

Tackling temporal decorrelation with the RMoG model

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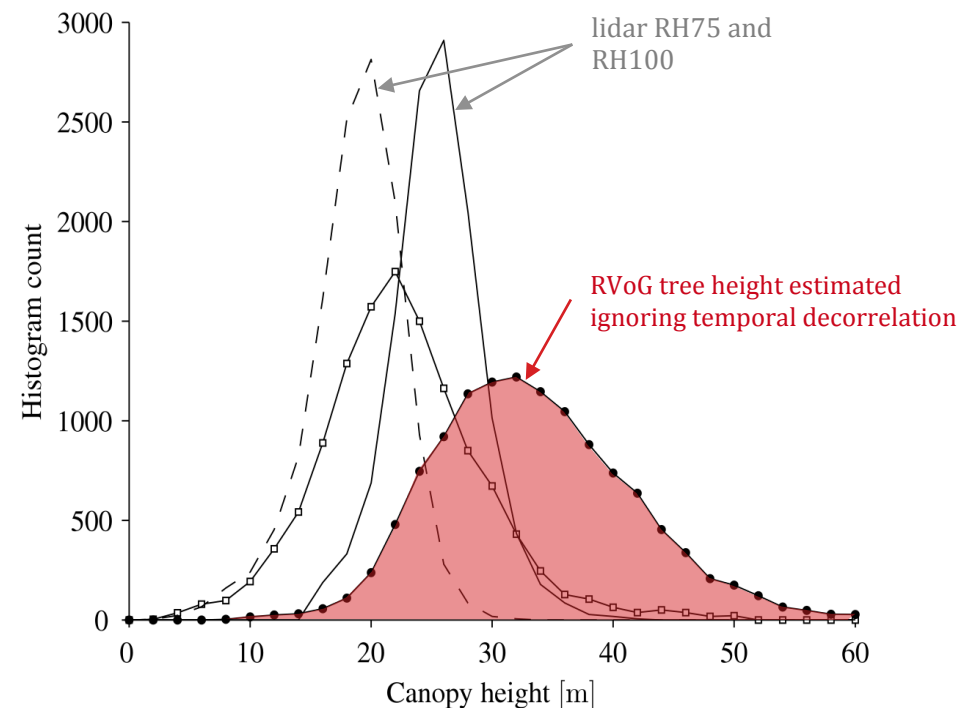
Outline

- Introduction and motivation
- **Part I:** The RMoG model
 - Modeling assumptions
 - Consequences of the RMoG model
- **Part II:** Inversion of the RMoG model
 - Inversion using single-baseline Pol-InSAR data
 - Numerical simulations
 - UAVSAR experiments

Motivation and objectives

- Current and forthcoming **low-frequency SAR missions** (ALOS-1/2, BIOMASS, DESDynI) collect repeat-pass data
- The **use of repeat-pass Pol-InSAR** data is predicated on solving/mitigating the problem of temporal decorrelation
- **Objective is** to provide a model-based algorithm that “compensates for” temporal decorrelation while forest parameter are estimated

Canopy height estimated from 2-day repeat-pass JPL/UAVSAR data (Harvard Forest, MA)



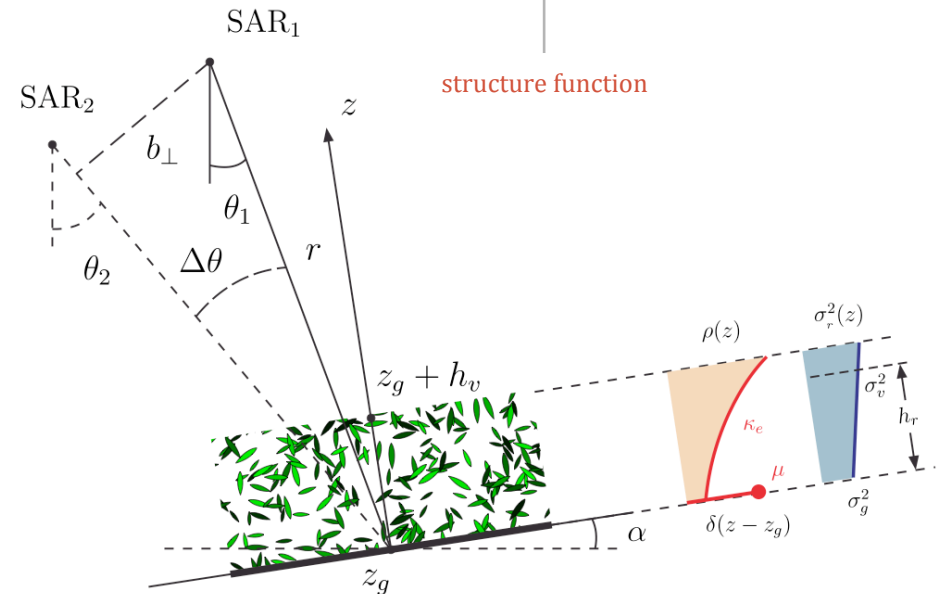
The RMoG model

- **Random-motion-over-ground (RMoG)** model:
RVoG model + refined Zebker's model
- Physical model of temporal-volumetric coherence proposed in late 2009 and improved throughout 2010-2012
- **Exponential structure function** for volumetric decorrelation
- First-order expansion of **arbitrary temporal function** for temporal decorrelation (time-dependence dropped)

$$\gamma = \frac{\int \rho(z) e^{jk_z z} \exp \left[-\frac{1}{2} \left(\frac{4\pi}{\lambda} \right)^2 \sigma_r^2(z) \right] dz}{\int \rho(z) dz}$$

temporal function

structure function



Key properties of the RMoG model

- 4 structural + 2 temporal = 6 model parameters
- Temporal and volumetric decorrelations are mixed and **not separable**

RMoG coherence

$$\gamma = e^{j\varphi_g} \frac{\mu \gamma_{tg} + \gamma_{vt} e^{-j\varphi_g}}{\mu + 1} \quad \gamma \neq \gamma_t \gamma_v$$

ground-layer coherence

$$\gamma_{tg} = \exp \left[-\frac{1}{2} \left(\frac{4\pi}{\lambda} \right)^2 \sigma_g^2 \right]$$

canopy-layer coherence

$$\gamma_{vt} = e^{j\varphi_g} \gamma_{tg} \frac{p_1 \left[e^{(p_2+p_3)h_v} - 1 \right]}{(p_2 + p_3) (e^{p_1 h_v} - 1)}$$

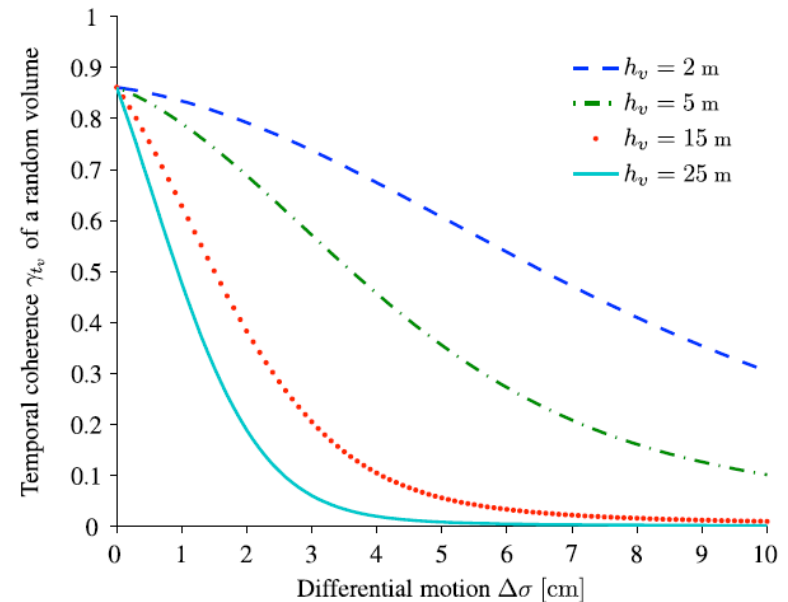
$$p_1 = \frac{2\kappa_e}{\cos(\theta - \alpha)},$$

$$p_2 = p_1 + jk_z,$$

$$p_3 = -\frac{\Delta\sigma^2}{2h_r} \left(\frac{4\pi}{\lambda} \right)^2$$

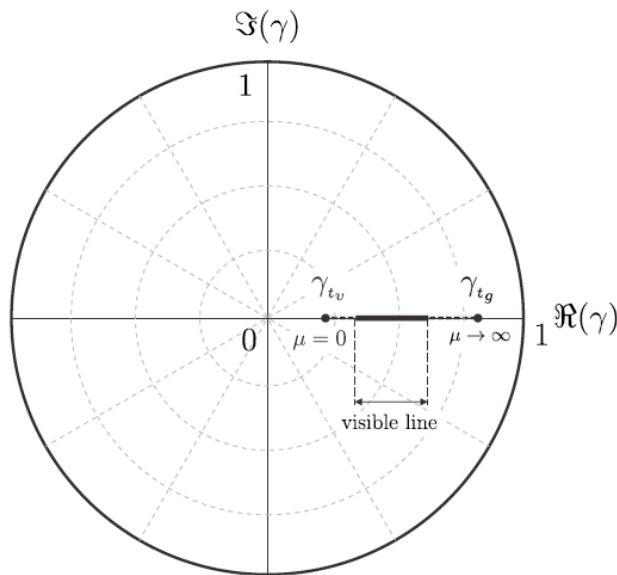
property n. 1

RMoG temporal decorrelation depends on vegetation structure (e.g. canopy height)



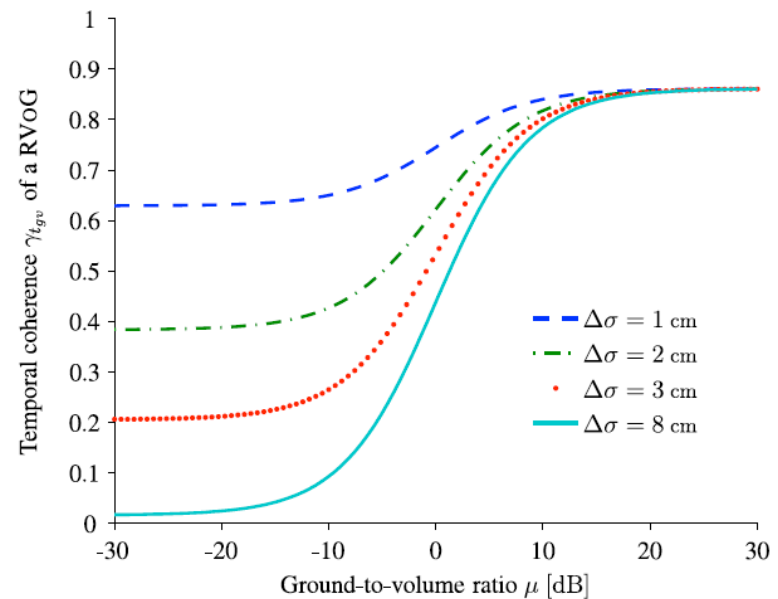
Key properties of the RMoG model

Coherence locus of RMoG temporal decorrelation



property n. 2

RMoG temporal decorrelation depends on wave polarization through the ground-to-volume ratio



M. Lavallo, M. Simard and S. Hensley, "A temporal decorrelation model for polarimetric radar interferometers", IEEE TGRS 2012.

Part II

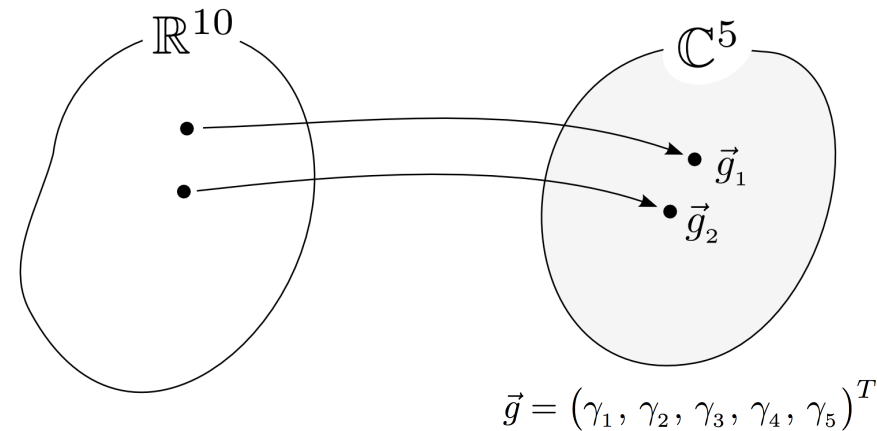
Inversion of the RMoG model

From RMoG model to RMoG forward problem

- **RMoG forward problem** formulated as mapping of ten-dimensional real vector into five-dimensional complex vector
- Each coherence observation has a **different ground-to-volume ratio**
- **Domain** of RMoG forward problem is a subset of the 10-dimensional real space
- **Codomain** of RMoG forward problem is a subset of the 5-dimensional complex space

$$f : \begin{pmatrix} \varphi_g \\ h_v \\ \kappa_e \\ \sigma_g \\ \sigma_v \\ \mu_1 \\ \mu_2 \\ \mu_3 \\ \mu_4 \\ \mu_5 \end{pmatrix} \mapsto \begin{pmatrix} \gamma_1 \\ \gamma_2 \\ \gamma_3 \\ \gamma_4 \\ \gamma_5 \end{pmatrix}$$

$$f : U \subset \mathbb{R}^{10} \rightarrow V \subset \mathbb{C}^5$$

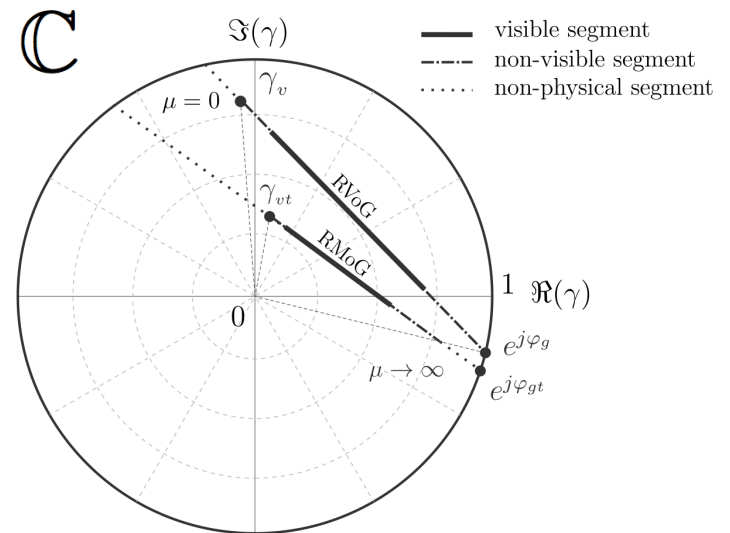
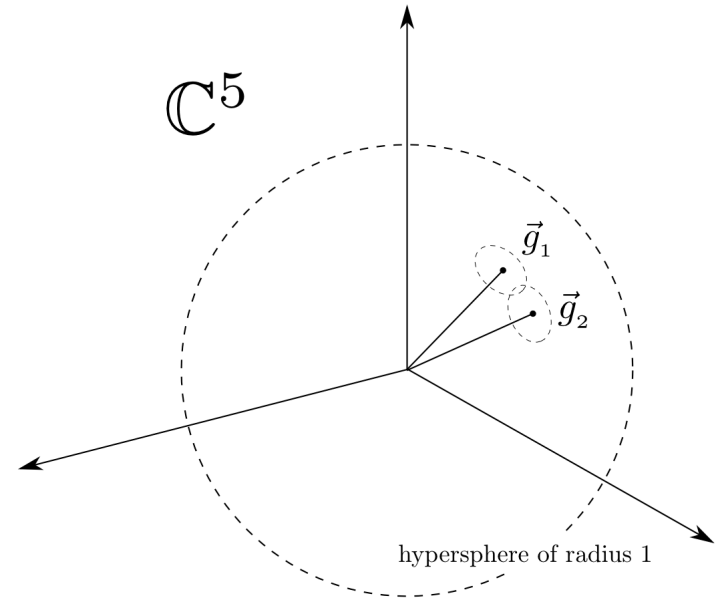


K. Papathanassiou and S. Cloude, "Single-Baseline Polarimetric SAR Interferometry," TGRS, vol. 39, no. 11, pp. 2352–2363, 2001.

I. Hajnsek et Al., "Tropical-Forest-Parameter Estimation by Means of Pol-InSAR: The INDREX-II Campaign," TGRS, vol. 47, no. 2, pp. 481–493, Feb. 2009.

RMoG inverse problem

- The codomain of the RMoG forward problem **is not the coherence locus**
- Two coherence observations are sufficient to estimate the coherence locus, but not the RMoG model parameters
- Values of RMoG model parameters **are inferred** from vector of observations
- The RMoG forward problem is **ambiguous** if two vectors of model parameters map in the same coherence vector



RMoG inversion strategy

1. **Coherence phase optimization** → end points of visible line
2. **Unit circle intersection** → approximate ground phase
3. **Constrained least-square optimization** of non-linear, complex problem using **interior-point algorithm** and analytically-derived gradient

$$\left\{ \begin{array}{l} \widehat{\gamma}_1 e^{-j\varphi_{gt}} = e^{j(\varphi_g - \varphi_{gt})} \frac{\mu_1 \gamma_{tg} + \gamma_{vt} e^{-j\varphi_g}}{\mu_1 + 1} \\ \widehat{\gamma}_2 e^{-j\varphi_{gt}} = e^{j(\varphi_g - \varphi_{gt})} \frac{\mu_2 \gamma_{tg} + \gamma_{vt} e^{-j\varphi_g}}{\mu_2 + 1} \\ \widehat{\gamma}_3 e^{-j\varphi_{gt}} = e^{j(\varphi_g - \varphi_{gt})} \frac{\mu_3 \gamma_{tg} + \gamma_{vt} e^{-j\varphi_g}}{\mu_3 + 1} \\ \widehat{\gamma}_4 e^{-j\varphi_{gt}} = e^{j(\varphi_g - \varphi_{gt})} \frac{\mu_4 \gamma_{tg} + \gamma_{vt} e^{-j\varphi_g}}{\mu_4 + 1} \\ \widehat{\gamma}_5 e^{-j\varphi_{gt}} = e^{j(\varphi_g - \varphi_{gt})} \frac{\mu_5 \gamma_{tg} + \gamma_{vt} e^{-j\varphi_g}}{\mu_5 + 1} \end{array} \right.$$

$$F = \sum_{i=1}^5 |\gamma_i - \widehat{\gamma}_i|^2$$

$$\gamma_i = e^{j\varphi_g} \frac{\mu_i \gamma_{tg} + \gamma_{vt} e^{-j\varphi_g}}{\mu_i + 1}$$

$$\widehat{\gamma}_i = \widehat{\gamma}_1 + F_i (e^{j\varphi_{gt}} - \widehat{\gamma}_1), \quad F_i = \frac{F_5}{4} (i-1)$$

$$\sigma_v \geq \sigma_g$$

$$\nabla f = \begin{pmatrix} \partial\gamma/\partial\varphi_g \\ \partial\gamma/\partial h_v \\ \partial\gamma/\partial\kappa_e \\ \partial\gamma/\partial\sigma_g \\ \partial\gamma/\partial\sigma_v \\ \partial\gamma/\partial\mu_1 \\ \partial\gamma/\partial\mu_2 \\ \partial\gamma/\partial\mu_3 \\ \partial\gamma/\partial\mu_4 \\ \partial\gamma/\partial\mu_5 \end{pmatrix}$$

RMoG inversion: Existence and uniqueness of the solution

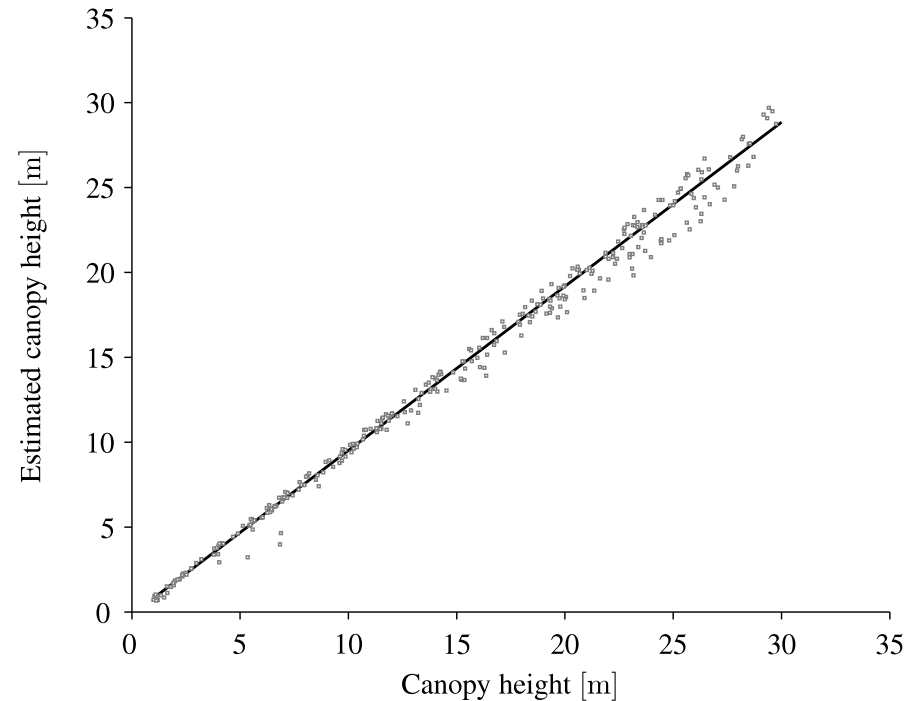
RMoG numerical simulations

- **large range** of model parameters
 - $\varphi_g \in [-\pi, \pi]$ rad
 - $h_v \in [0, 30]$ m
 - $\kappa_e \in [0.1, 0.3]$ dB m⁻¹
 - $\sigma_g = 0$ cm
 - $\sigma_v = 0$ cm
 - $\mu_{\max} \in [0, 10]$ dB
 - $\mu_{\min} \in [-10, -30]$ dB
- **UAVSAR** radar and acquisition geometry
 - $k_z = 0.12$ m⁻¹
 - $\lambda = 0.2384$ m
 - $\theta = 45$ deg
- **300 RMoG coherence** simulations and RMoG inversions

RMoG inversion: Existence and uniqueness of the solution

RMoG numerical simulations

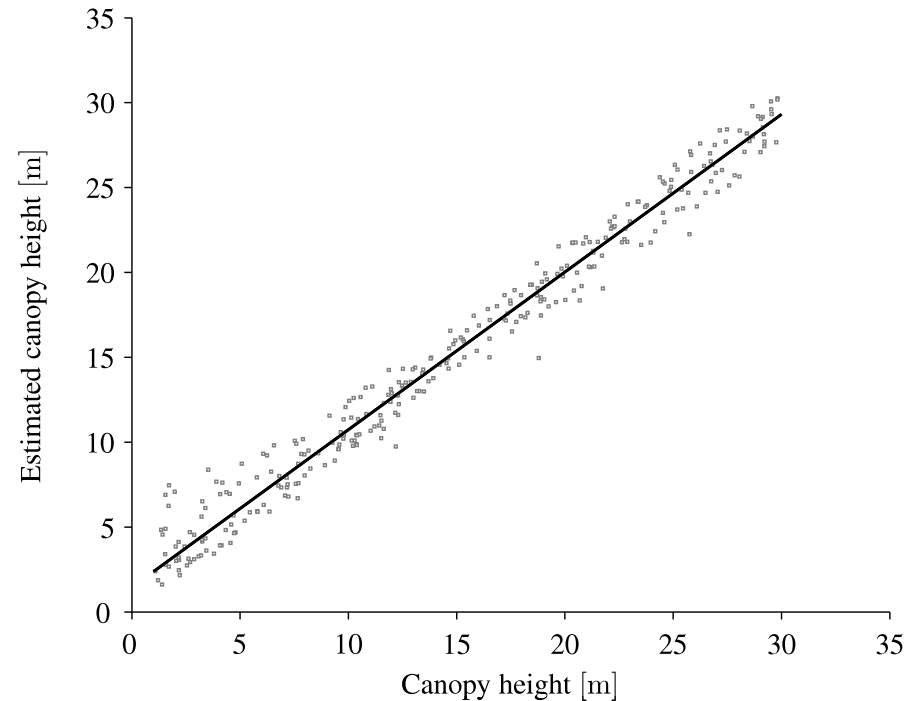
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 - $\varphi_g \in [-\pi, \pi]$ rad
 - $h_v \in [0, 30]$ m
 - $\kappa_e \in [0.1, 0.3]$ dB m⁻¹
 - $\sigma_g \in [0, 1]$ cm ($\gamma_t \simeq 0.87$)
 - $\sigma_v \in [1, 2]$ cm ($\gamma_t \simeq 0.57$)
 - $\mu_{\max} \in [0, 10]$ dB
 - $\mu_{\min} \in [-10, -30]$ dB
- **UAVSAR** radar and acquisition geometry
 - $k_z = 0.12$ m⁻¹
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RMoG inversion: Conditioning of the solution

RMoG numerical simulations

- **linear** motion variance (RMoG model)

$$\sigma^2 = \sigma_g^2 + (\sigma_v^2 - \sigma_g^2) \frac{z - z_g}{h_r}$$

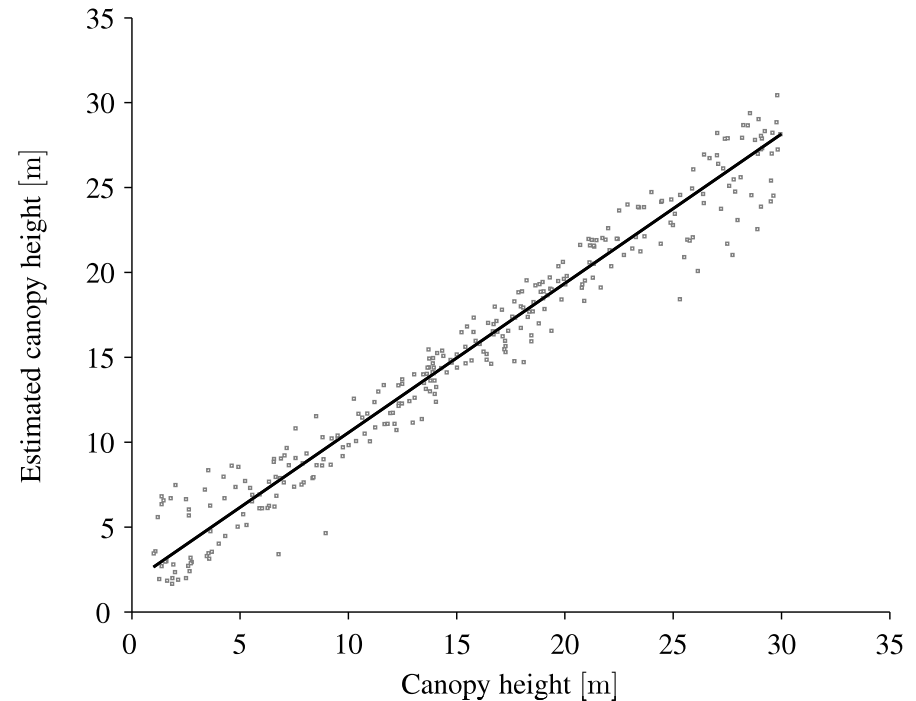
- **exponential** motion variance

$$\sigma^2 = \sigma_g^2 \exp \left[\frac{z - z_g}{h_r} \ln \frac{\sigma_v^2}{\sigma_g^2} \right]$$

- **quadratic** motion variance

$$\sigma^2 = \sigma_g^2 + (\sigma_v^2 - \sigma_g^2) \sqrt{\frac{z - z_g}{h_r}}$$

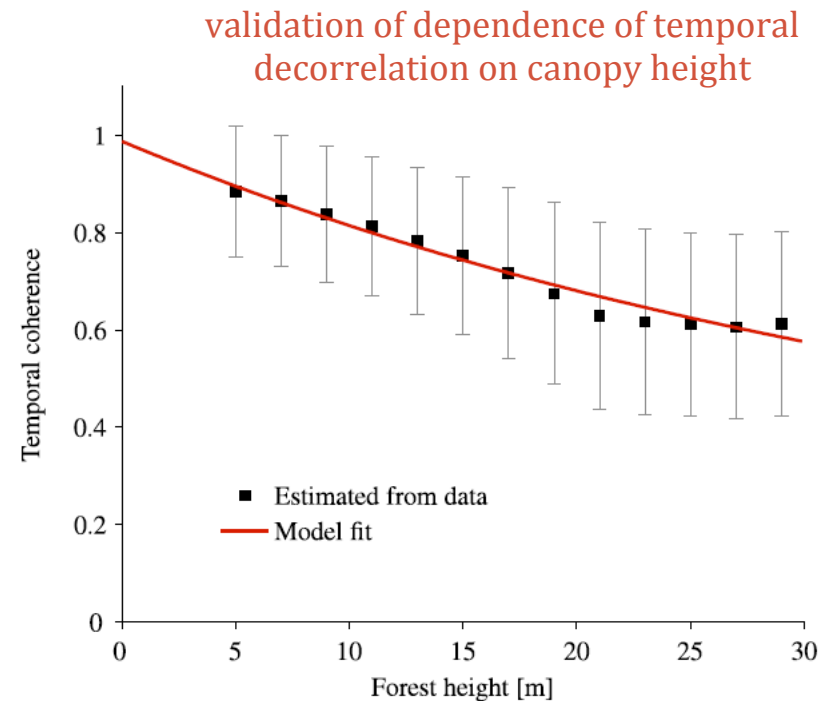
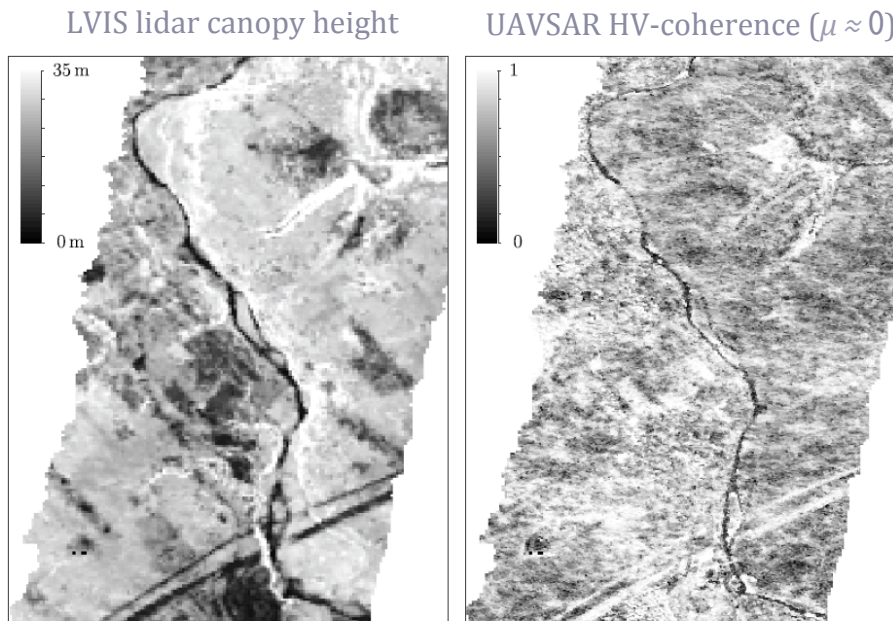
- Exponential- and quadratic-based coherences inverted using the RMoG model



RMoG model VS reality: UAVSAR experiments

Validation of temporal decorrelation model ($b_{\perp} = 0$)

Quebec (Canada); 45 min temporal interval; \sim zero vertical wavenumber; L-band UAVSAR

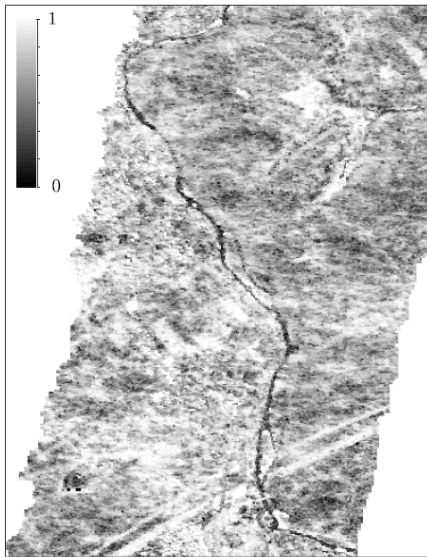


M. Lavalle, M. Simard and S. Hensley, "A temporal decorrelation model for polarimetric radar interferometers", IEEE TGRS 2012.

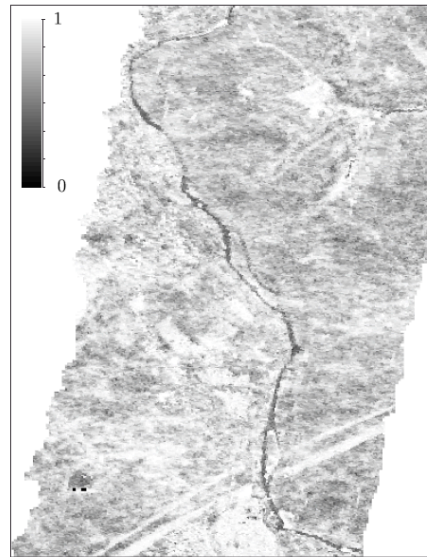
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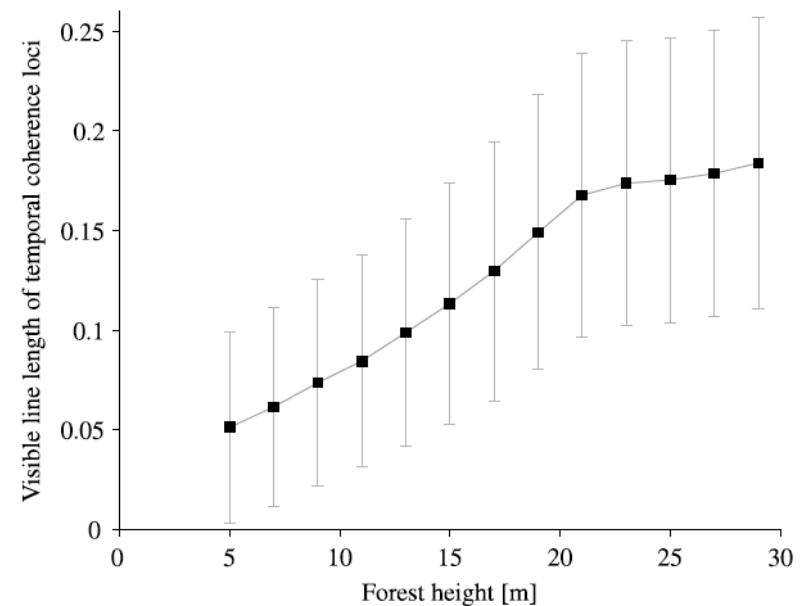
UAVSAR HV-coherence ($\mu \approx 0$)



optimized high coherence



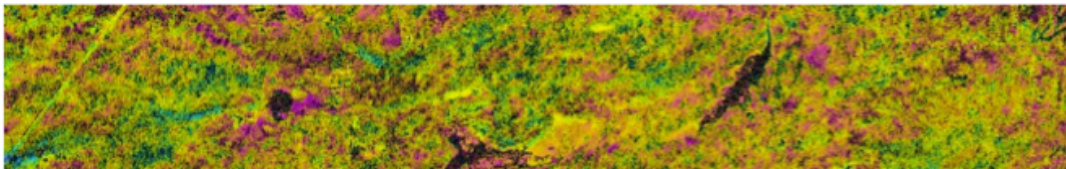
validation of dependence of temporal correlation on wave polarization



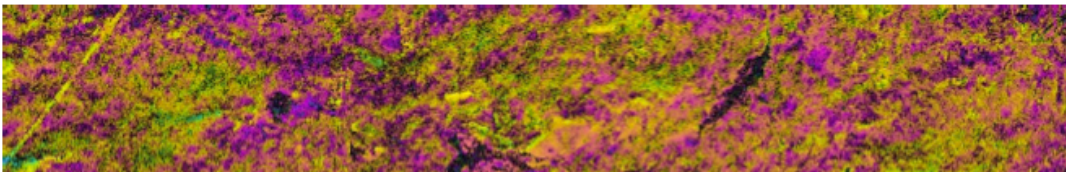
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Tree height from Pol-InSAR UAVSAR data

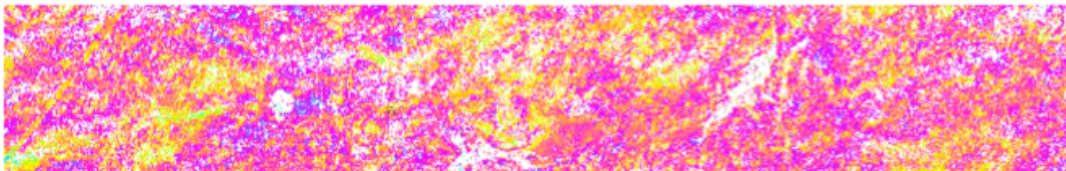
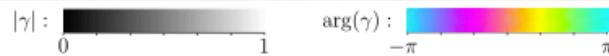
Harvard Forest, MA (US); 2 days temporal interval; 0.075 m^{-1} vertical wavenumber; L-band



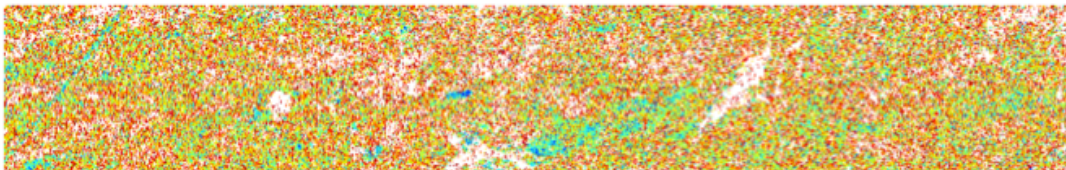
Canopy-dominated coherence



Ground-dominated coherence



Estimated ground topography

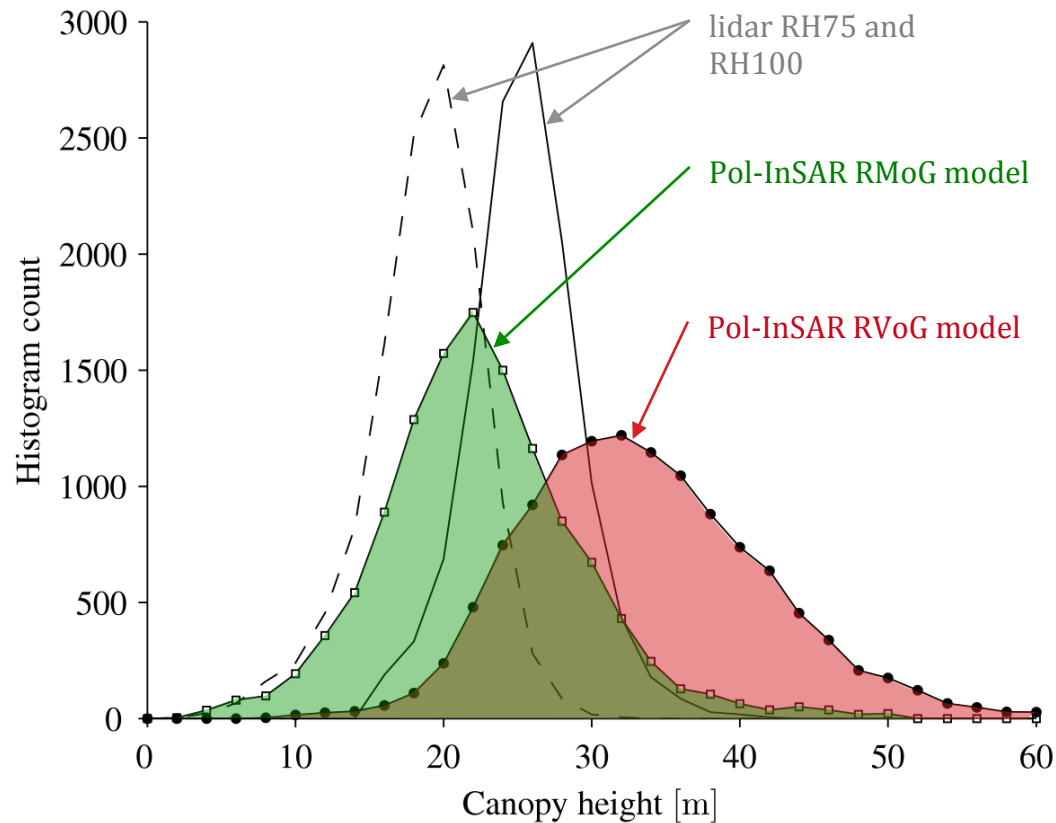


Estimated canopy height



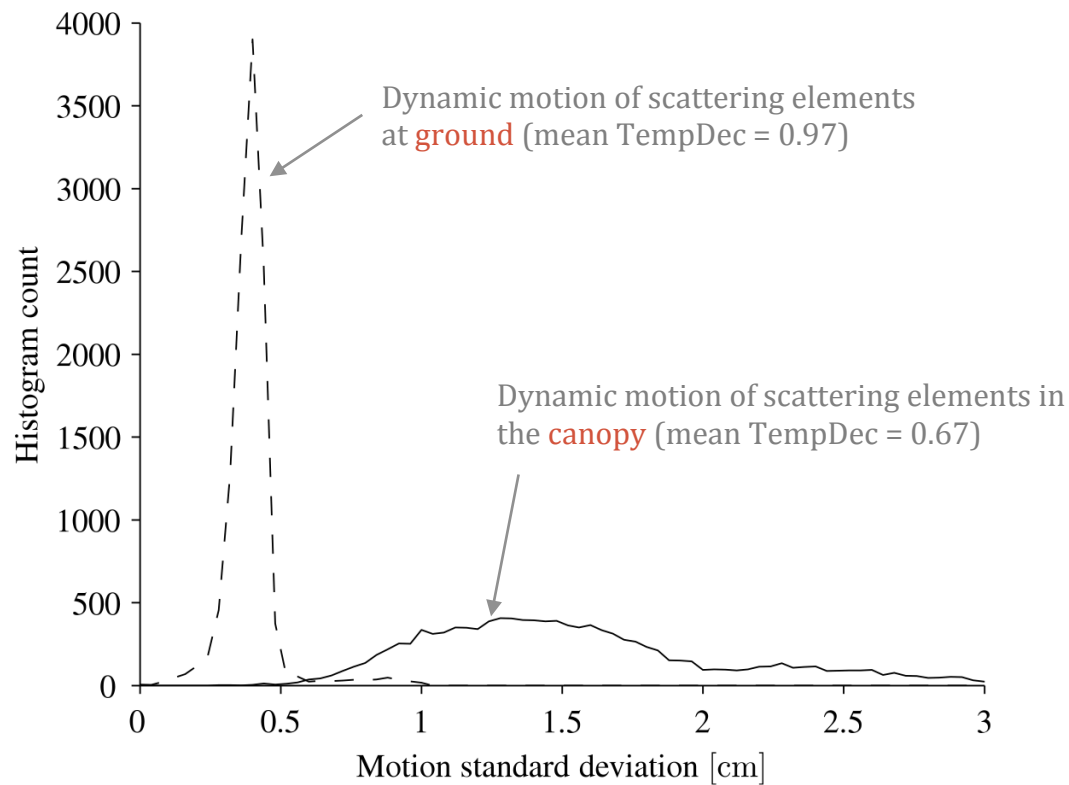
Tree height from Pol-InSAR UAVSAR data VS lidar LVIS

Harvard Forest, MA (US); 2 days temporal interval; 0.075 m^{-1} vertical wavenumber; L-band



RMoG temporal parameters from Pol-InSAR UAVSAR data

Harvard Forest, MA (US); 2 days temporal interval; 0.075 m^{-1} vertical wavenumber; L-band



Conclusions

- Proposed an **inversion strategy** for estimating tree height from single-baseline, repeat-pass Pol-InSAR data using the **RMoG model**
 - **Current strengths:** tree height from single-baseline RP-PolInSAR; model-based inversion with no a-priori assumptions; available with open-source libraries
 - **Current weaknesses:** length of visible line might be short; RMoG doesn't model complex temporal phenomena; inversion might be time consuming
- **Model and method validated** with numerical simulations and **JPL/UAVSAR** data
- Attractive avenue for **estimating forest parameters** using **Pol-InSAR data** from forthcoming radar missions (ALOS-2, SENTINEL-1, DESDynI, BIOMASS)