Observation quality control: methodology and applications

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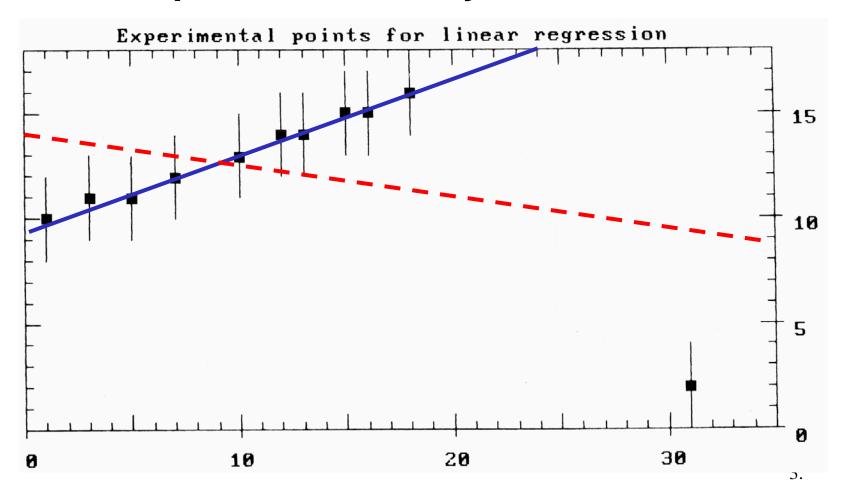
Presentation at the
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Introduction

- Nature of data received and used at operational centres
 - * Wide variety of data that come from numerous sources
 - * Many possible problems can corrupt the data
- Incorrect data can have a significant impact on the assimilation
- Data acquisition and quality control
 - Reception of the data
 - Check the quality of the data and reject data that have a high probability of being erroneous

Example: least-square fit involving an erroneous datum (from Tarantola, 2005)

Least-square fit of data: y = ax + b

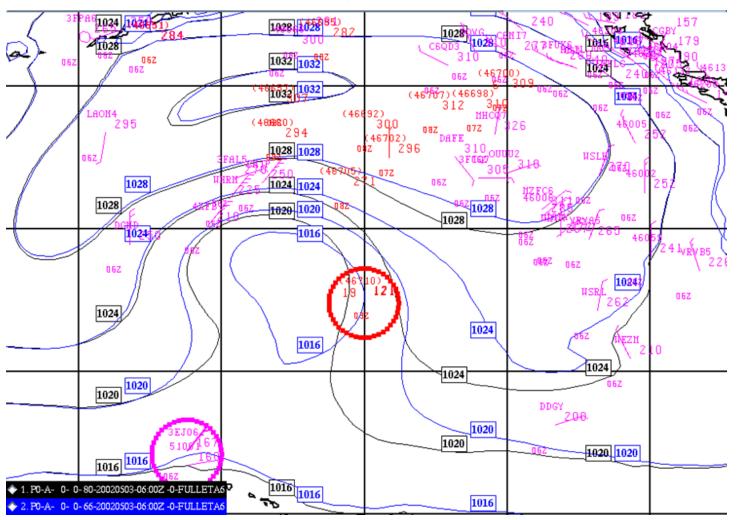


Impact of an erroneous datum on the analysis

Report from a drifting buoy:p = 1012.1 hPa (10 hPa too low)

Analysis with QC in black

Analysis without QC in blue



Quality Control

Sources of errors :

- * measurement errors inherent in the instruments
- * error of representativeness
- * improperly calibrated instruments
- * incorrect registration of observations
- * data coding errors
- data transmission errors

Goals :

- reject all errors other than measurement errors
- associate predefined flags with each observation throughout its assimilation

Quality Control

Preliminary checks for individual reports :

- at decoding stage, verification of observation source and location
- hydrostatic checks for temperatures and geopotential heights from upper air soundings
- * check for limiting wind shear in wind profiles from upper air soundings
- verification of deviation from climatological values

Quality Control

Limit values for surface temperature								
	Winter			Summer				
Area	Min2	Min1	Max1	Max2	Min2	Min1	Max1	Max2
45°S - 45°N	-40°C	-30°C	+50°C	+55°C	-30°C	-20°C	+50°C	+60°C
45°N - 90°N 45°S - 90°S	-90°C	-80°C	+35°C	+40°C	-40°C	-30°C	+40°C	+50°C

Limit values for surface dew-point temperature								
	Winter				Summer			
Area	Min2	Min1	Max1	Max2	Min2	Min1	Max1	Max2
45°S - 45°N	-45°C	-35°C	+35°C	+40°C	-35°C	-25°C	+35°C	+40°C
45°N - 90°N 45°S - 90°S	-99°C	-85°C	+30°C	+35°C	-45°C	-35°C	+35°C	+40°C

Notations

Model state

x: model state comprising 3D and surface atmospheric

fields $(N=NV3D \times NLEVELS \times NI \times NJ \sim 10^8)$

x_b: background state (*a priori* estimate of the state of the

atmosphere)

x_t: true (unknown state) of the atmosphere

 $\varepsilon_b = \mathbf{x}_b - \mathbf{x}_t$: background error

Observations

y: observation vector (M~10⁶)

 \mathbf{y}_{t} : true observations

 $\varepsilon_0 = \mathbf{y} - \mathbf{y}_f$: observation error

Notations

Observation operator

H: observation operator producing a model equivalent of

all observations ($R^N \rightarrow R^M$)

 $\mathbf{H} = (\partial H/\partial \mathbf{x})$: Jacobian of the observation operator

(linear operator associated with an (MxN) matrix)

Error statistics

R: observation error covariance matrix (MxM)

(diag **R** = σ_o^2 observation error variances)

B: background error covariances

(diag **B** = σ_b^2 background error variances)

HBH^T: image in observation space of the background error

covariances

Information contained in innovations

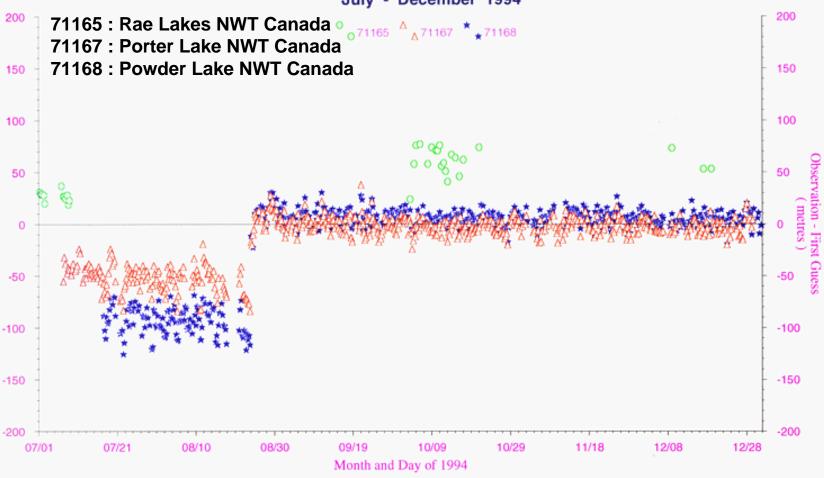
- Innovation vector: $d = y H(x_b)$
 - * short-term forecast (background) contains information gained from past observations
 - * Comparison of observations against the background which is our *a priori* knowledge of the state of the atmosphere
 - * Offers a common ground against which it is possible to compare all observations

Monitoring of observations

- innovations are represented by observation types and averaged over a large number of data, binned according to different categories
- * Allows to detect systematic problems with observations

Residuals of Geopotential 71165, 71167 and 71168

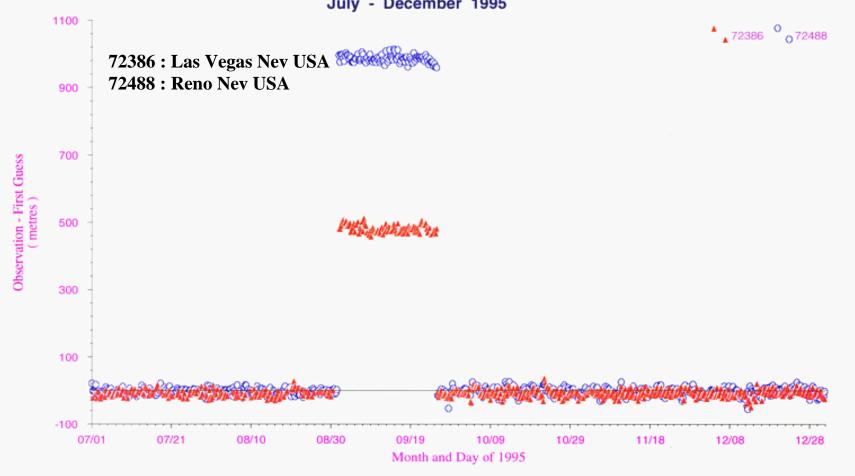
July - December 1994



wrongly assigned station elevation

Residuals of Geopotential 72386 and 72488

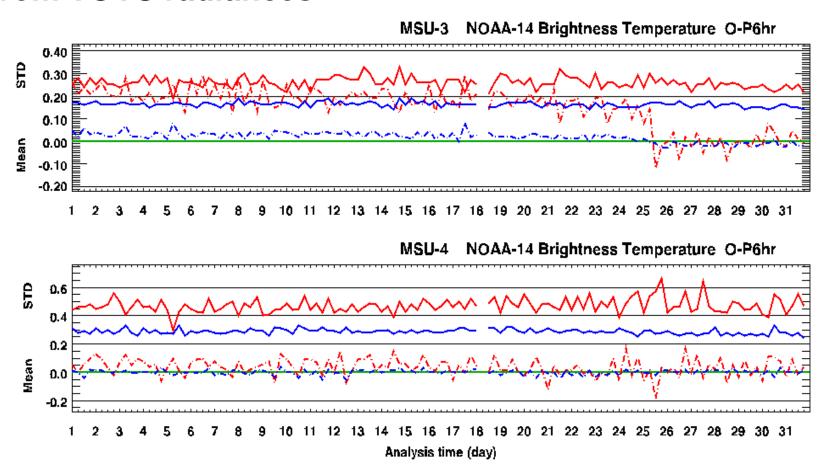
July - December 1995



wrongly assigned station pressure

Monitoring and quality control

Statistics based on innovations (y -HX_b): example from TOVS radiances



Monitoring Web Site of the Canadian Meteorological Centre (CMC)

http://collaboration.cmc.ec.gc.ca/cmc/data_monito ring/

User: monitoring

Password: CMC

with CMC in uppercase.

Verification against the background state

• Observation departure from x_b : $d = y - H(x_b)$

$$\mathbf{y} - \mathbf{H}(\mathbf{x}_b) = \mathbf{y}_t + \varepsilon_o - H(\mathbf{x}_t + \varepsilon_b) \cong (\mathbf{y}_t - H(\mathbf{x}_t)) + \varepsilon_o - \mathbf{H}' \varepsilon_b$$
$$= \varepsilon_o - \mathbf{H}' \varepsilon_b$$

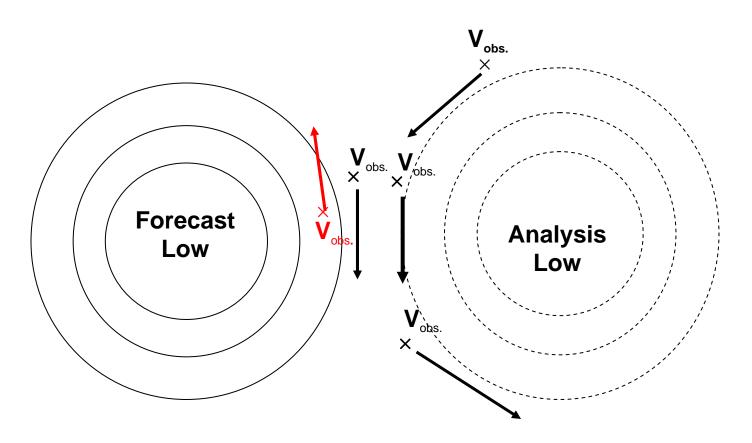
$$\langle (\varepsilon_o - \mathbf{H}' \varepsilon_b) (\varepsilon_o - \mathbf{H}' \varepsilon_b)^T \rangle = \mathbf{R} + \mathbf{H}' \mathbf{B} \mathbf{H}'^T$$

- For a single observation: $(y H(\mathbf{X}_b))^2 \cong \sigma_o^2 + \sigma_b^2$
- Need to compute H'BH'
 which can be done by a randomization method
- Observation is rejected if

$$\hat{y} = y - H\mathbf{x}_b \ge \lambda(\sigma_o^2 + \sigma_b^2)^{1/2}$$

with λ being large enough.

Difficulties that arise with the background-check procedure



Quality control based on local analyses

- Consider a set of k observations y₁, ..., y_k
- Probability of $y_1 = y_t$ assuming that all the other observations are true
- Analysis is made using all observations but y₁ and then comparing y₁ against the resulting analysis

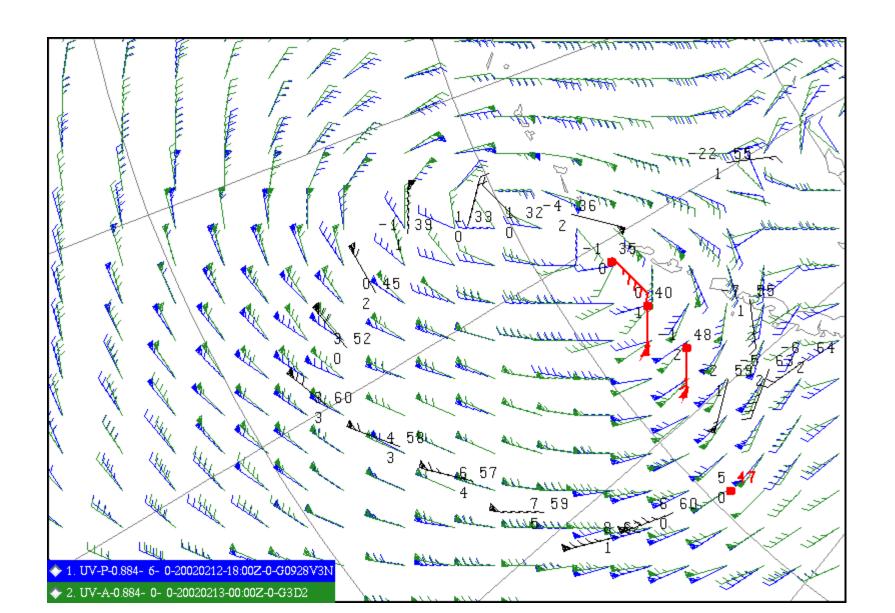
$$\left(y - H(\mathbf{X}_a^{(k-1)})\right)^2 = \sigma_o^2 + \sigma_a^2$$

$$\hat{y} = y - H \mathbf{x}_a^{(k-1)} \ge \lambda (\sigma_o^2 + \sigma_a^2)^{1/2}$$

 To avoid contamination by erroneous data, the procedure is repeated until no more data are being rejected

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Dropsonde data rejected by Bgnd Check



Bayesian approach to inverse problems

Joint probability distribution function (pdf): p(x,y)

Associated marginal probability densities

$$P(\mathbf{x}) = \int p(\mathbf{x}, \mathbf{y}) d\mathbf{y}, \quad P(\mathbf{y}) = \int p(\mathbf{x}, \mathbf{y}) d\mathbf{x}$$

- * A priori pdf $P(\mathbf{x})$: probability of $\mathbf{x} = \mathbf{x}_t$
- * Example: the Gaussian case in which we know the error covariance and we have \mathbf{x}_h as the only realization of \mathbf{x} .

$$P(\mathbf{x}) = \frac{1}{C} \exp\left\{-\frac{1}{2} (\mathbf{x} - \mathbf{x}_b)^T \mathbf{B}^{-1} (\mathbf{x} - \mathbf{x}_b)\right\}$$

x in normally distributed with mean **x**_b and covariance **B**

In absence of any other information, $\mathbf{x} = \mathbf{x}_b$ is the most probable state

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Similarly, for P(y), if y_0 stands for the actual observation,

P(y) : probability of $y = y_t$

Estimate of the mean : $y = y_0$

Gaussian case :

$$P(\mathbf{y}) = \frac{1}{C_2} \exp\left\{-\frac{1}{2} (\mathbf{y} - \mathbf{y}_o)^T \mathbf{R}^{-1} (\mathbf{y} - \mathbf{y}_o)\right\}$$

* Normally distributed with mean **y**_o and covariance **R**

Bayes' Theorem

Conditional probability distribution

Probability of having \mathbf{y} given that $\mathbf{x} = \mathbf{x}_t$

$$p(\mathbf{y} \mid \mathbf{x} = \mathbf{x}_t) = \frac{p(\mathbf{x}_t, \mathbf{y})}{\int p(\mathbf{x}_t, \mathbf{y}) d\mathbf{y}} \equiv \frac{p(\mathbf{x}_t, \mathbf{y})}{P(\mathbf{x}_t)}$$

Probability of having **x** given that $\mathbf{y} = \mathbf{y}_{\circ}$

$$p(\mathbf{x} \mid \mathbf{y} = \mathbf{y}_o) = \frac{p(\mathbf{x}, \mathbf{y}_o)}{\int p(\mathbf{x}, \mathbf{y}_o) d\mathbf{x}} \equiv \frac{p(\mathbf{x}, \mathbf{y}_o)}{P(\mathbf{y}_o)}$$

Thus, $p(\mathbf{x}_t, \mathbf{y}_0) = p(\mathbf{x}_t | \mathbf{y}_0) P(\mathbf{y}_0) = p(\mathbf{y}_0 | \mathbf{x}_t) P(\mathbf{x}_t)$

Bayes' Theorem:
$$p(\mathbf{x} \mid \mathbf{y} = \mathbf{y}_o) = \frac{p(\mathbf{y} \mid \mathbf{x} = \mathbf{x}_t)P(\mathbf{x} = \mathbf{x}_t)}{P(\mathbf{y} = \mathbf{y}_o)}$$

Conditional probability

- p(x|y): probability that x= x_t given that y = y_o has been observed
 - * A posteriori probability distribution associated with that of the analysis error
- p(y|x=x_t): probability of y given that x is the true value
 - * **Hx**: estimate of the mean value of **y**.

$$\rightarrow$$
 If $\mathbf{x} = \mathbf{x}_t$, then $\mathbf{H}\mathbf{x}_t = \mathbf{y}_t$.

- * $(\mathbf{y} \mathbf{H}\mathbf{x}) = \mathbf{y}_t + \varepsilon_o \mathbf{H}\mathbf{x}_t = \varepsilon_o$
- * (y Hx) is normally distributed with zero mean and covariance R

$$p(\mathbf{y} | \mathbf{x}) = \frac{1}{C_3} \exp \left\{ -\frac{1}{2} (\mathbf{y} - \mathbf{H} \mathbf{x})^T \mathbf{R}^{-1} (\mathbf{y} - \mathbf{H} \mathbf{x}) \right\}$$

Representation of the associated probability distributions (Rodgers, 2000) $P(\mathbf{y}|\mathbf{x})$ У 1 $\mathbf{H}\mathbf{x}_{\mathrm{b}}$ \mathbf{y}_{t} **y**o $P(\mathbf{y})$ $P(\mathbf{x})$

Mode:
$$\frac{d}{dx}(-\ln p) = -\frac{1}{p}\frac{dp}{dx} = 0 \implies \frac{dp}{dx} = 0$$

From Bayes' theorem:

$$p(x \mid y) = C \frac{\exp\left\{-\frac{1}{2}(\mathbf{y} - \mathbf{H}\mathbf{x})^T \mathbf{R}^{-1}(\mathbf{y} - \mathbf{H}\mathbf{x})\right\} \exp\left\{-\frac{1}{2}(\mathbf{x} - \mathbf{x}_b)^T \mathbf{B}^{-1}(\mathbf{x} - \mathbf{x}_b)\right\}}{\exp\left\{-\frac{1}{2}(\mathbf{y} - \mathbf{y}_o)^T \mathbf{R}^{-1}(\mathbf{y} - \mathbf{y}_o)\right\}}$$

$$-\ln p(\mathbf{x}|\mathbf{y}) = J(\mathbf{x})$$

$$= \frac{1}{2} (\mathbf{x} - \mathbf{x}_b)^T \mathbf{B}^{-1} (\mathbf{x} - \mathbf{x}_b)^T + \frac{1}{2} (\mathbf{H}\mathbf{x} - \mathbf{y})^T \mathbf{R}^{-1} (\mathbf{H}\mathbf{x} - \mathbf{y}) + C$$

- In the case of Gaussian error statistics, the maximum likelihood and the minimum variance estimate coincide.
- Formulation includes the case where H(x) is nonlinear.

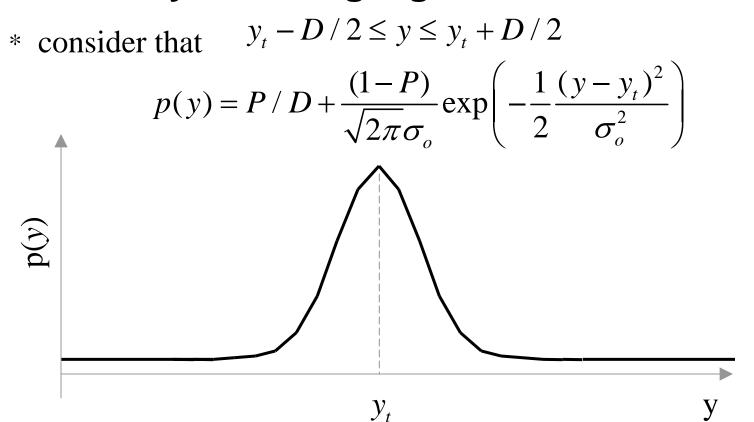
References

Rodgers, R.D., 2000: *Inverse Methods for Atmospheric Sounding: theory and practice*. World Scientific Series On Atmospheric and Planetary Physics, vol.2, 238 pages.

Tarantola, A., 2005: *Inverse problem theory and methods for model parameter.* SIAM, Philadelphia, USA, 342 pages.

Variational Quality Control (QC-Var)

- Dharssi et al. (1992), Ingleby and Lorenc (1993),
 Andersson and Järvinen (1999)
- Probability of having a gross error



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QC-Var

Definition of the cost function

$$J_o^{QC}(\mathbf{X}) \equiv J_o^{QC}(\hat{y}(\mathbf{X})) = -\ln p(y_o \mid H(\mathbf{X}))$$
 where
$$= -\ln \left(P/D + C \exp\left(-J^N(\hat{y})\right)\right)$$

$$J^{N}(\hat{y}(\mathbf{x})) = \frac{1}{2} \hat{y}^{T} \mathbf{R}^{-1} \hat{y} \equiv \frac{1}{2} \frac{(H(\mathbf{x}) - y_o)^2}{\sigma_o^2}$$

Gradient of the QC-Var cost function

$$\nabla_{\hat{y}} J_o(\mathbf{x}) = \frac{\exp(-J^N)}{\gamma + \exp(-J^N)} \nabla_{\hat{y}} J^N(\hat{y}) \equiv W_{QC} \nabla_{\hat{y}} J_o^N(\hat{y})$$

$$= W_{QC} \frac{(H(\mathbf{x}) - y_o)}{\sigma_o^2}$$

$$\nabla_{\mathbf{x}} J_o(\mathbf{x}) = \left[\frac{\partial H}{\partial \mathbf{x}}(\mathbf{x})\right]^* W_{QC} \frac{(H(\mathbf{x}) - y_o)}{\sigma_o^2}$$

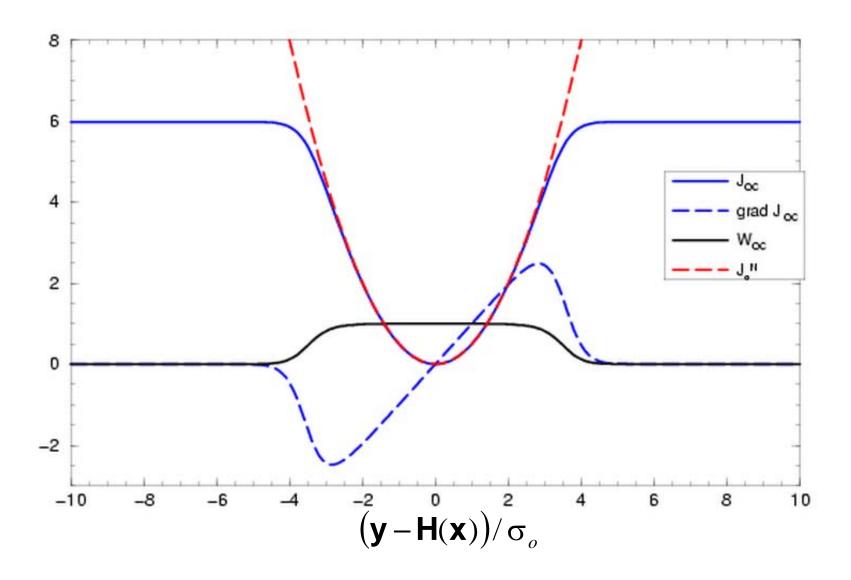
where
$$\gamma = (P\sigma_o \sqrt{2\pi})/(1-P)D$$

 W_{QC} depends on the current estimate of the state.

 A posteriori weights are then based on the departure from the analysis

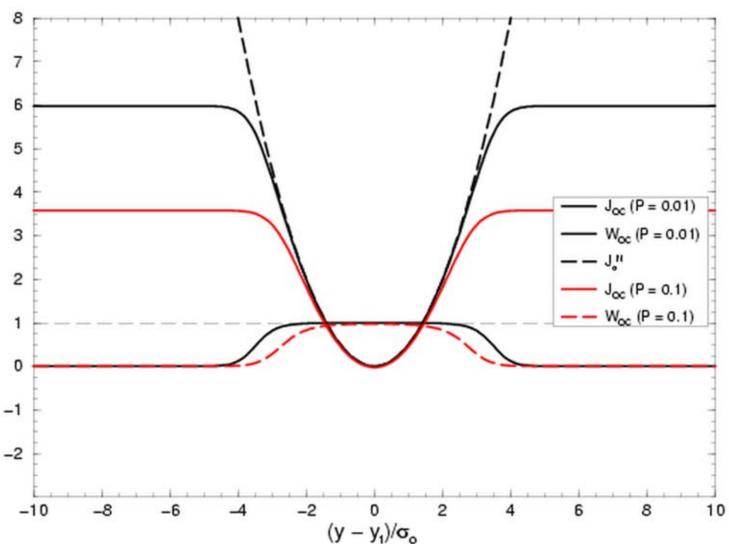
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Representation of the QC-Var cost function (P = 0.01)

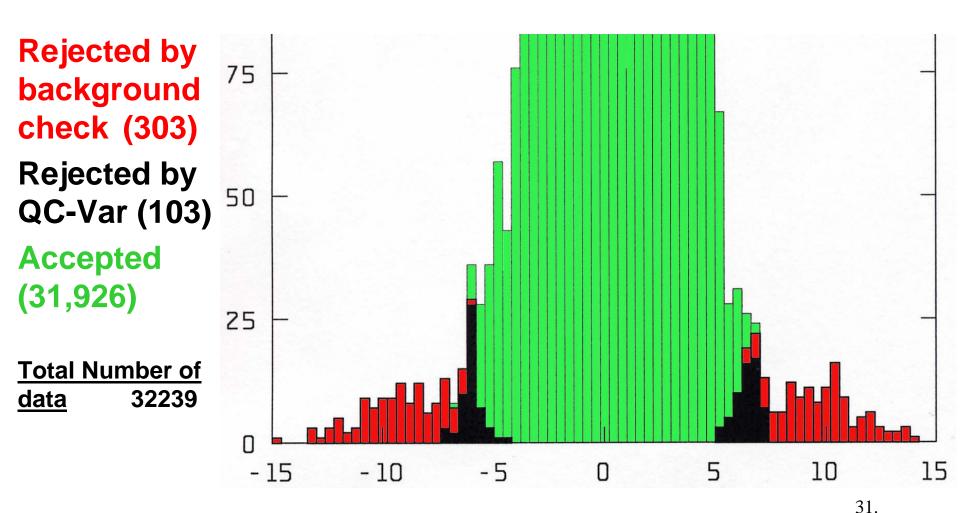


QC-Var cost function with different probabilities

of gross errors (P = 0.01 and 0.1)



Observation - Forecast $(y - H(x_b))$ AIREP temperatures Period: March-April 2002



Estimation of the probability of gross error

Distribution innovations

Gaussian:

Jaussian:

$$-\ln p(\hat{y}) = \frac{\hat{y}^2}{2\sigma_o^2} + C$$

$$\frac{\hat{y}}{2\ln p(\hat{y})} = \frac{\hat{y}}{2\sigma_o^2}$$

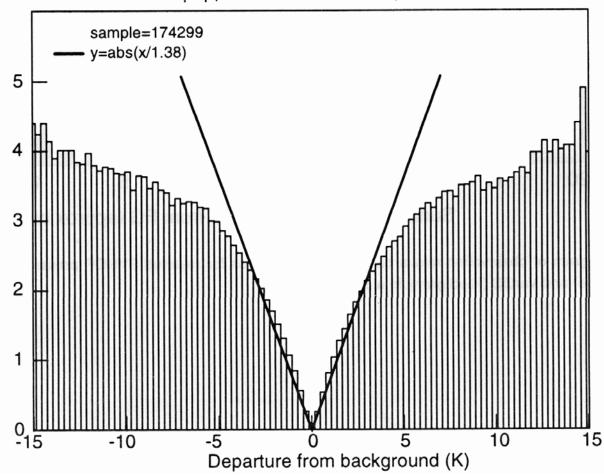
$$\sqrt{-2\ln p(\hat{y})} = \frac{\hat{y}}{\sigma_o}$$

Probability of gross error is obtained in the limit where

$$|\hat{y}| >> \sigma_o$$

AIREP Temperature

apdp, 1997041919970502, 00 06 12 18



(from Järvinen and Andersson, 1999)

Comparison of the two QC procedures

Obs.	Obs. Quantity	Rejection Ratio		Approxim ate		
Type		(%)		Rejection Limits		
		VarQC	OIQC	VarQC	OIQC	
SYNOP	Pressure (height)	2.7	1.9	3.6 hPa	n/a	
	(T- T _d)	0.3	0.0	8.5 K	22 K	
	Temperature	2.2	1.2	6.6 K	16.6 K	
SHIP	W ind Pressure (height)	7.6 2.3	0.5 3.5	8 m/s 8.5 hPa	19 m/s n/a	
	(T- T _d)	0.3	0.0	9.5 K	26 K	
	Temperature	1.5	0.9	5.7 K	11.7 K	
DRIBU	Pressure (height) Temperature	2.8 3.1	3.1 2.4	6.6 hPa 5.8 K	n/a 6.2 K	
TEMP	Wind	2.7	0.4	8 - 14 m/s	11 - 20 m/s	
	(T- T _d)	1.8	0.0	5 - 16 K	14 - 22 K	
	Temperature	3.0	1.3	2.1 - 6.6 K	3.4 - 9.4 K	

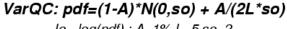
Obs. Type	Obs. Quantity	Rejection Ratio (%)		Approximate Rejection Limits		
		VarQC	OIQC	VarQC	OIQC	
AMDAR	Wind Temperature	1.0 0.7	0.4 0.5	11 m/s 4.0 K	15 m/s 5.0 K	
SATOB	Wind	1.3	0.2	13 - 27 m/s	16 - 36 m/s	
AIREP	Wind	5.2	1.0	13 m/s	29 m/s	
	Temperature	1.7	0.8	5.7 K	9.2 K	
ACARS	Wind	2.3	1.0	10 m/s	14 m/s	
	Temperature	1.6	2.1	4.0 K	5.0 K	

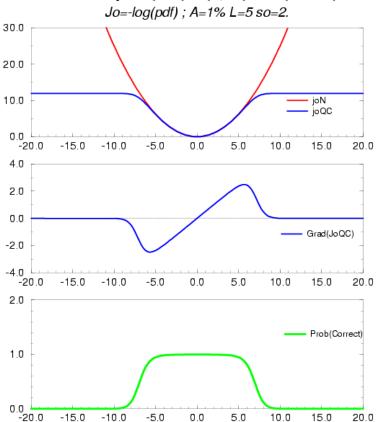
Comments

- When observation error is uncorrelated:
 - QC-Var is easy to implement and computationally inexpensive
 - * A number of iterations need to be done *without* the $W_{\mathcal{QC}}$ to correct main deficiencies that may exist in the background state (assuming the bulk of the observations to be good ones)
- Procedure aims at detecting punctual observations that may be in error
- Complexities arise when observation errors are correlated but they can be addressed (Järvinen et al.,1999)

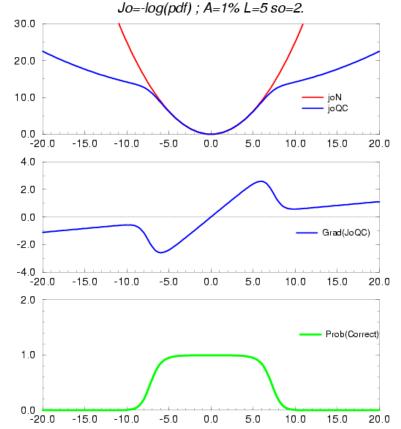
Gaussian + flat PDF

Sum of 2 Gaussians





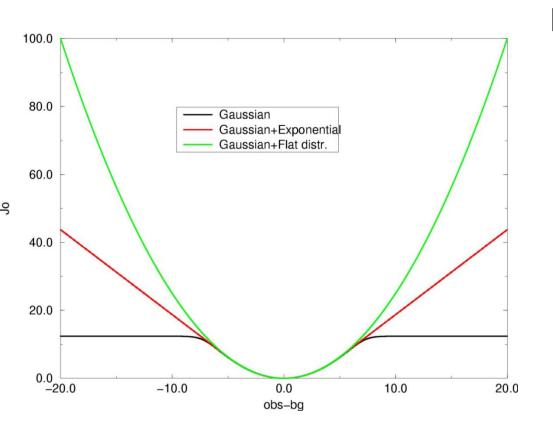
VarQC: pdf=(1-A)*N(0,so) + A*N(0,3*so)



(Isaksen, 2010 ECMWF)

Recent developments in variational quality control

(Isaksen, L., 2010: presentation at the ECMWF training course)



Huber norm

- * Adds some weight on observations with large departures
- * A set of observations with consistent large departures will influence the analysis

Definition of the pdf associated with the Huber norm

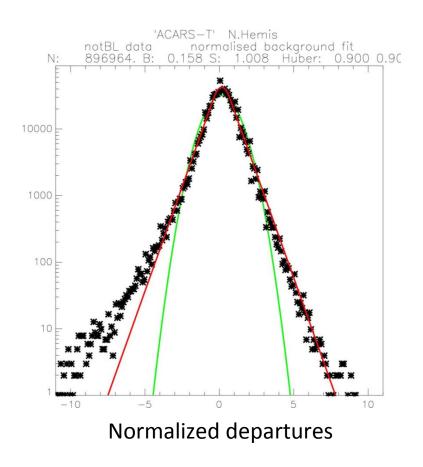
$$p(y|x) = \begin{cases} \frac{1}{\sigma_o \sqrt{2\pi}} \exp\left(\frac{a^2}{2} - |ad|\right) & \text{if } a < d \\ \frac{1}{\sigma_o \sqrt{2\pi}} \exp\left(-\frac{1}{2}d^2\right) & \text{if } a \le d \le b \\ \frac{1}{\sigma_o \sqrt{2\pi}} \exp\left(\frac{b^2}{2} - |bd|\right) & \text{if } d > b \end{cases}$$

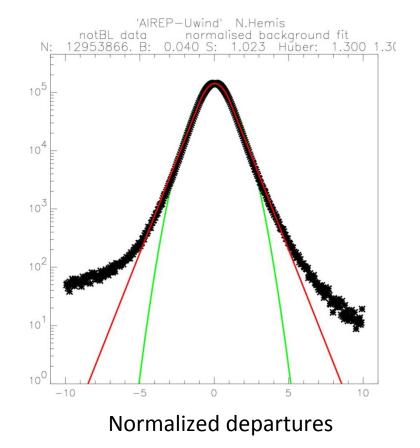
with

$$d = \frac{y - H(\mathbf{X})}{\sigma_o}$$

Aircraft temperature and winds Northern Hemisphere

Huber norm distributed with some deviation for cold departures



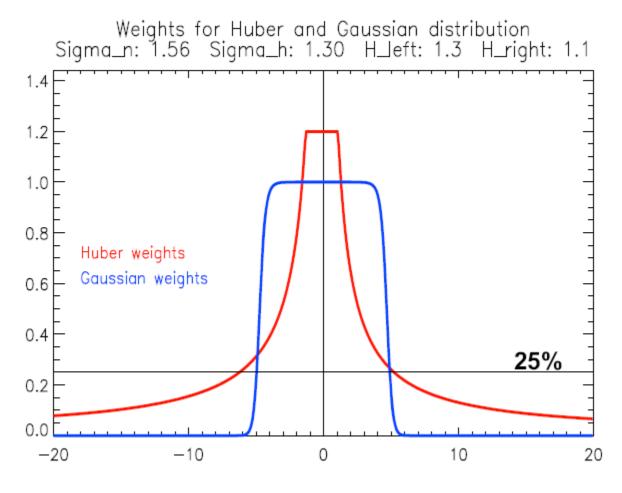


(Isaksen, 2010 ECMWF)

Comparing observation weights:

Huber-norm (red) versus Gaussian+flat (blue)

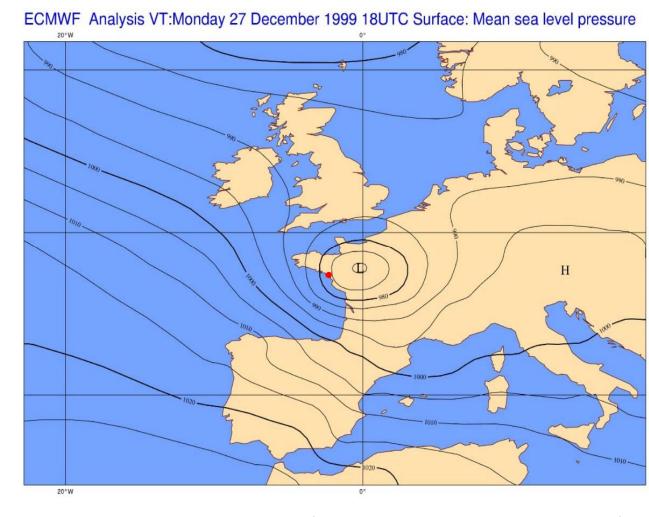
- More weight in the middle of the distribution
- More weight on the edges of the distribution
- More influence of data with large departures
 Weights: 0 – 25%



(Isaksen, 2010 ECMWF)

27 Dec 1999 – French storm 18UTC (Example from Isaksen, 2010 ECMWF)

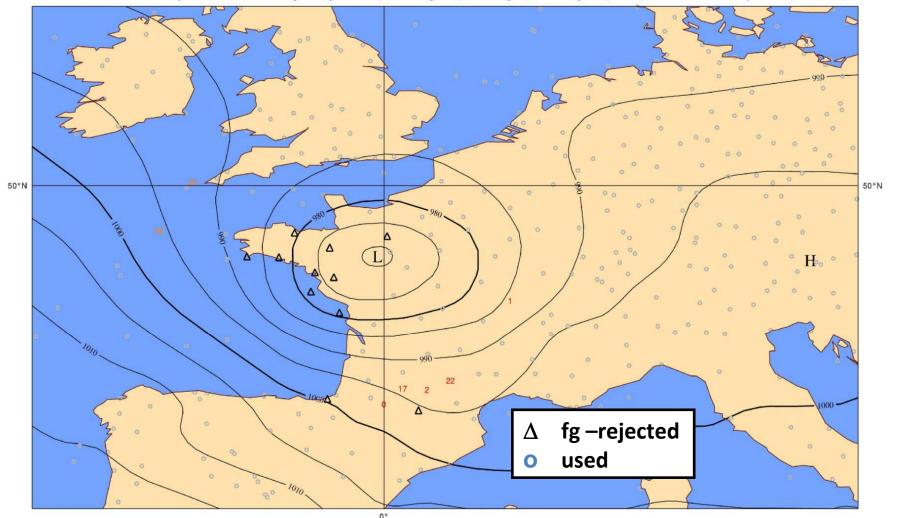
- •Era interim analysis produced a low with min 970 hPa
- Lowest pressure observation (SYNOP: red circle)
- -963.5 hPa (supported by neighbouring stations)
- At this station the analysis shows 977 hPa
- -Analysis wrong by 16.5 hPa!



(Isaksen, 2010 ECMWF)

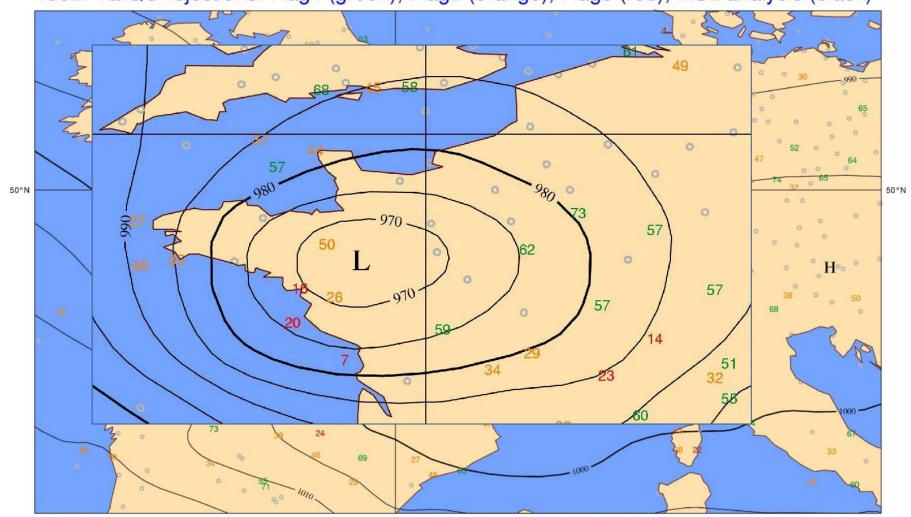
Data rejection and VarQC weights (Isaksen 2010)

1112: VarQC-rejections: Flag1 (green), Flag2 (orange), Flag3 (red), MSL analysis (black)



Data rejection and VarQC weights with Huber norm formulation (Isaksen, 2010)

1362: VarQC-rejections: Flag1 (green), Flag2 (orange), Flag3 (red), MSL analysis (black)



Conclusion

- Quality control is a crucial component of any data assimilation system
- Acceptance of bad data and rejection of good data happens
 - * to avoid this as much as possible, the error characteristics need to be regularly reestimated (e.g., probability of gross error, existence of biases, background and observational error covariances).
- In 4D-Var, small changes to the analysis can lead to substantial differences in the forecast
 - Impact of accepting bad data or rejecting good ones can be significant
- Management of a huge database of information associated with the observations is technically challenging

Bias correction

(from Auligné. McNally and Dee, QJ 2007)

A quick introduction to bias correction

- Systematic errors in the analysis can be attributed to observation and/or background error
- Biases can be observed in innovations for a particular instrument
 - * If no bias is observed for other instruments, then it is likely the observations that is biased
- Principle in bias correction schemes
 - * Find a way to detect biases (e.g., monitoring) and relate it to likely causes of the source of systematic error and correct it
 - Example: systematic error associated with the scan angle of a satellite instruments.

Static bias correction

- Consider innovations d = y -H(x_b) over a period of time (order of a month)
- Modify the observation operator as

$$\tilde{H}(\mathbf{x}, \boldsymbol{\beta}) = H(\mathbf{x}) + \sum_{i=0}^{N} \beta_i P_i(\mathbf{x})$$

• Find the coefficients β by minimising

$$J(\beta) = \frac{1}{2} \left(\mathbf{y} - \tilde{H} \left(\mathbf{x}_{b}, \beta \right) \right)^{T} \left(\mathbf{y} - \tilde{H} \left(\mathbf{x}_{b}, \beta \right) \right)$$

 The quantities P_i(x) are the predictors which relate to the measurements

Predictors used for different satellite instruments

Instrument		Predictors		
AIRS	1000-300	200-50	10-1	50-5
ATOVS	1000-300	200-50	10-1	50-5
GEOS	1000-300	200-50	TCWV	
SSMI	V _s	T _s	TCWV	

- Geopotential thicknesses for the layers comprised between the pressures (in hPa)
- TCWV: total content in water vaport
- V_s : surface wind speed T_s : skin temperature

Limitations of the static scheme

- Bias is assumed to be constant over the period
 - Inappropriate to detect instrument problems
- Based on the assumption that the background error itself is unbiased

- * Background error is constrained by all observations
 - Justified where in biased of set vations are prailed to a radiosondes)

Adaptive offline scheme

Bias correction is recalibrated before every analysis

- Second term $= \frac{1}{ac} (8 = 4 \times mem dry)^T R^{-1} (8 \times mem dry)^$
 - * Could be interpreted as a static scheme applied with a running mean. $+\frac{1}{2}(\beta-\beta_b)^{\beta}\mathbf{B}_{\beta}^{-1}(\beta-\beta_b)$

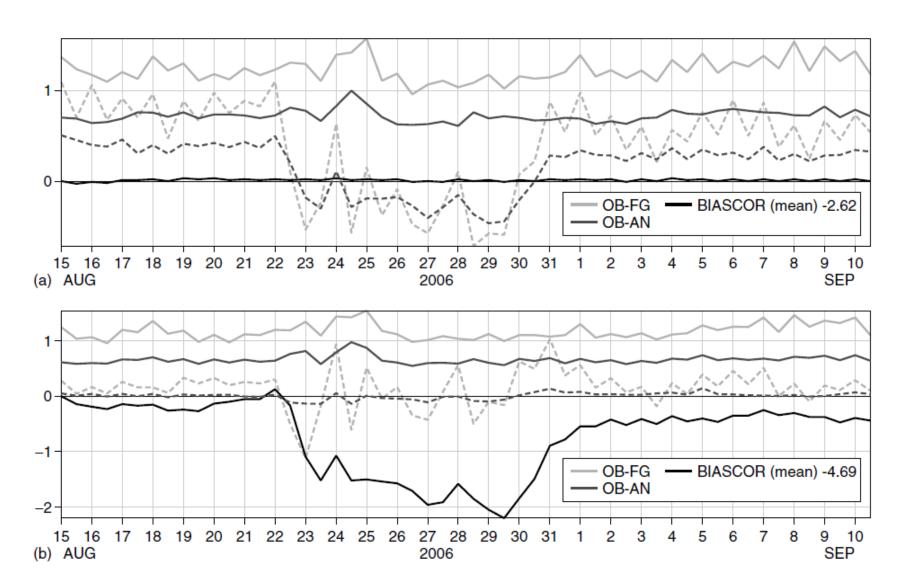
Adaptive online scheme: Var-BC

Bias correction is incorporated within the assimilation scheme itself

$$J(\beta) = \frac{1}{2} (\mathbf{y} - \tilde{H}(\mathbf{x}_b, \beta))^T \mathbf{R}^{-1} (\mathbf{y} - \tilde{H}(\mathbf{x}_b, \beta))$$
$$+ \frac{1}{2} (\beta - \beta_b)^T \mathbf{B}_{\beta}^{-1} (\beta - \beta_b)$$

• More apt to distinguish between model bias and observation biases. B (X-X_b)

Auligné et al. (2007): comparaison between VarBC and static bias correction

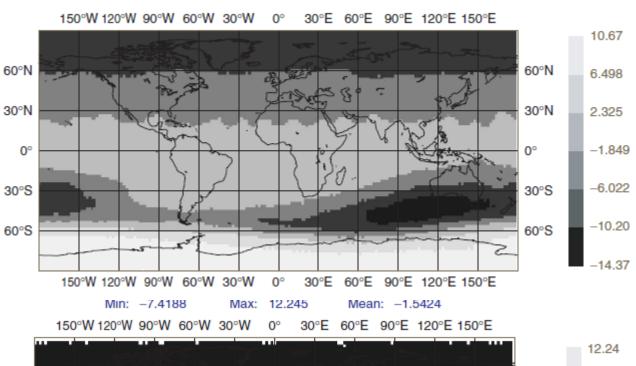


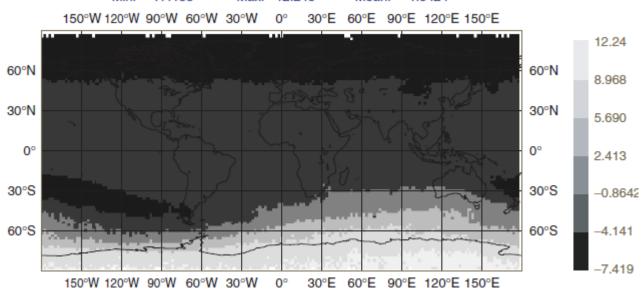
Results for AMSU-a channel 14 (peak at 1hPa) (average over 3 weeks) Auligné et al. (2007)

No assimilation of satellite data

$$\langle \mathbf{y} - H(\mathbf{x}_a) \rangle$$

Offline bias correction

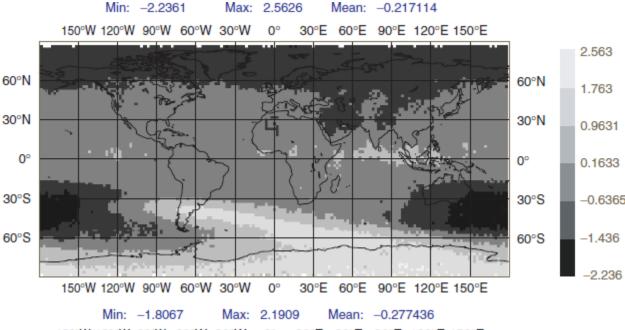


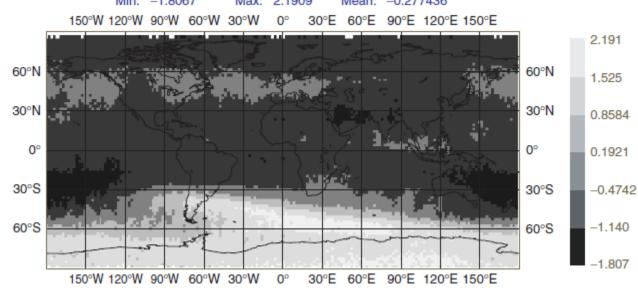


Results for AMSU-a channel 14 (average over 3 weeks) Auligné et al. (2007)

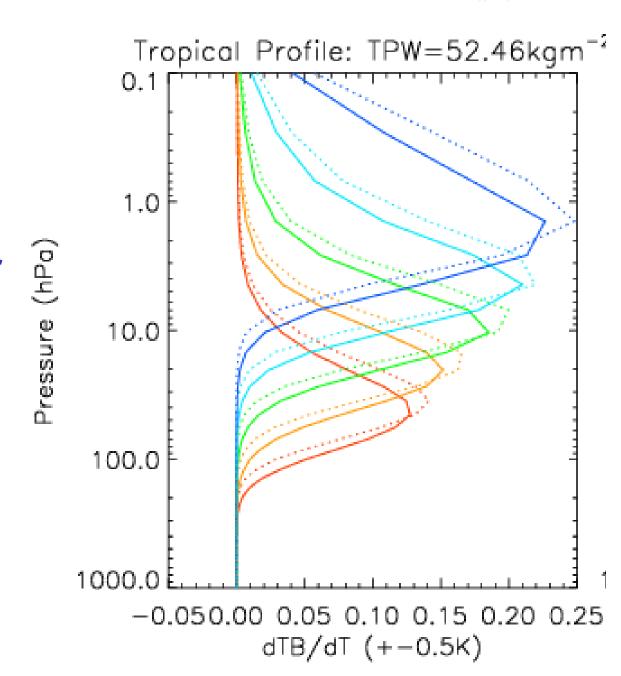
Var-BC bias correction

Var-BC bias correction using a mask





Sensitivity to temperature for different channels of AMSU-a



Conclusions

- Distinguishing between model and observation biases remains delicate
- VarBc automates the bias corrections and has shown some skill to in distinguishing between the two
- Choice of the predictors is being revisited regularly to reflect the nature of the instrument
- Long term drift may result due to the interaction between QC-Var and Var-BC (Auligné and McNally, 2007)
 - Important for reanalyses as biases in the analyses may be wrongly interpreted as a climate drift.