



**Comparison between the conformity coefficient
and previous classification techniques for bare
surface discrimination and application to
compact polarimetry mode**

My-Linh Truong-Loï, ONERA

Pascale Dubois-Fernandez, ONERA

Anthony Freeman, JPL

Eric Pottier, IETR-UMR CNRS 6164, Université Rennes 1



retour sur innovation

Overview

- Context
- The conformity coefficient, μ
 - Definition
 - Published classifications
 - Comparison between the conformity coefficient and previous classifications
 - Over Ramses data
 - Over PALSAR data
- Faraday rotation (FR) estimate
 - Freeman and Bickel&Bates methods, FR estimate from CP data
 - Over Ramses data
 - Over PALSAR data
- Application : soil moisture inversion

Context

- Compact polarimetry ($\pi/2$ mode) at low frequency (P-band)
 - Higher incidence angles
 - Larger swaths
 - Higher power of penetration in the canopy
- $\pi/2$ mode : An unique circular transmission and two independant receptions (linear H&V or circular R&L).
 - Here, we use a right circular transmission and two linear receptions

$$\begin{pmatrix} S_{RH} \\ S_{RV} \end{pmatrix} = \frac{1}{\sqrt{2}} \begin{pmatrix} S_{HH} & S_{HV} \\ S_{VH} & S_{VV} \end{pmatrix} \begin{pmatrix} 1 \\ -j \end{pmatrix}$$

$$\begin{pmatrix} M_{RH} \\ M_{RV} \end{pmatrix} = \frac{1}{\sqrt{2}} \begin{pmatrix} \cos \Omega & \sin \Omega \\ -\sin \Omega & \cos \Omega \end{pmatrix} \begin{pmatrix} S_{HH} & S_{VH} \\ S_{HV} & S_{VV} \end{pmatrix} \begin{pmatrix} \cos \Omega & \sin \Omega \\ -\sin \Omega & \cos \Omega \end{pmatrix} \begin{pmatrix} 1 \\ -j \end{pmatrix}$$

The conformity coefficient - Definition

Definition

$$\mu = \frac{2 \operatorname{Im} \langle M_{RH} M_{RV}^* \rangle}{\langle M_{RH} M_{RH}^* \rangle + \langle M_{RV} M_{RV}^* \rangle}$$

FR independent

$$\mu = \frac{2 \operatorname{Im} \langle S_{RH} S_{RV}^* \rangle}{\langle S_{RH} S_{RH}^* \rangle + \langle S_{RV} S_{RV}^* \rangle} = \frac{2 \operatorname{Im} \langle M_{RH} M_{RV}^* \rangle}{\langle M_{RH} M_{RH}^* \rangle + \langle M_{RV} M_{RV}^* \rangle}$$

Over natural targets with reflection symmetry hypothesis

$$\mu = \frac{2 \operatorname{Im} \langle M_{RH} M_{RV}^* \rangle}{\langle M_{RH} M_{RH}^* \rangle + \langle M_{RV} M_{RV}^* \rangle} \approx \frac{\operatorname{Re}(S_{HH} S_{VV}^*) - |S_{HV}|^2}{(|S_{HH}|^2 + 2|S_{HV}|^2 + |S_{VV}|^2)}$$

The conformity coefficient

$$\mu = \frac{2 \operatorname{Im} \langle M_{RH} M_{RV}^* \rangle}{\langle M_{RH} M_{RH}^* \rangle + \langle M_{RV} M_{RV}^* \rangle} \approx \frac{\operatorname{Re}(S_{HH} S_{VV}^*) - |S_{HV}|^2}{(|S_{HH}|^2 + 2|S_{HV}|^2 + |S_{VV}|^2)}$$

Double-bounce

$$S_{HV} \sim 0$$

S_{HH} , S_{VV} correlated

$$\operatorname{Arg} \langle S_{HH} S_{VV}^* \rangle \approx 180^\circ$$

$$-1 < \mu < t_2$$

Volume

$$S_{HV} \gg 1$$

S_{HH} , S_{VV} less correlated

$$t_2 < \mu < t_1$$

Surface

$$S_{HV} \sim 0$$

S_{HH} , S_{VV} correlated

$$\operatorname{Arg} \langle S_{HH} S_{VV}^* \rangle \approx 0$$

$$t_1 < \mu < 1$$

- This coefficient
 - Is FR independent
 - Can be used with CP data as well as FP data
 - Allows distinguishing 3 different types of scattering

Published classifications

- Freeman-Durden Model¹

$$\langle |S_{hh}|^2 \rangle = f_s |\beta|^2 + f_d |\alpha|^2 + f_v$$

$$\langle |S_{vv}|^2 \rangle = f_s + f_d + f_v$$

$$\langle S_{hh} S_{vv}^* \rangle = f_s \beta + f_d \alpha + f_v / 3$$

$$\langle |S_{hv}|^2 \rangle = f_v / 3$$

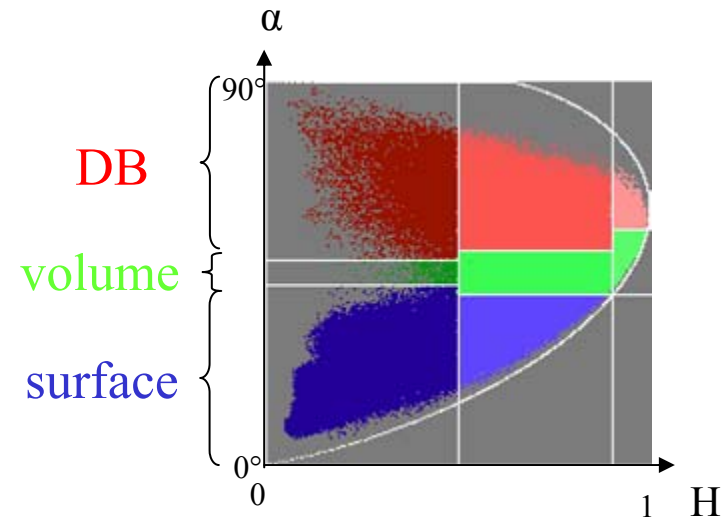
- Cloude and Pottier² classification

$$H = \sum_{i=1}^n -P_i \log_n P_i$$

$$P_i = \frac{\lambda_i}{\sum_{j=1}^n \lambda_j}$$

$$\alpha = \sum_{k=1}^3 P_k \alpha_k$$

$$\alpha_k = \arccos |v_{k1}|$$



¹ "A Three-Component Scattering Model for Polarimetric SAR Data", A. Freeman, *IEEE TGRS*, vol. 36, no. 3, May 1998

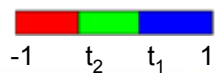
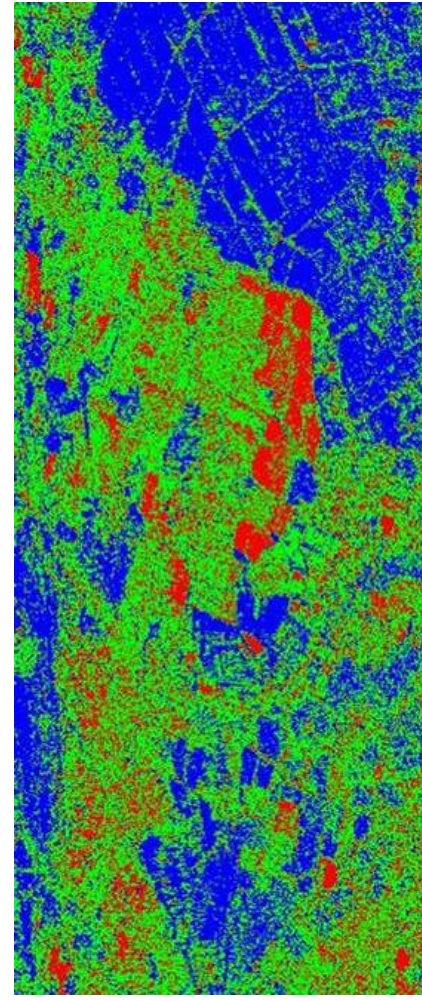
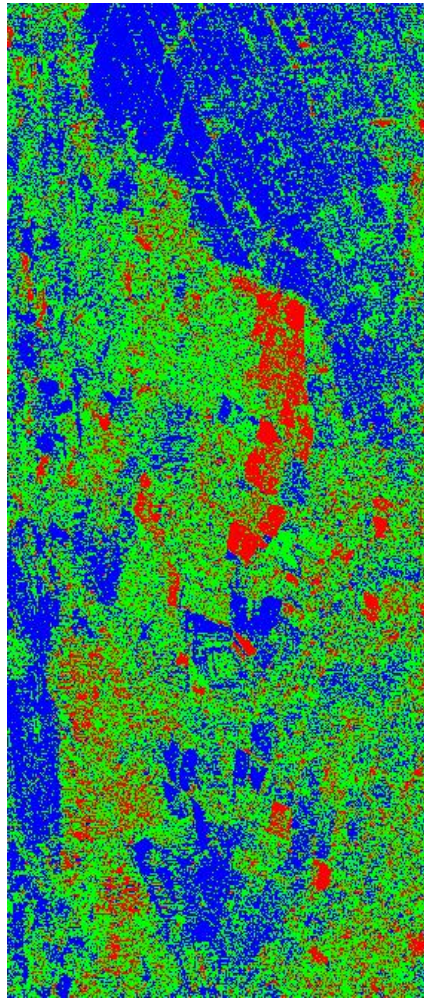
² "An Entropy Based Classification Scheme for Land Applications of Polarimetric SAR", S.R. Cloude and E. Pottier, *IEEE TGRS*, vol. 35, no. 1, pp. 68-78, January 1997.

Conformity coefficient vs Cloude-Pottier (H/α) classification over Ramses data

$\{R;G;B\}=\{Hh;Hv;Vv\}$

Conformity coefficient

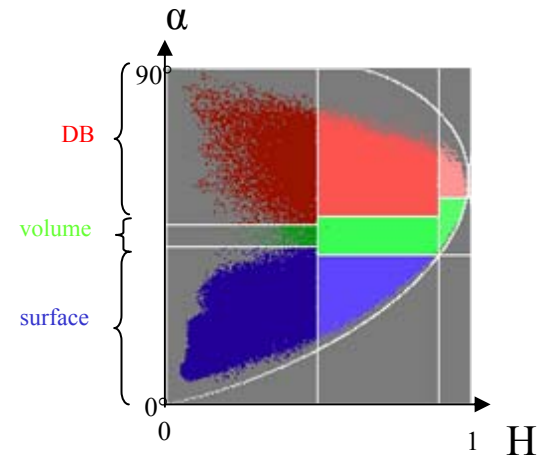
Cloude-Pottier classification



$t_1 = 0.35$
 $t_2 = -0.2$

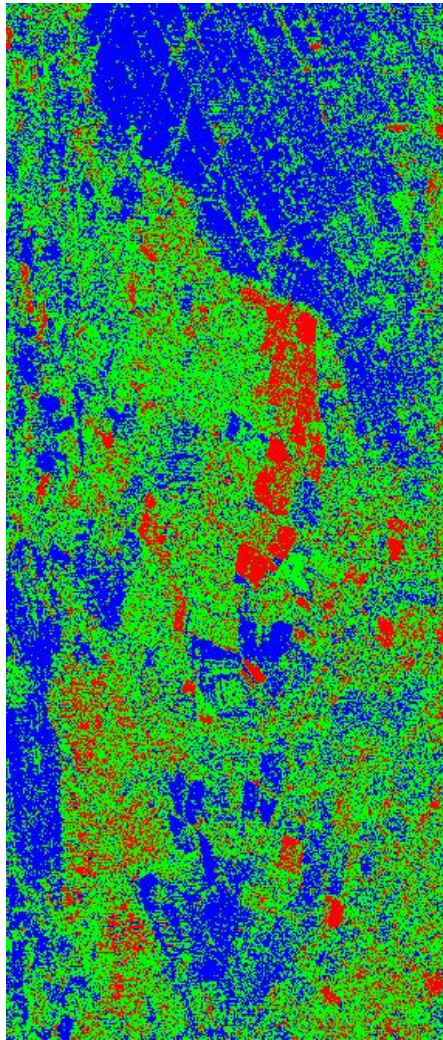
$$\begin{bmatrix} (S1 \& S2)\% & (S1 \& X2)\% \\ (X1 \& S2)\% & (X1 \& X2)\% \end{bmatrix}$$

μ

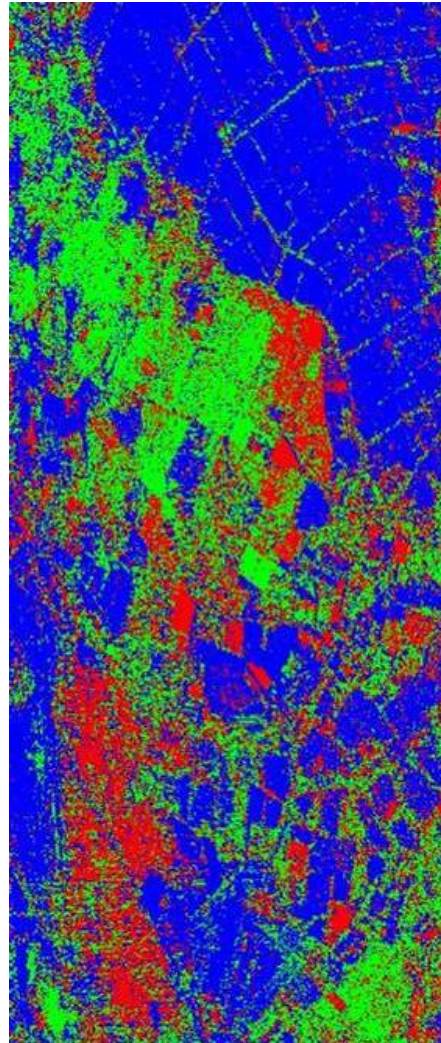
$$H/\alpha \begin{bmatrix} 30.05\% & 5.50\% \\ 6.93\% & 57.52\% \end{bmatrix}$$


Conformity coefficient vs Freeman-Durden classification over Ramses data

Conformity coefficient



Freeman-Durden classification

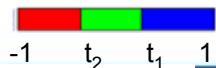


	μ	
FD	35.38%	14.12%
	7.12%	43.40%

$P_s > P_d \ \& \ P_s > P_v \rightarrow$ surface

$P_d > P_s \ \& \ P_d > P_v \rightarrow$ Double-Bounce

$P_v > P_d \ \& \ P_v > P_s \rightarrow$ volume

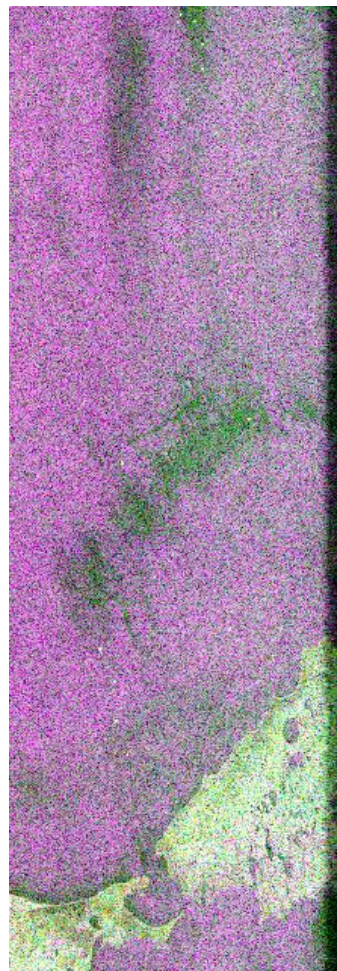


$t_1 = 0.35$

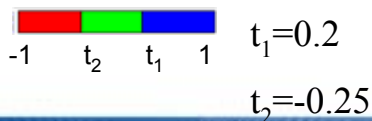
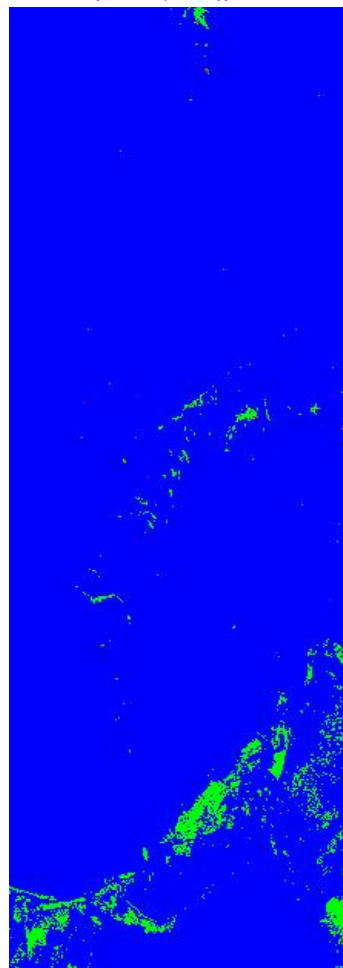
$t_2 = -0.2$

Conformity coefficient vs Freeman-Durden classification over PALSAR data

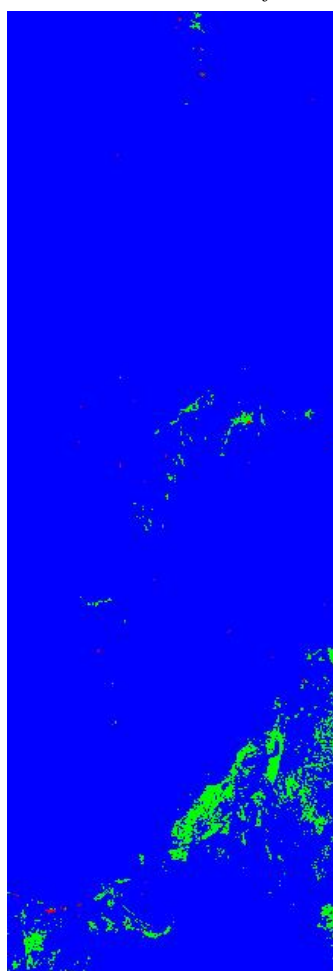
$\{R;G;B\}=\{Hh;Hv;Vv\}$



Conformity coefficient



Freeman-Durden classification



$$\text{FD} \begin{matrix} \mu \\ \left[\begin{array}{cc} 96.66\% & 0.88\% \\ 0.67\% & 1.79\% \end{array} \right] \end{matrix}$$

$P_s > P_d \ \& \ P_s > P_v \rightarrow$ surface

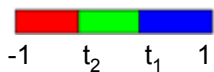
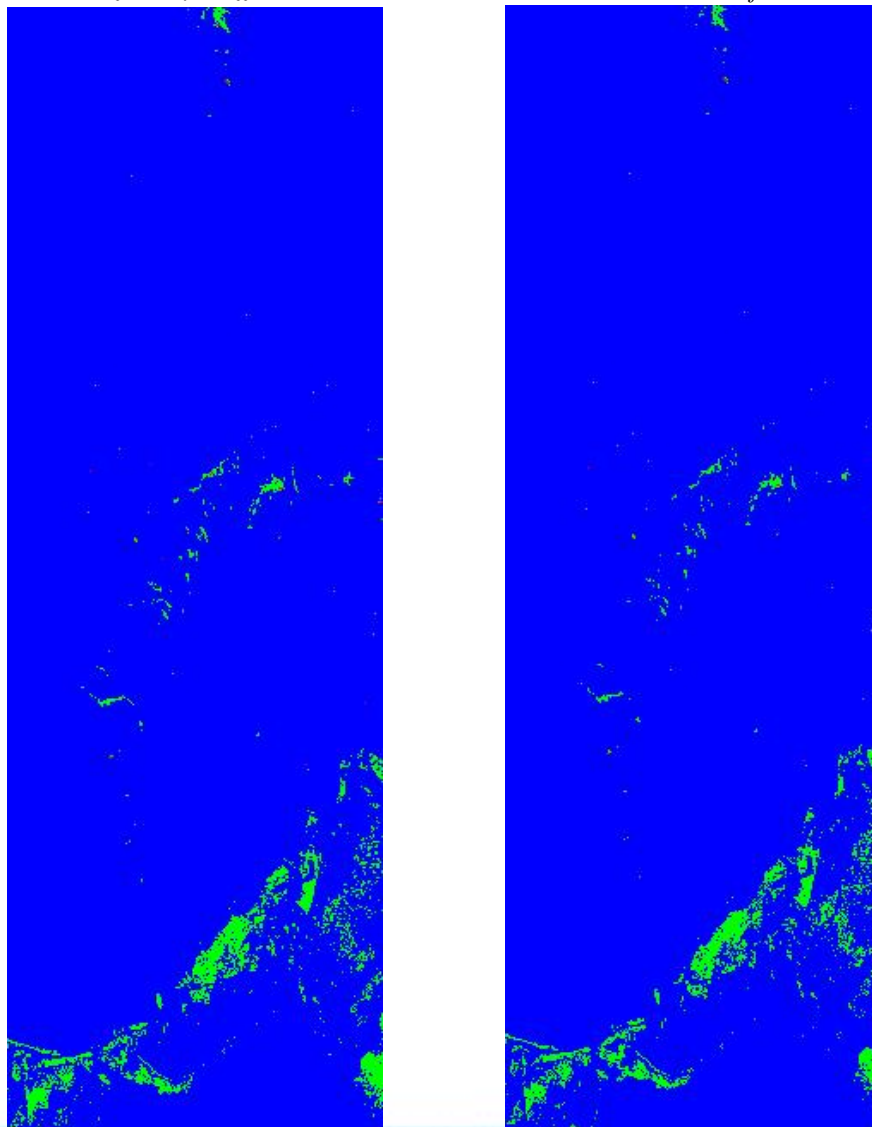
$P_d > P_s \ \& \ P_d > P_v \rightarrow$ Double-Bounce

$P_v > P_d \ \& \ P_v > P_s \rightarrow$ volume

Conformity coefficient vs H/ α classification over PALSAR data

Conformity coefficient

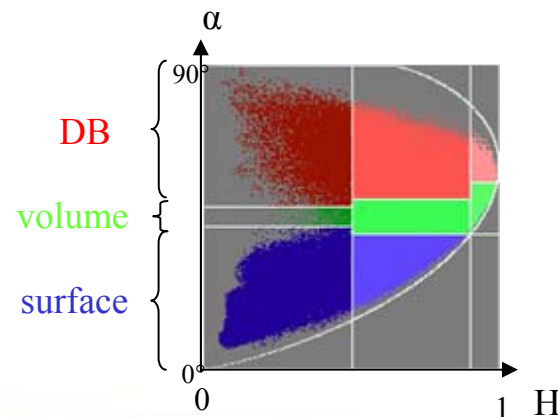
Cloude-Pottier classification



$t_1=0.2$

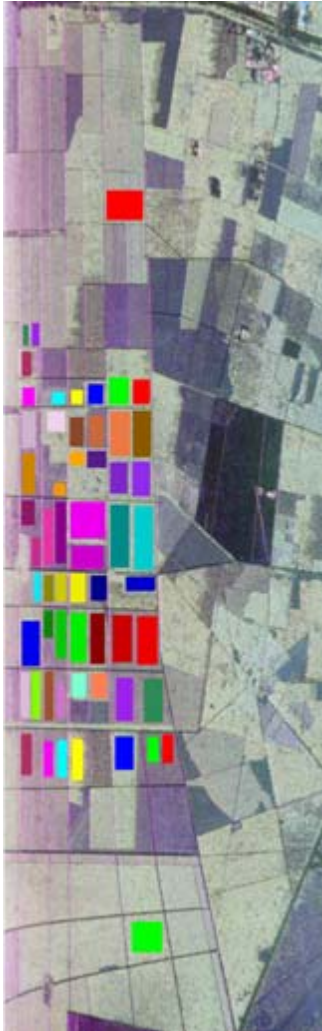
$t_2=-0.25$

$$H/\alpha \begin{matrix} \mu \\ \left[\begin{array}{cc} 96.94\% & 0.41\% \\ 0.39\% & 2.26\% \end{array} \right] \end{matrix}$$

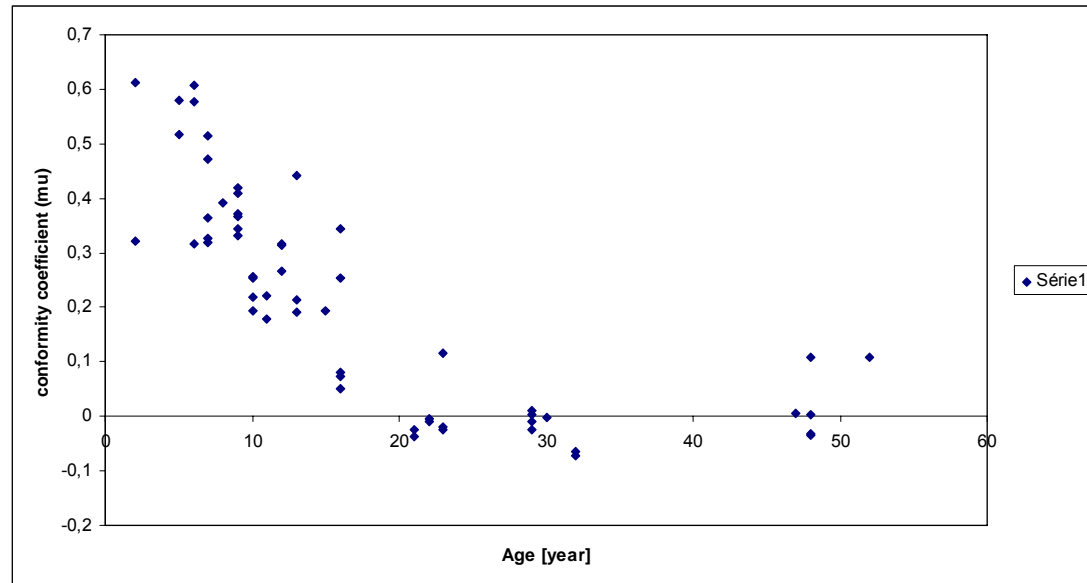


Behavior of μ with parcels ages

RAMSES data, Pyla, 2001, P-band



$\{R;G;B\}=\{Hh;Hv;Vv\}$



- young parcels (<20 years), $0,2 < \mu < 1$
- old parcels, $\mu \sim 0$

Faraday rotation (FR) estimate

- Using FP data

- Freeman method (2004, FP data) $\Omega = \pm \frac{1}{2} \tan^{-1} \sqrt{\frac{4 \langle Z_{hv} Z_{hv}^* \rangle}{\langle M_{hh} M_{hh}^* \rangle + \langle M_{vv} M_{vv}^* \rangle + 2 \operatorname{Re} \langle M_{hh} M_{vv}^* \rangle}} \pm \frac{\pi}{4}$
with $Z_{hv} = 0.5(M_{vh} - M_{hv})$

- Bickel and Bates (FP linear data transformed in circular basis)

$$\Omega = \frac{1}{4} \arg \langle M_{RL} M_{LR}^* \rangle \pm \frac{\pi}{4}$$

- Using CP data

- By correcting the data, then estimating $\operatorname{Arg} \langle \tilde{S}_{Rh} \tilde{S}_{Rv}^* \rangle$ until it reaches the value of $90^\circ \pm n180^\circ$

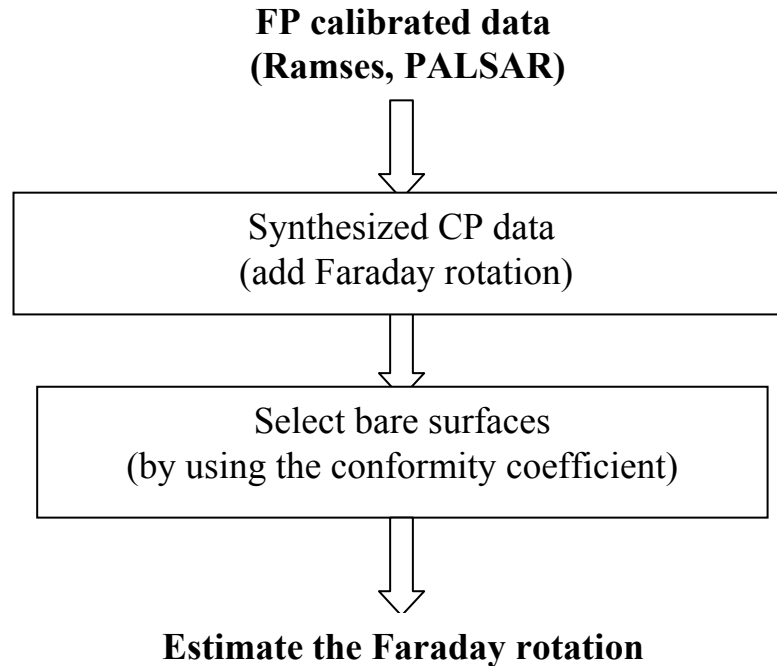
- Linear receptions (H & V) $\Omega = \frac{1}{2} \operatorname{Arc} \tan \left(2 \frac{\operatorname{Re} \langle M_{RH} M_{RV}^* \rangle}{\langle M_{RV} M_{RV}^* \rangle - \langle M_{RH} M_{RH}^* \rangle} \right) \pm \frac{\pi}{4}$

- Circular receptions (L & C) $\Omega = \frac{1}{2} \operatorname{Arg} \langle M_{RR} M_{RL}^* \rangle \pm n \frac{\pi}{2}$

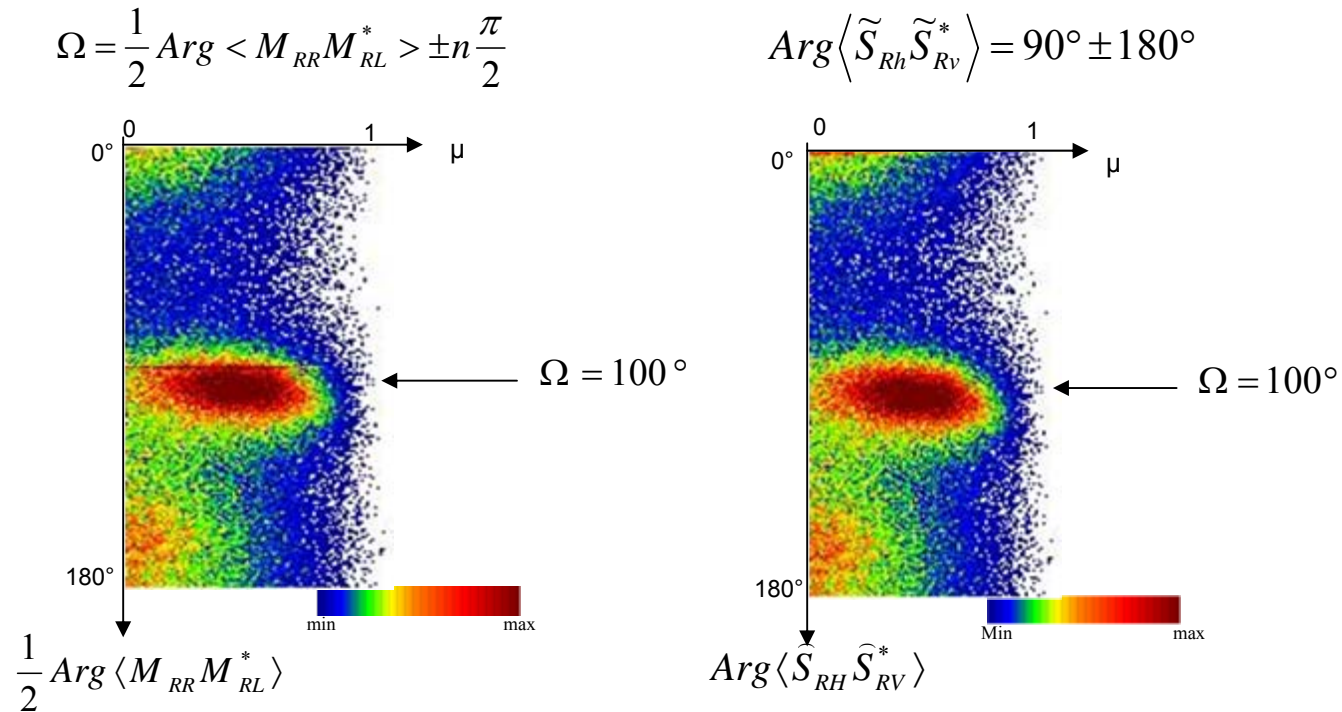
With assumptions: $\langle S_{HH} S_{HV}^* \rangle \approx \langle S_{VV} S_{HV}^* \rangle \approx 0$ and $\operatorname{Arg} \langle S_{HH} S_{VV}^* \rangle \approx 0$

Process

- Flow diagram of the process



FR estimate vs conformity coefficient



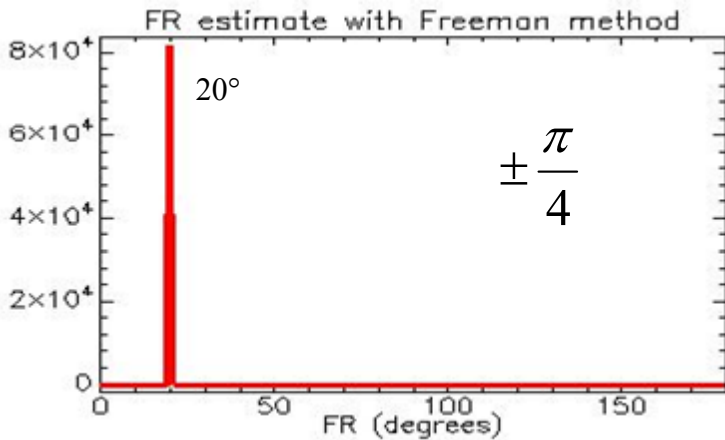
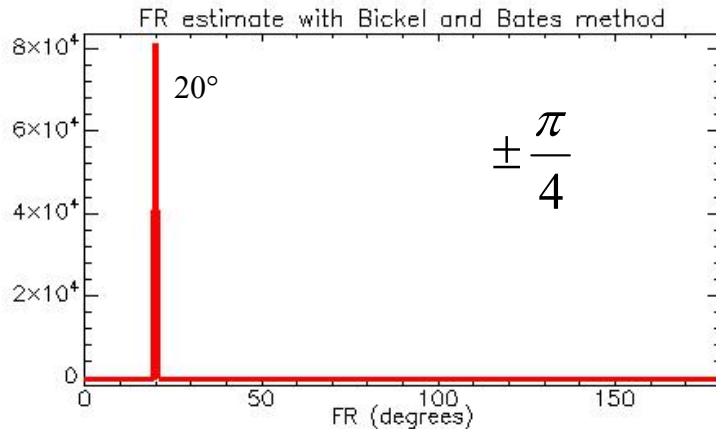
μ identifies the bare surfaces in CP

is FR independent

provides a robust estimate of FR

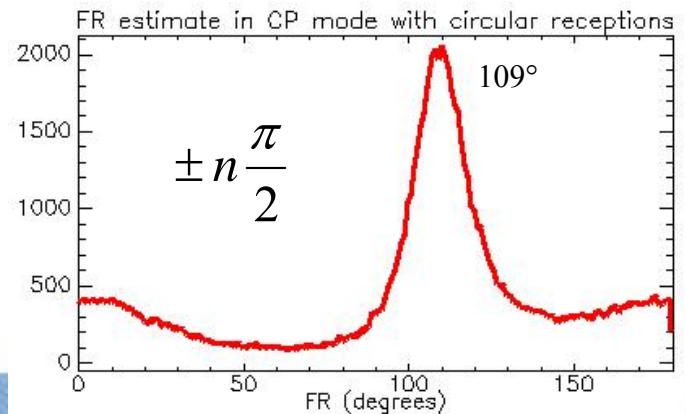
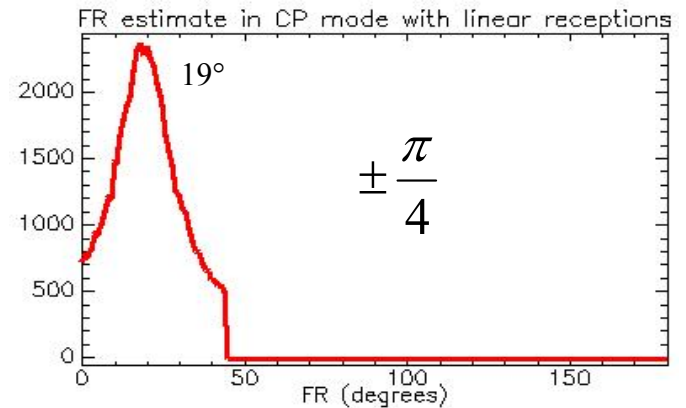
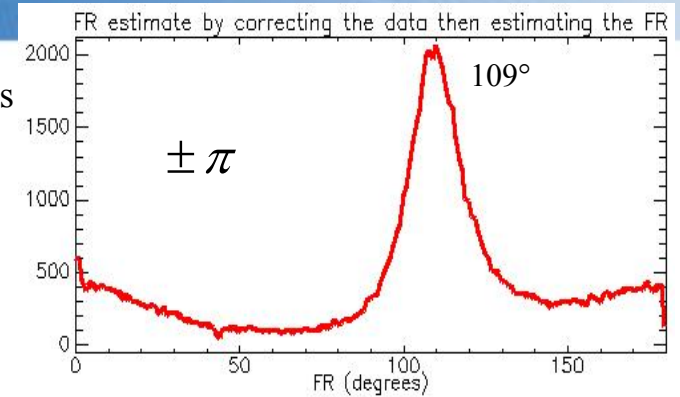
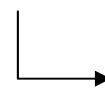
FR estimate over Ramses data (110° FR has been introduced)

Over the full scene



Over bare surfaces

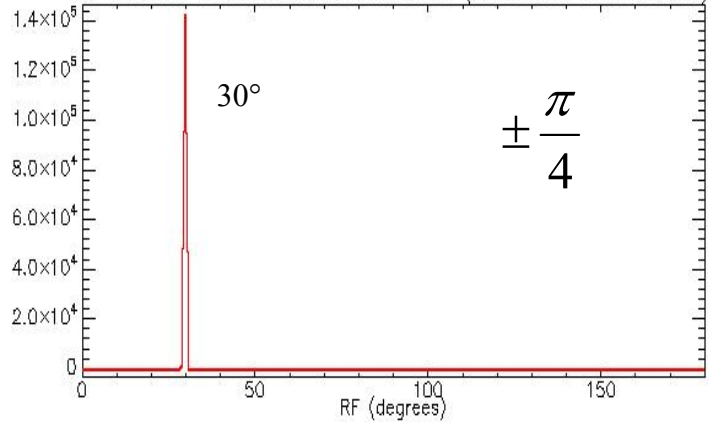
$\mu > 0.35$



FR estimate over PALSAR data (30° FR has been introduced)

Over the full scene

RF estimate with Bickel & Bates method (FP data in circular basis)

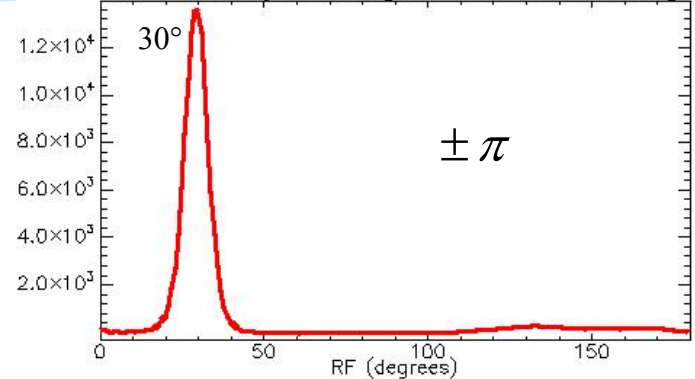


Over bare surfaces

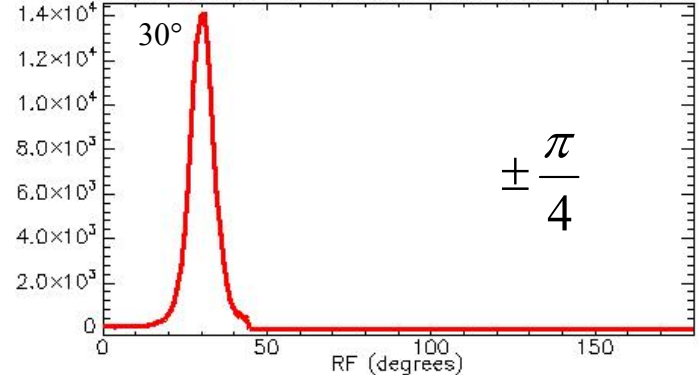
$\mu > 0.2$



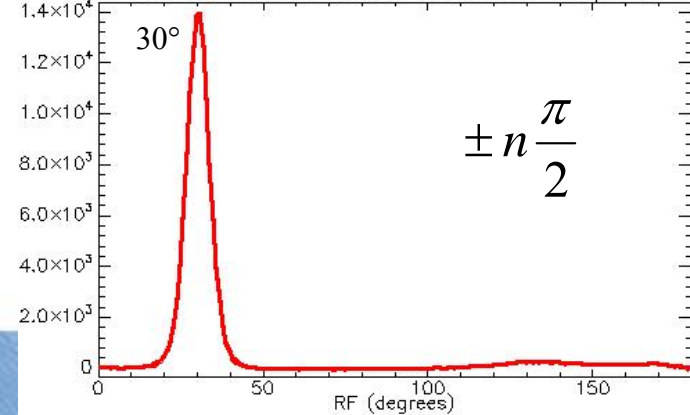
RF estimate by correcting the data then estimating



RF estimate in CP mode with linear reception

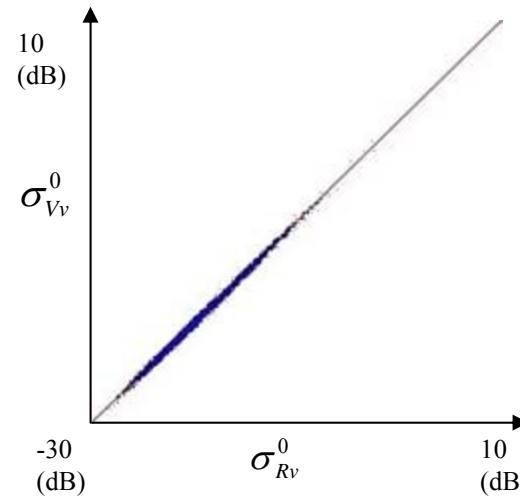
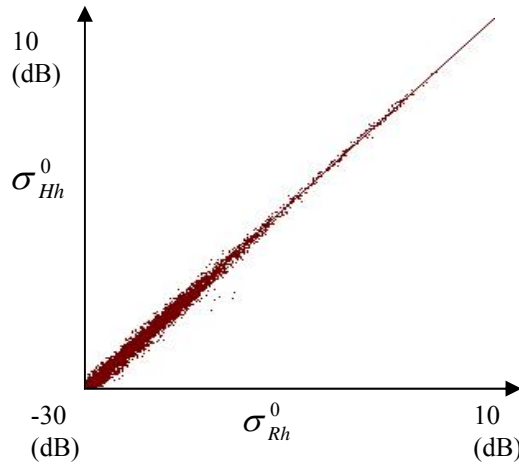


RF estimate in CP mode with circular reception

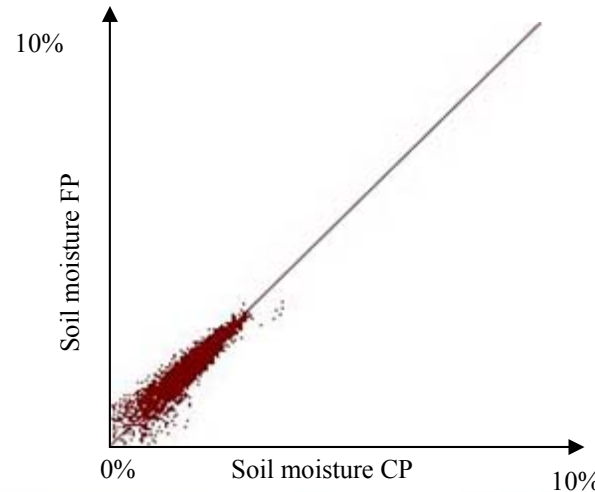


CP vs FP signatures and applying the Dubois et al. (1995*) algorithm to Ramses CP data

- Over bare surfaces $\begin{pmatrix} \tilde{S}_{RH} \\ \tilde{S}_{RV} \end{pmatrix} \cong \begin{pmatrix} S_{HH} - jS_{HV} \\ S_{VH} - jS_{VV} \end{pmatrix}$



WS : 7x7, RMS deviation less than 1dB



WS : 7x7, RMS deviation less than 2%

Summary

- Compared conformity coefficient, μ , which is FR-invariant and can separate scattering types with
 - Freeman-Durden classification
 - Cloude-Pottier classification
 - Assess μ over Ramses and PALSAR data
- Used μ to screen for surface scatterers → estimate of FR
 - Assess FR estimates using CP data with FP methods (Freeman and Bickel&Bates)
 - Compute FR over Ramses and PALSAR data
- For the same bare surfaces, shown that soil moisture can be estimated from CP data with an equivalent accuracy than with FP data.