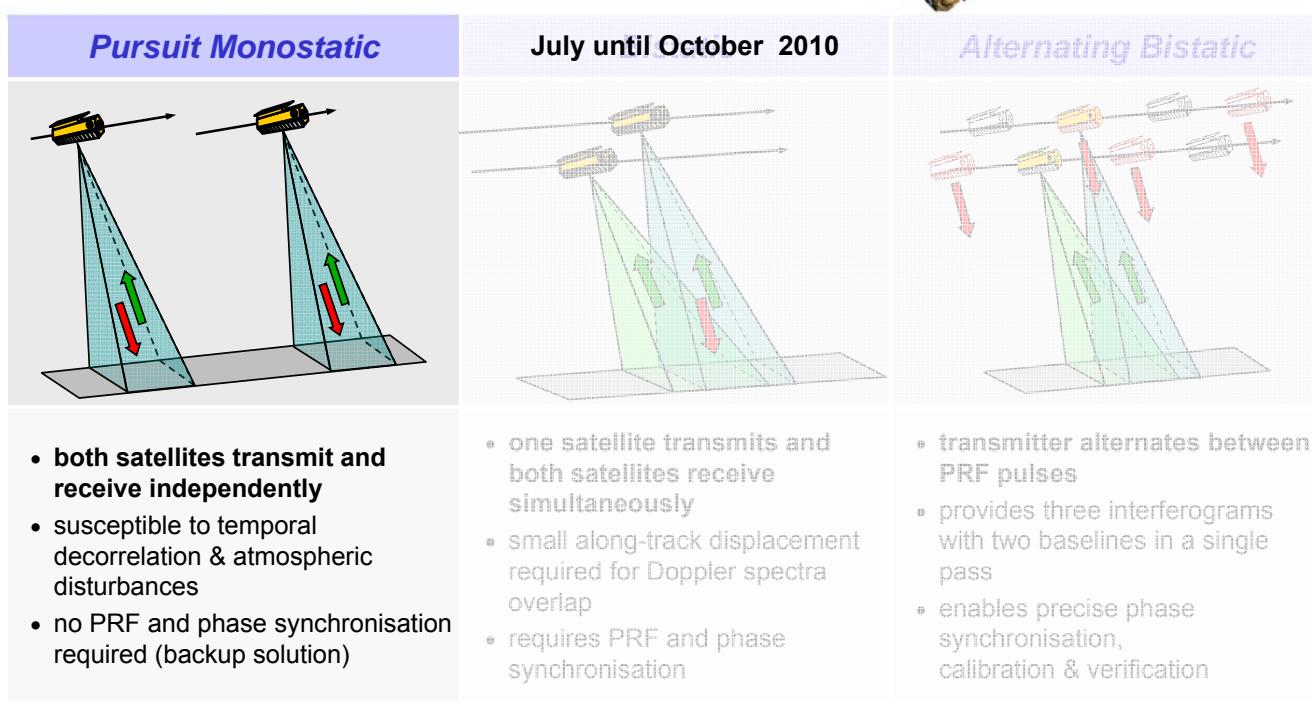


DEMs	Spatial Resolution	Absolute Vertical Accuracy (90%)	Relative Vertical Accuracy (point-to-point in 1° cell, 90%)
DTED-1	90m x 90m	< 30m	< 20m
DTED-2	30m x 30m	< 18m	< 12m
TanDEM-X DEM	12m x 12m	< 10m	< 2m
HDEM	6m x 6m	< 5m	< 0.8m





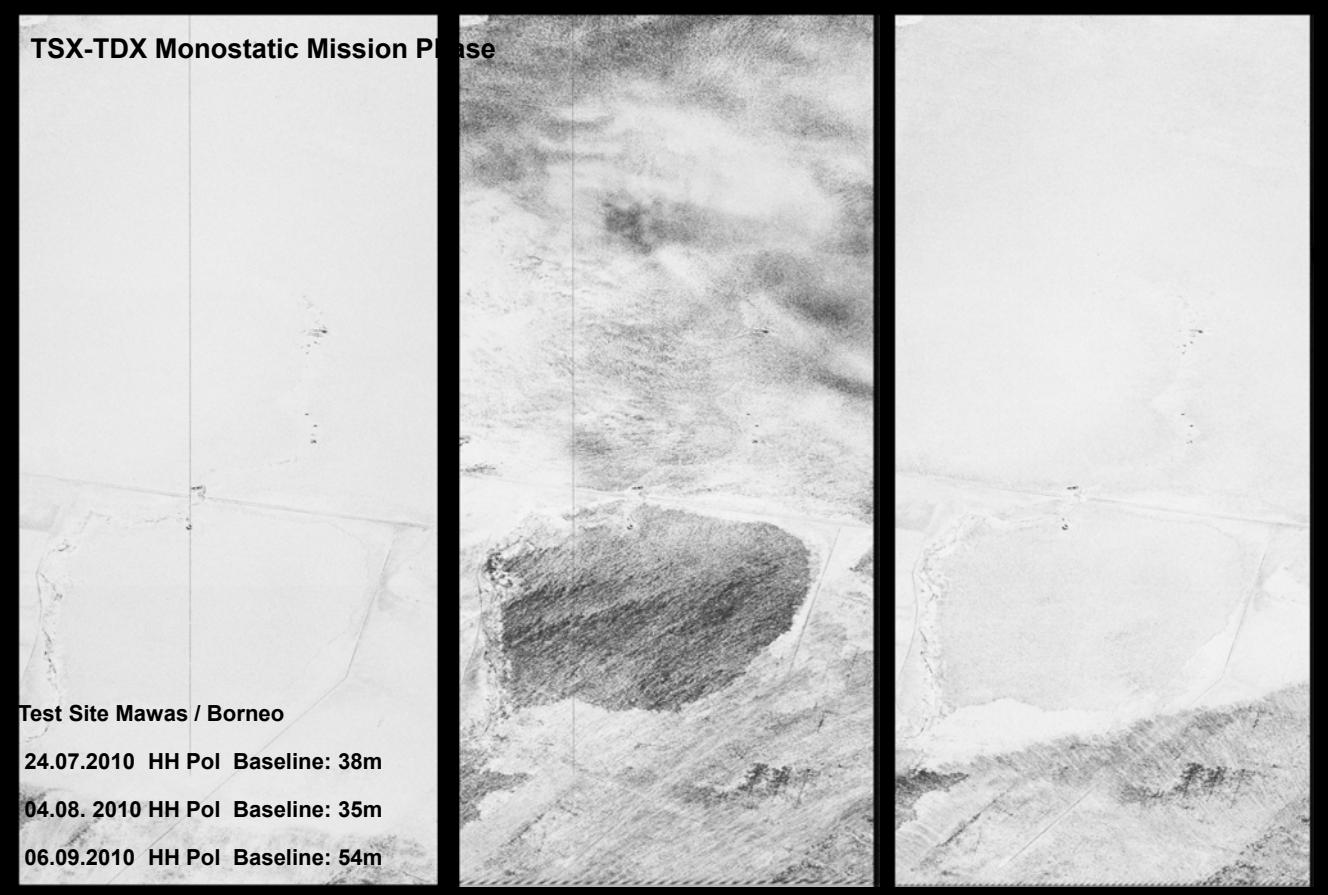
TanDEM-X Data Acquisition Modes



TSX-TDX Monostatic Mission Phase



TSX-TDX Monostatic Mission Phase



TSX-TDX Monostatic Mission Phase

Test Site Mawas / Borneo

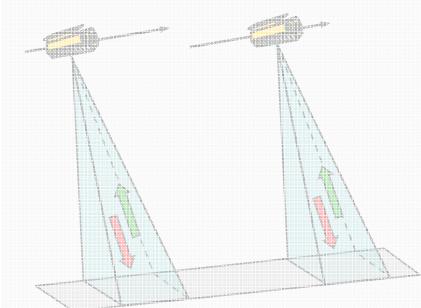
24.07.2010 HH Pol Baseline: 38m
04.08. 2010 HH Pol Baseline: 35m
06.09.2010 HH Pol Baseline: 54m



TanDEM-X Data Acquisition Modes

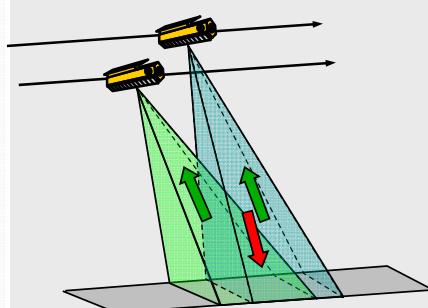


Pursuit Monostatic



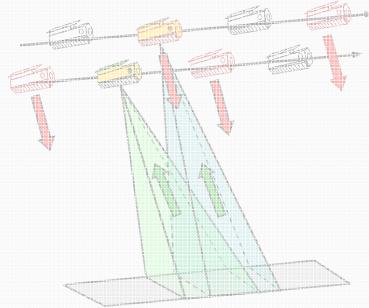
- both satellites transmit and receive independently
- susceptible to temporal decorrelation & atmospheric disturbances
- no PRF and phase synchronisation required (backup solution)

Bistatic



- one satellite transmits and both satellites receive simultaneously
- small along-track displacement required for Doppler spectra overlap
- requires PRF and phase synchronisation

Alternating Bistatic



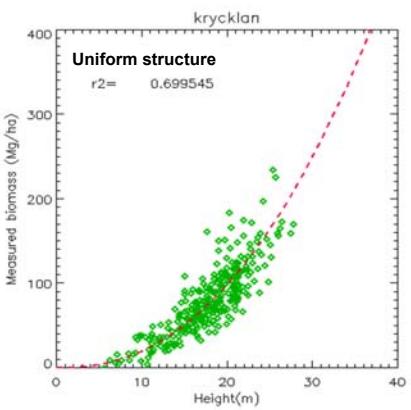
- transmitter alternates between PRF pulses
- provides three interferograms with two baselines in a single pass
- enables precise phase synchronisation, calibration & verification

Standard DEM Mode

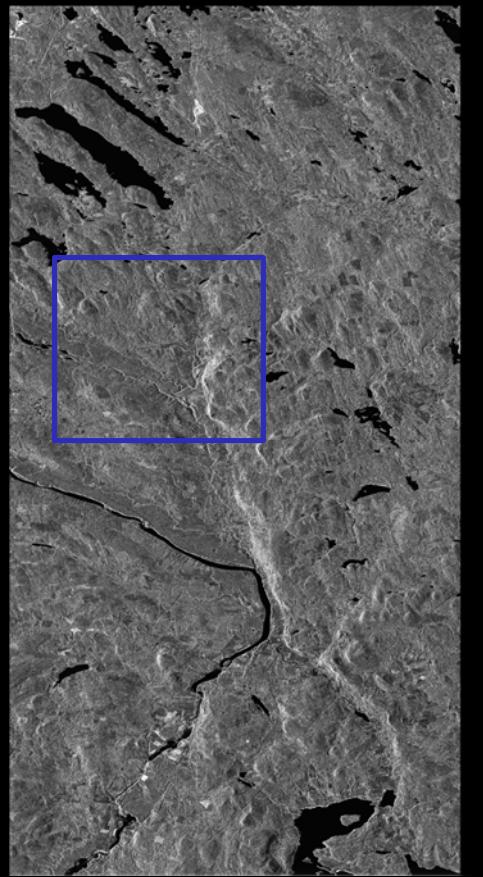
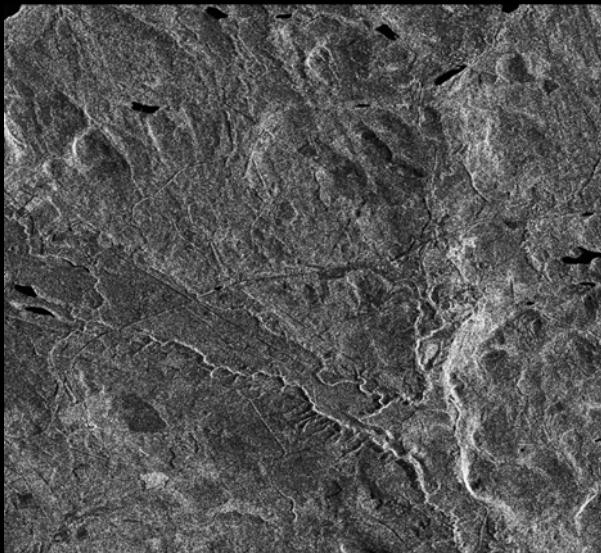


Deutsches Zentrum
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in der Helmholtz-Gemeinschaft

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Test Site: Krycklan, Sweden



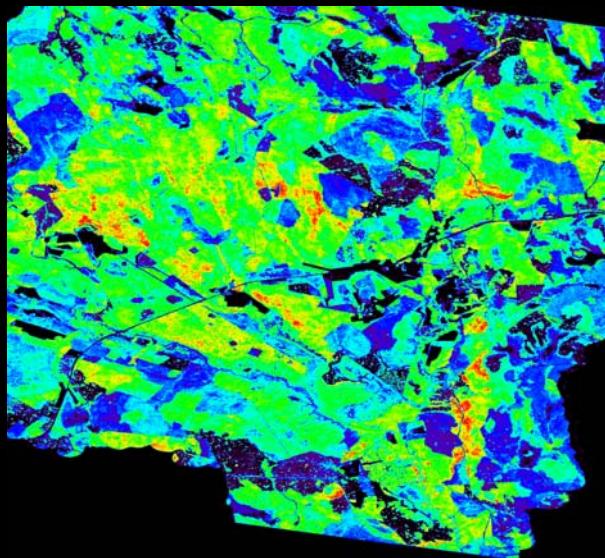
Test Site: Krycklan, Sweden



Interferometric Coherence HH

0

1

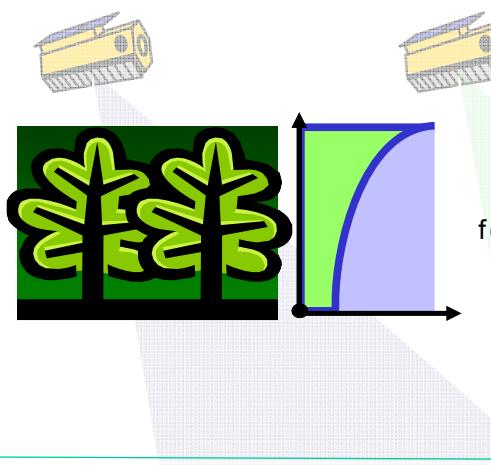
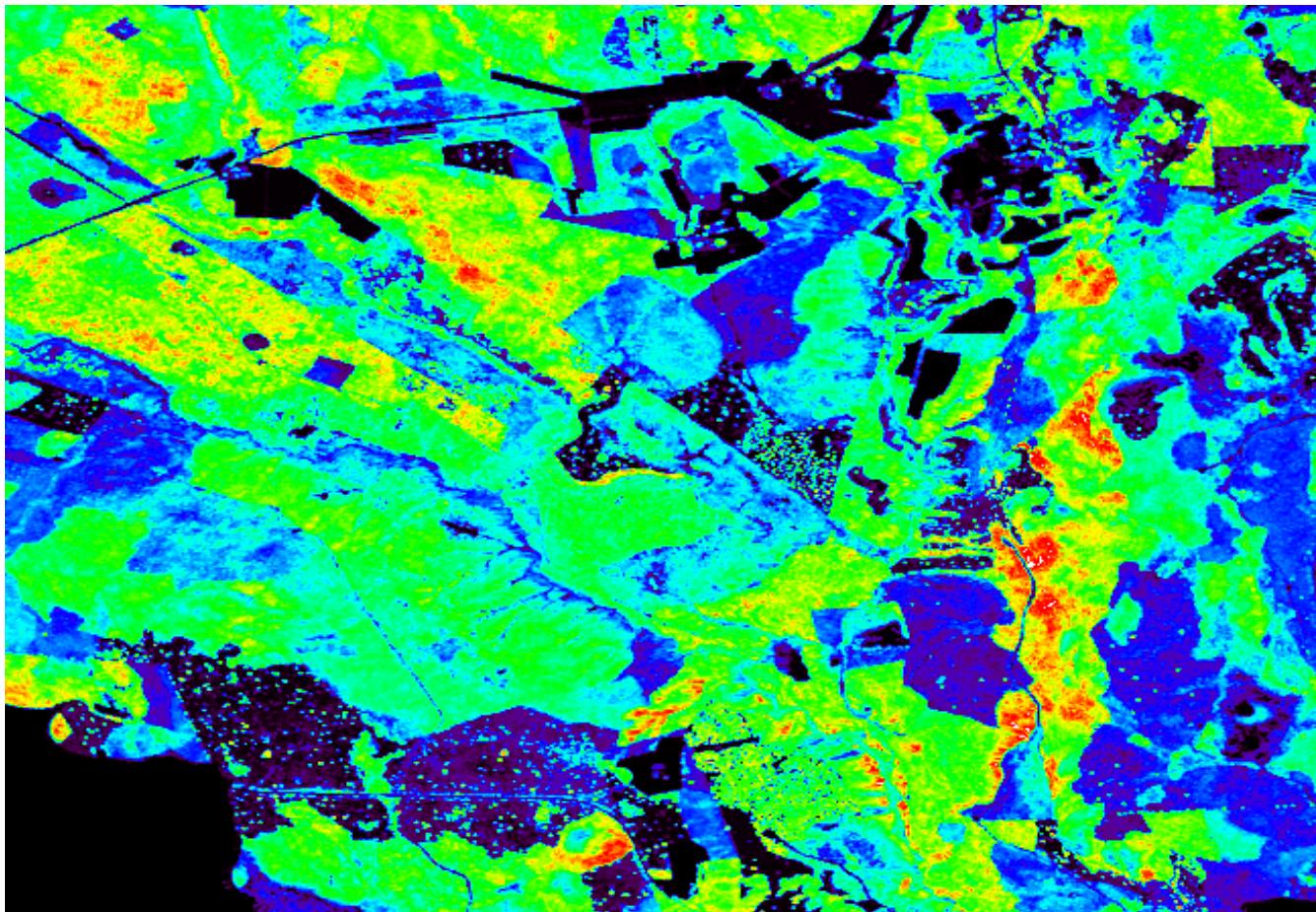


Lidar H100

0 [m]

30





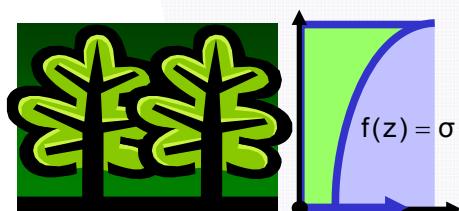
Single-Pol: 1 Layer Scattering Model

$$f(z) = \sigma_{V0} \exp\left(\frac{2 \sigma z}{\cos \theta_0}\right)$$

$$\tilde{\gamma}(\bar{w}) = \exp(i\phi_0) \tilde{\gamma}_v$$

DEM ► Topography ϕ_0

Volume Height h_v Extinction σ



Dual-Pol: 2 Layer Scattering Model

$$f(z) = \sigma_{V0} \exp\left(\frac{2 \sigma z}{\cos \theta_0}\right) + m'_G \delta(z - z_0)$$

$$\tilde{\gamma}(\bar{w}) = \exp(i\phi_0) \frac{\tilde{\gamma}_v + m(\bar{w})}{1 + m(\bar{w})}$$

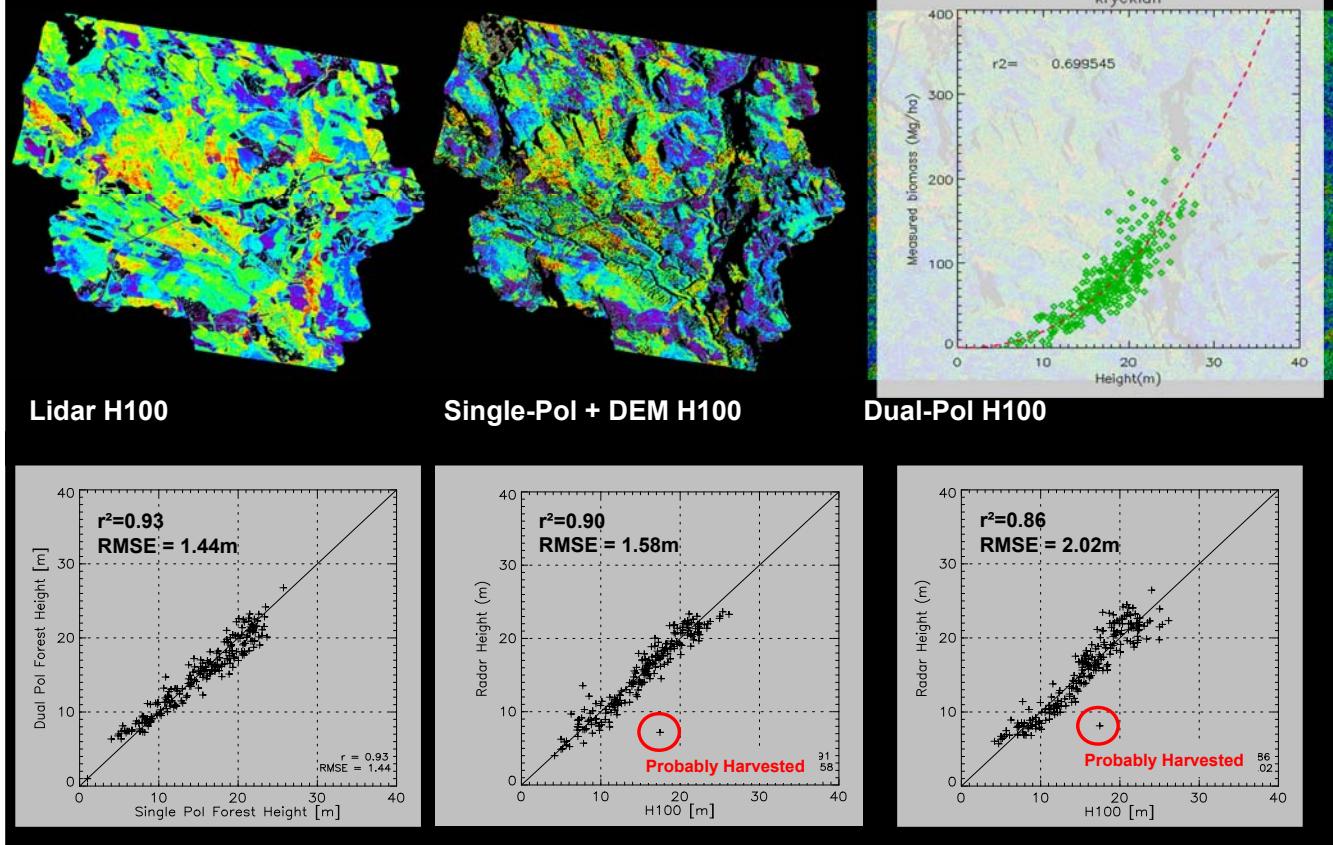
Volume Height h_v Extinction σ

Topography ϕ_0 G/V Ratio $m(\bar{w})$

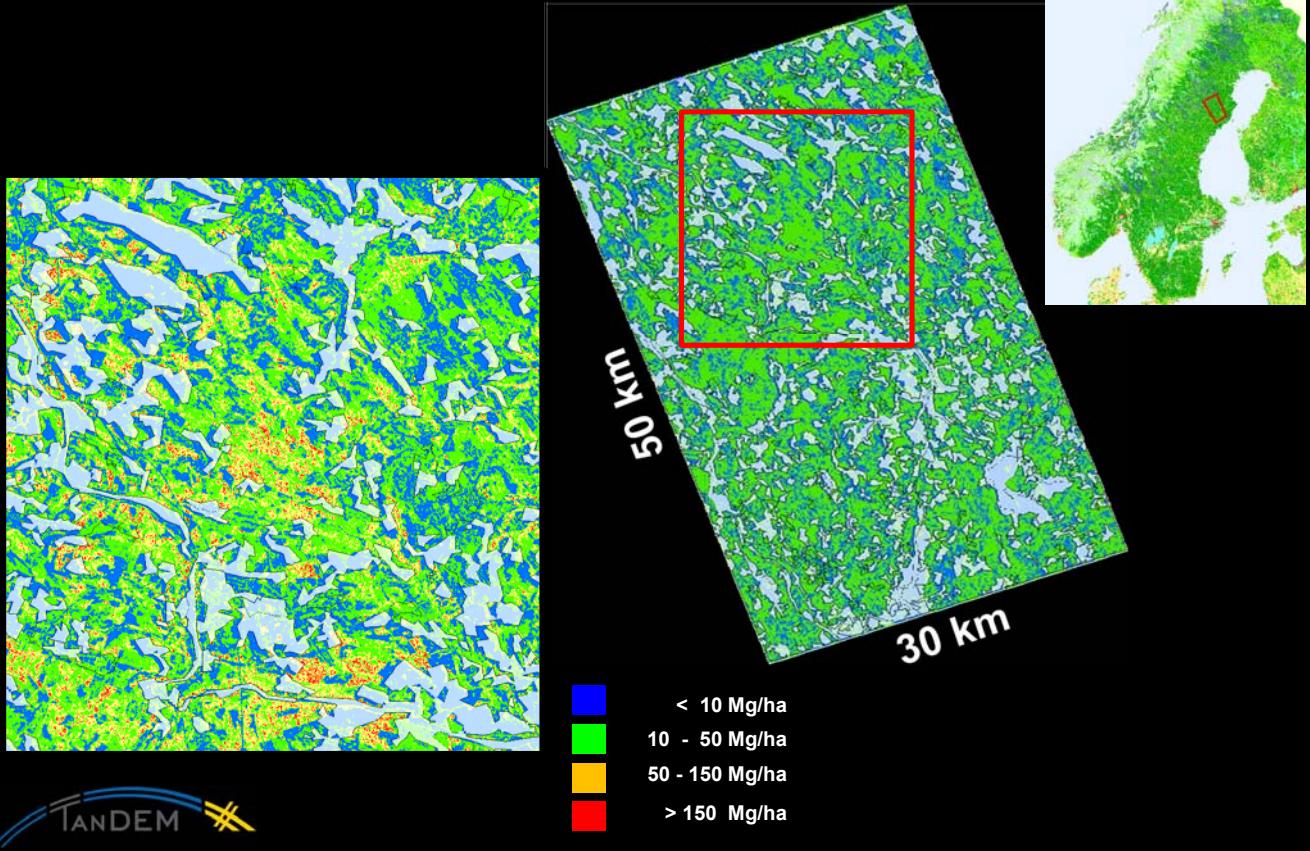
$$\tilde{\gamma}_v = \frac{I}{I_0} \begin{cases} I = \int_0^{h_v} \exp(i\kappa_z z') \exp\left(\frac{2 \sigma z'}{\cos \theta_0}\right) dz' \\ I_0 = \int_0^{h_v} \exp\left(\frac{2 \sigma z'}{\cos \theta_0}\right) dz' \end{cases}$$

G/V Ratio: $m(\bar{w}) = \frac{m_G(\bar{w})}{m_V(\bar{w})l_0}$ **Vertical Wavenumber:** $\kappa_z = \frac{\kappa \Delta \theta}{\sin(\theta_0)}$

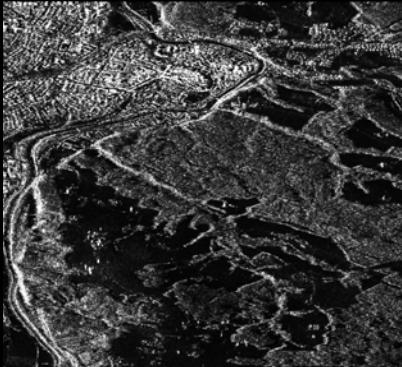
Test Site: Krycklan, Sweden



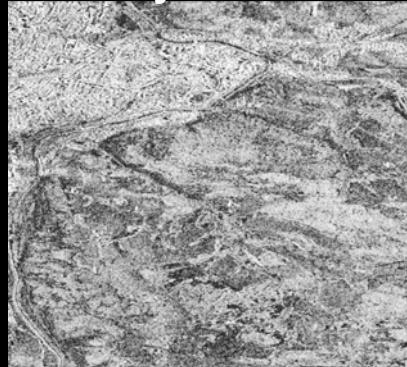
CORINE Land Cover Classes - Krycklan



Test Site: Traunstein, Germany



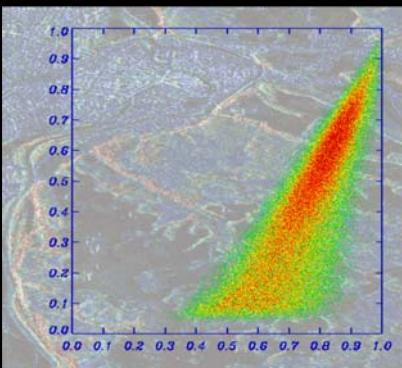
HH Amplitude



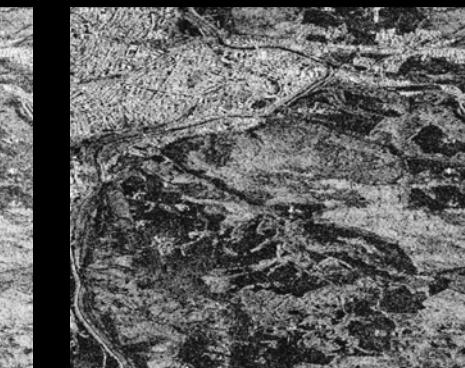
Interferometric Coherence HH



Interferometric Coherence Max



Interferometric Coherence VV

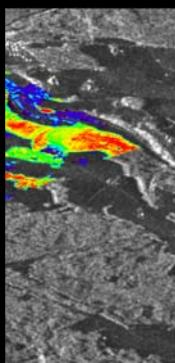
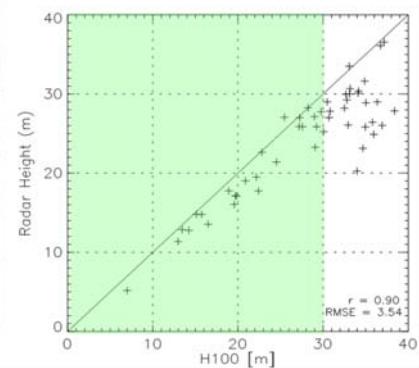


Interferometric Coherence Min

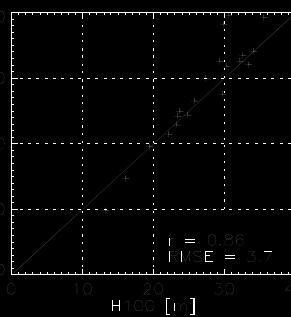


Test Site: Traunstein, Germany

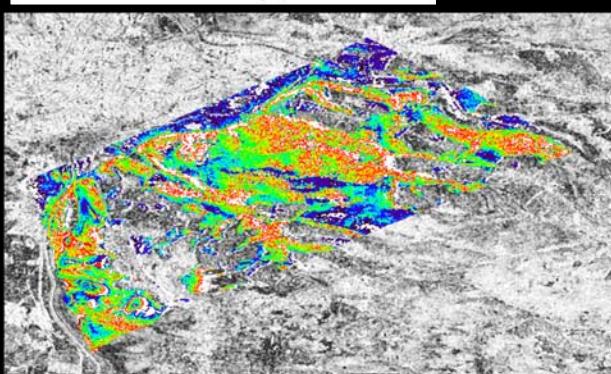
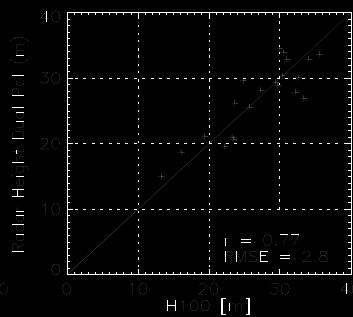
ESAR Inversion Results



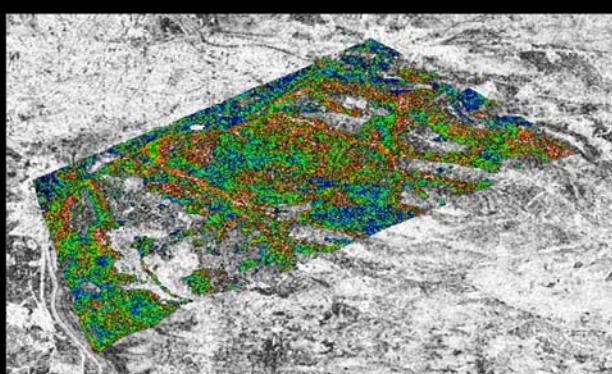
Single-Pol (HH) + DEM



Dual-Pol

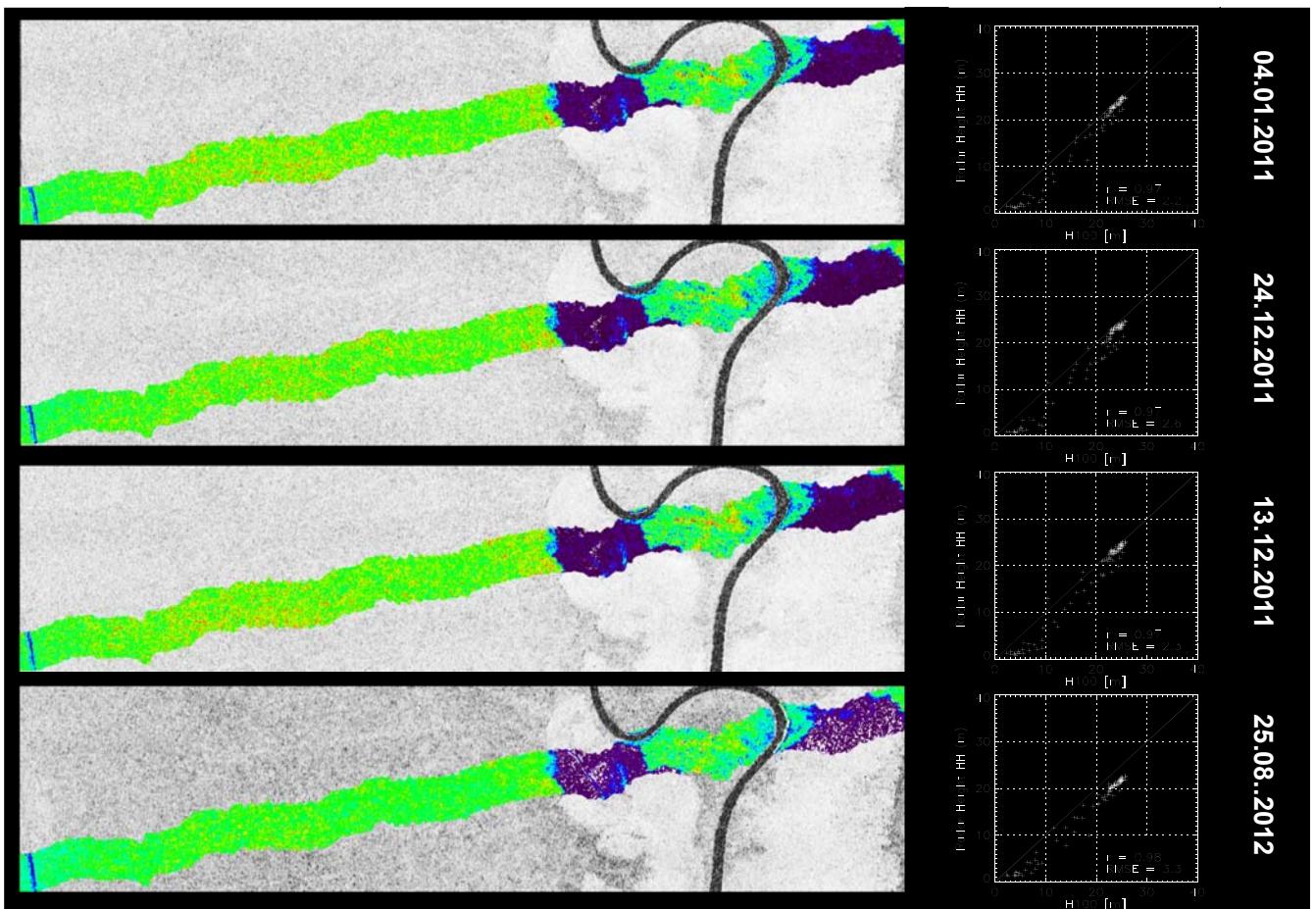
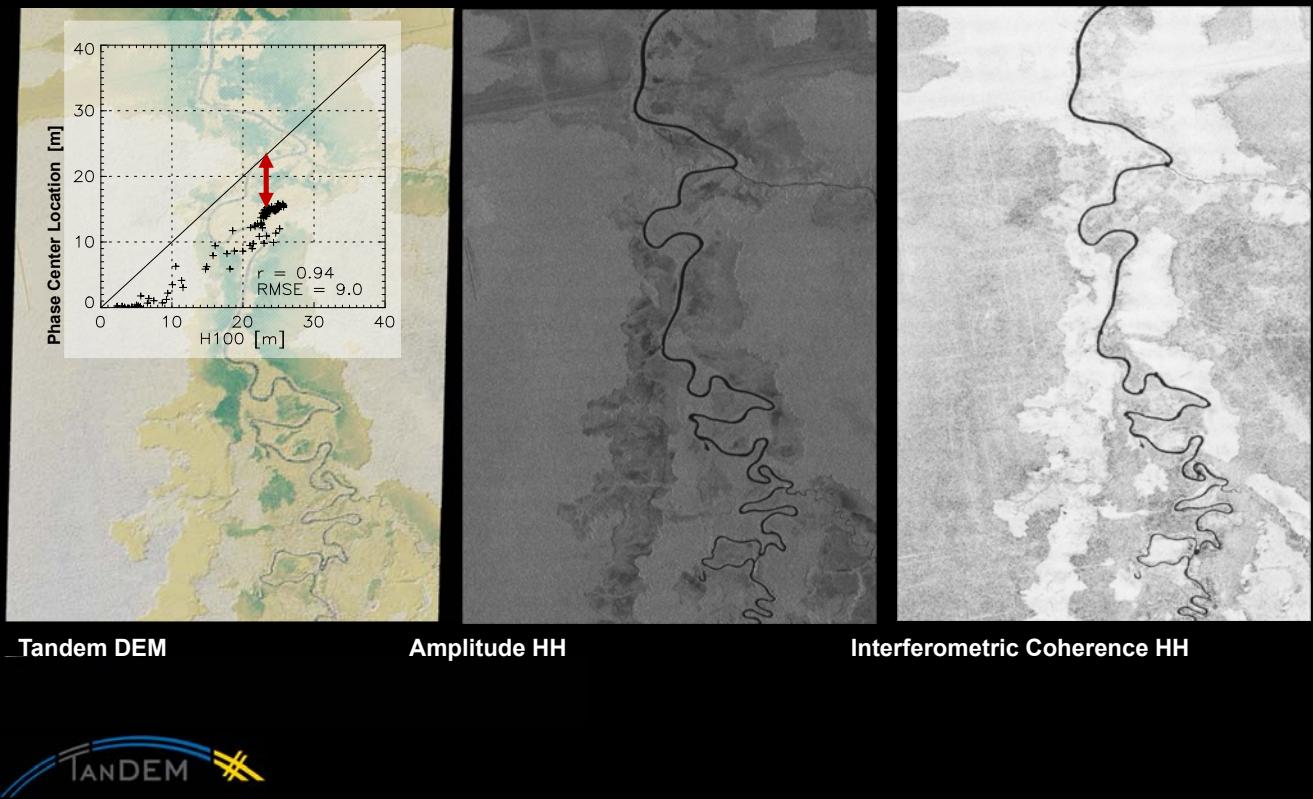


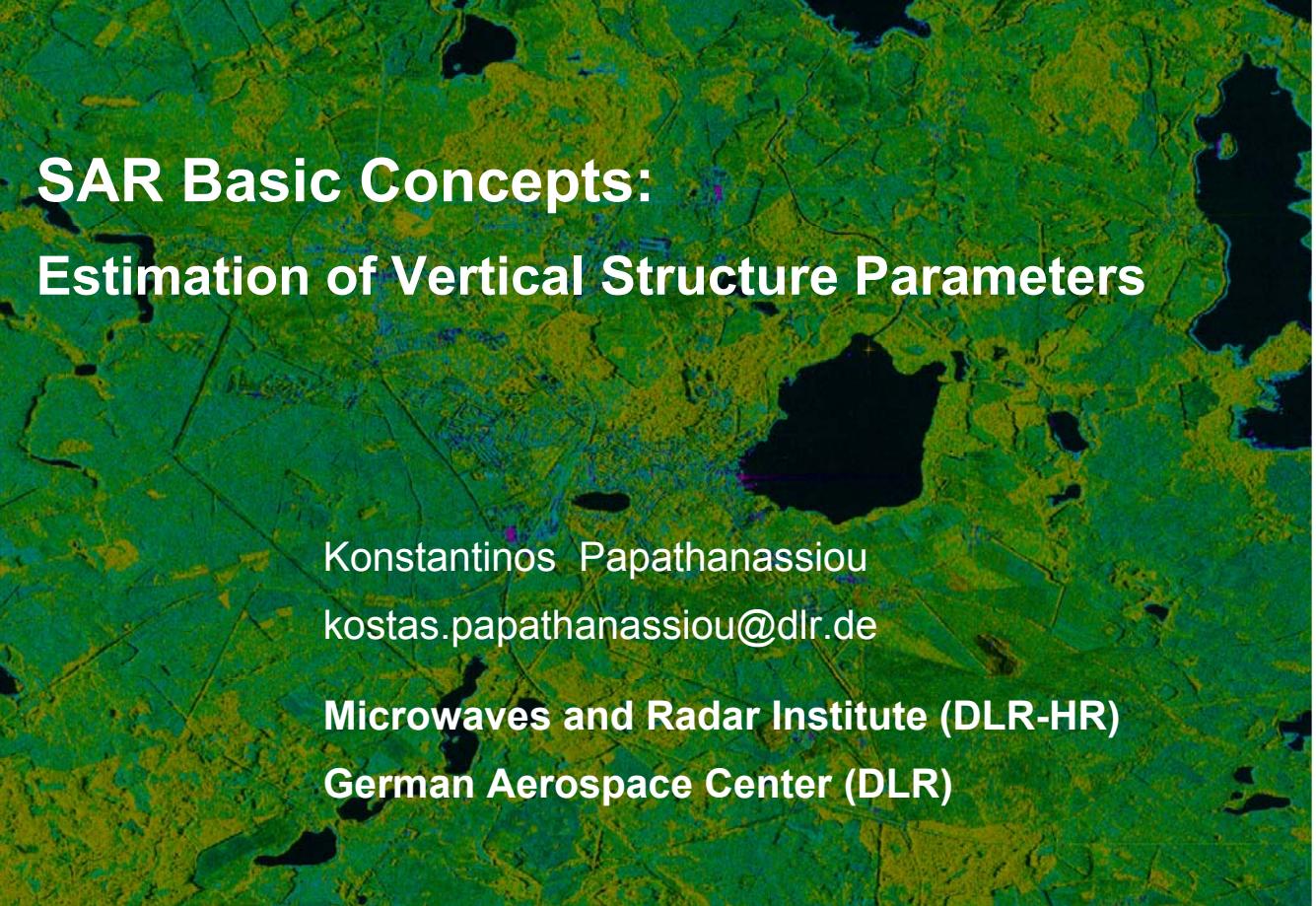
Single-Pol (HH) + DEM H100



Dual-Pol H100

Test Site: Mawas, Indonesia





SAR Basic Concepts: Estimation of Vertical Structure Parameters

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