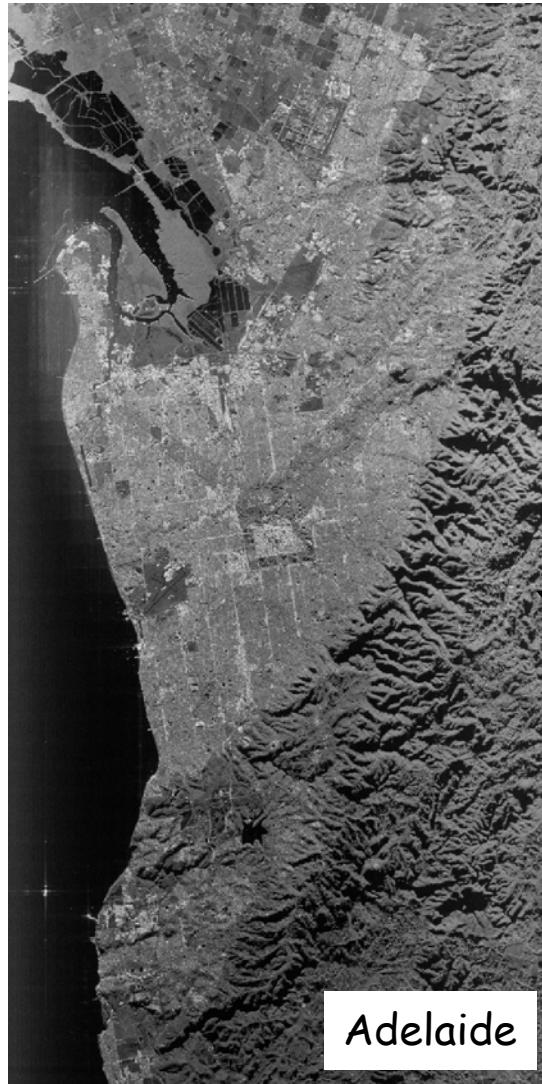


Polarimetric SAR Interferometry: Status and Future Trends



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Summary

"POLInSAR involves the combination of multiple interferograms in different polarisation channels for the purposes of studying vertical structure and problems involving combined surface and volume scattering"

Primary Application Area

- Forestry (mainly L and some P band studies)
 - Tree Height/Biomass
- Future Research Trends (P,L,C,X....)
 - Urban applications (PPS)
 - Concealed Target Detection
 - Snow/Ice Studies (thickness/SWE etc)
 - Multi-baseline techniques:
 - a) Vertical Structure Mapping
 - b) Temporal Decorrelation
 - Agriculture
 - a) Plant Water Content
 - b) Sub-Canopy Moisture

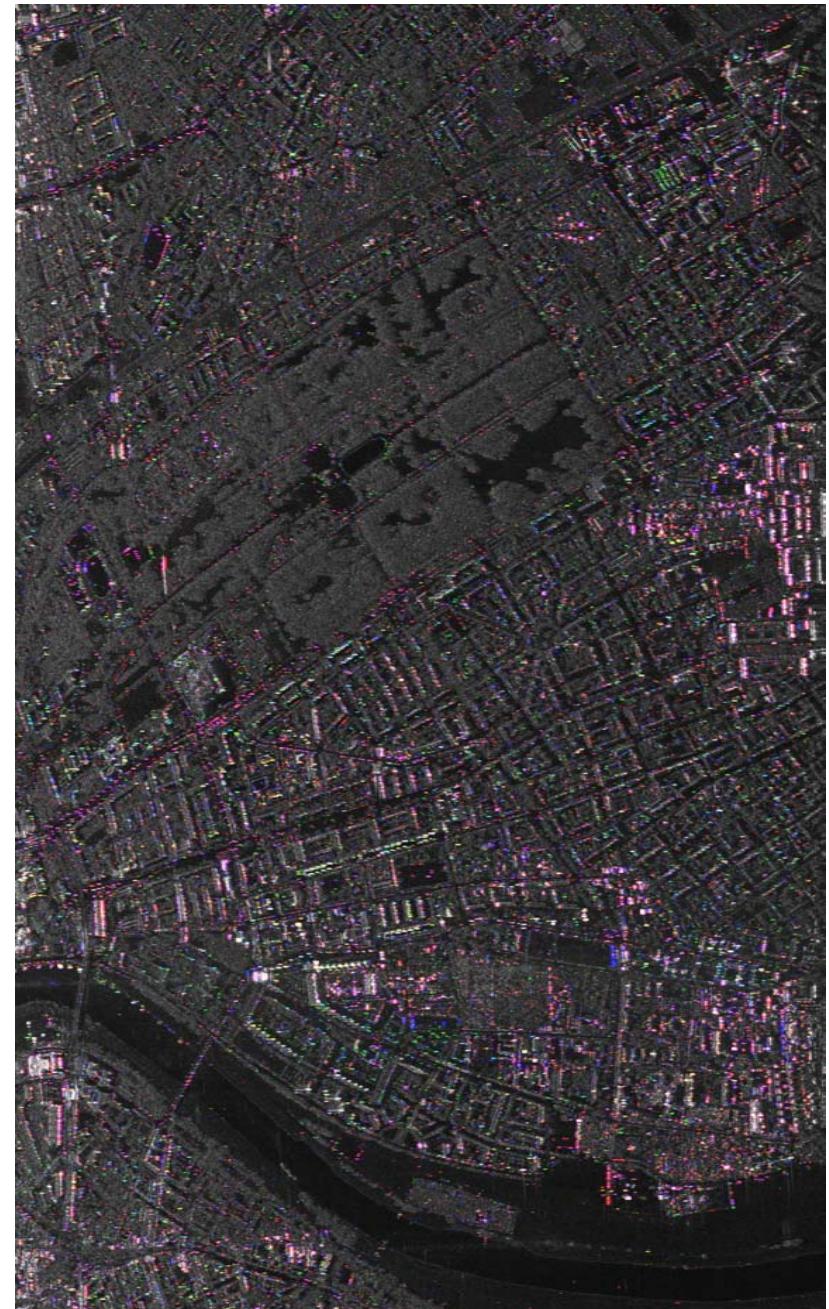


Polarisation Dependence Of Candidate Permanent Scatterers

E-SAR L band Data,
City of Dresden

...but vegetated areas show poor polarimetric phase stability due to depolarisation (high entropy)..

...one possible solution...
combine polarimetry with interferometry



Polarimetric Radar Interferometry



$$T = T_V + T_S$$

T_V = Polarimetric Coherency matrix (Volume)

T_S = Polarimetric Coherency matrix (Surface)

German Aerospace Center

Institute

..provides Entropy Control...via (user) choice of baseline
...measure phase ϕ with high coherence, even for vegetation

Coherent Vegetation Mapping

Method 1: DEM Differencing Algorithms

Stage 1 : Surface Topography Estimation

$$\hat{\phi} = \arg(\tilde{\gamma}_{rs})$$

- Coherence Optimisation
- Coherence Region Analysis
- ESPRIT Superresolution
- Sub-space coherence analysis

Stage 2 : Height Estimation

pq - polarisation 1

rs - polarisation 2

$$h_v = \frac{\arg(\gamma_{pq}) - \hat{\phi}}{k_z}, \quad k_z = \frac{4\pi\Delta\theta}{\lambda \sin\theta} \approx \frac{4\pi B_n}{\lambda R \sin\theta}$$

Stage 3 : Volume/Surface scattering separation

$$s(\underline{w}) = \underline{w}^{*T} T_V \underline{w} + \underline{w}^{*T} T_s \underline{w}$$

Coherent Vegetation Mapping

Method 2 : 2-layer coherence model inversion

Stage 1 : Surface Topography Estimation

$$\hat{\phi} = \arg(\tilde{\gamma}_{pq} - \tilde{\gamma}_{rs}(1 - L_{pq})) \quad 0 \leq L_{pq} \leq 1$$

$$AL_{pq}^2 + BL_{pq} + C = 0 \Rightarrow L_{pq} = \frac{-B - \sqrt{B^2 - 4AC}}{2A}$$

$$A = |\tilde{\gamma}_{rs}|^2 - 1 \quad B = 2 \operatorname{Re}((\tilde{\gamma}_{pq} - \tilde{\gamma}_{rs})\tilde{\gamma}_{rs}^*) \quad C = |\tilde{\gamma}_{pq} - \tilde{\gamma}_{rs}|^2$$

Stage 2 : Height Estimation...with regularisation parameter λ

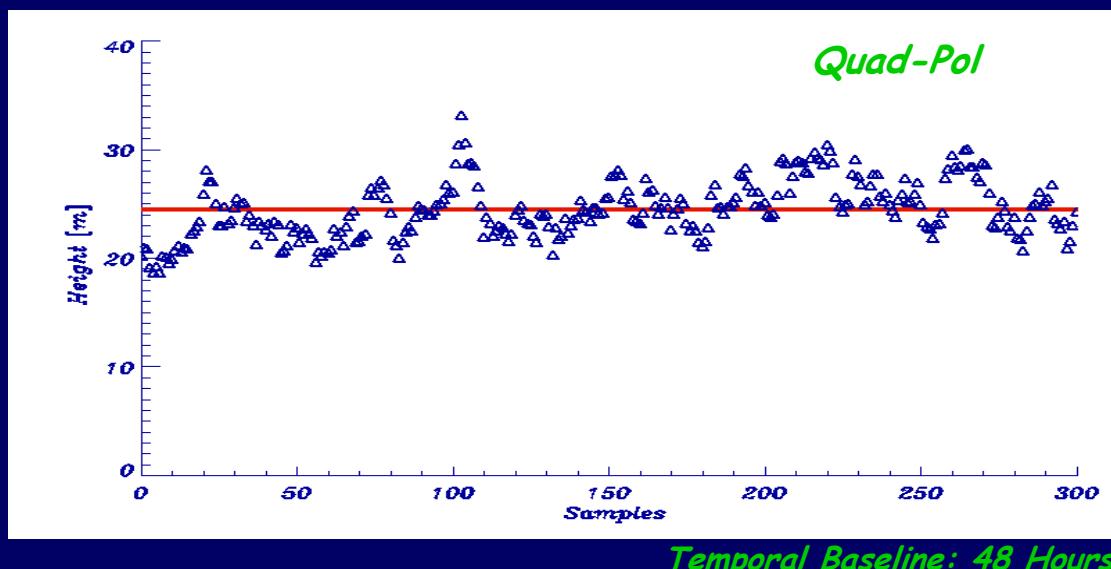
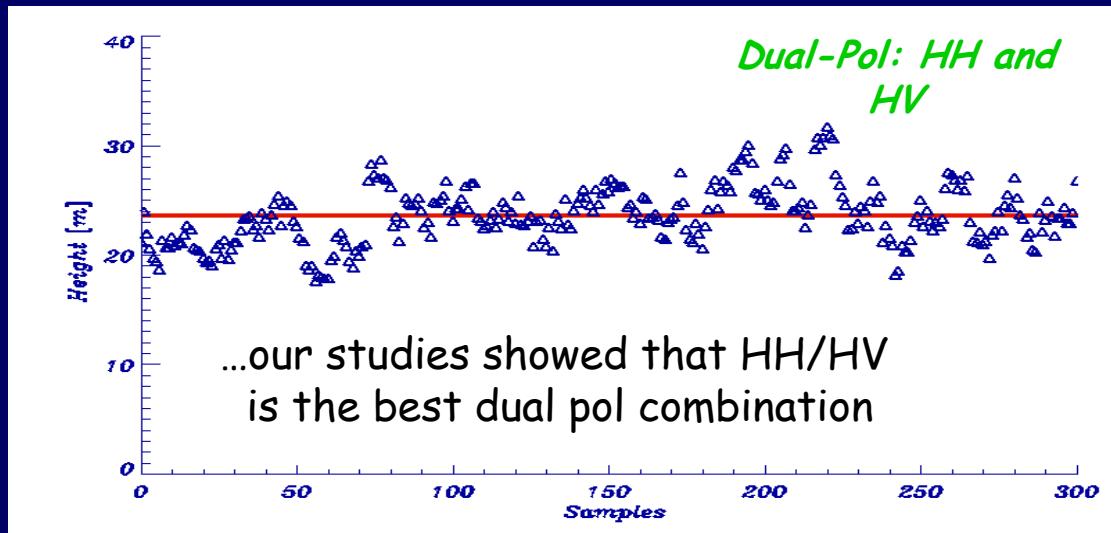
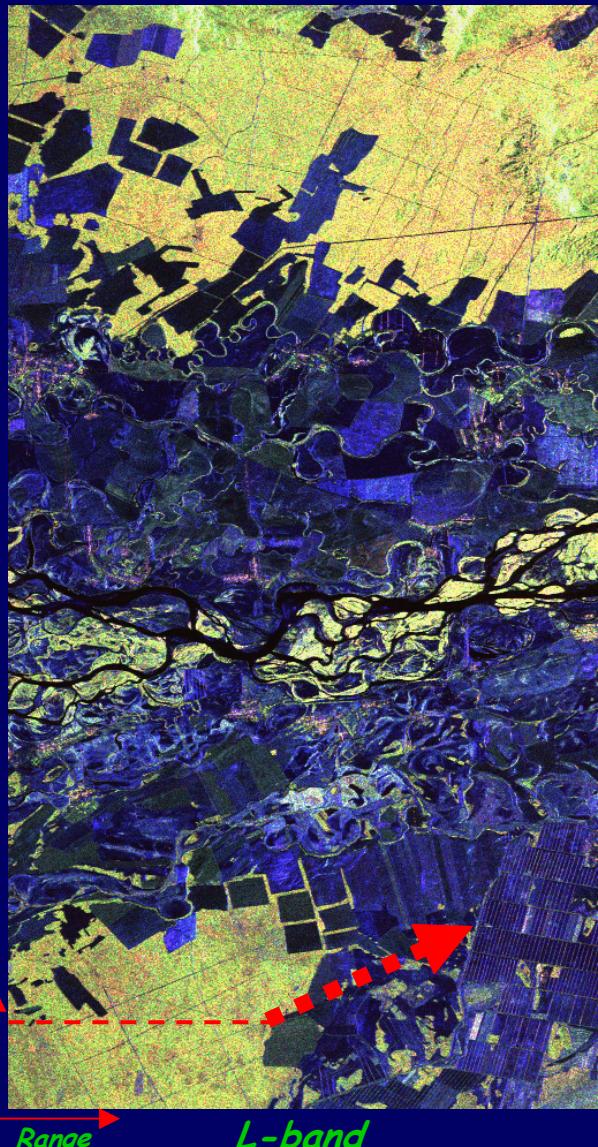
$$\min_{h_v, \sigma} L_1(\lambda) = \left\| \tilde{\gamma}_{rs} + \lambda \left(e^{i\hat{\phi}_2} - \tilde{\gamma}_{rs} \right) - e^{i\hat{\phi}} \frac{p}{p_1} \frac{e^{p_1 h_v} - 1}{e^{ph_v} - 1} \right\| \quad \text{where} \begin{cases} p = \frac{2\sigma}{\cos \theta} \\ p_1 = p + ik_z \\ k_z = \frac{4\pi \Delta \theta}{\lambda \sin \theta} \approx \frac{4\pi B_n}{\lambda R \sin \theta} \\ \hat{\phi}_2 = \arg(\tilde{\gamma}_{rs} - \tilde{\gamma}_{pq}(1 - L_{rs})) \end{cases}$$

Stage 3 : Volume/Surface scattering separation

$$s(\underline{w}) = \underline{w}^{*T} T_V \underline{w} + \underline{w}^{*T} T_s \underline{w}, \quad 0 \leq L(\underline{w}) = \frac{\hat{p} \frac{e^{\hat{p}_1 \hat{h}_v} - 1}{e^{\hat{p} \hat{h}_v} - 1} - e^{-i\hat{\phi}} \hat{\gamma}(\underline{w})}{\hat{p} \frac{e^{\hat{p}_1 \hat{h}_v} - 1}{e^{\hat{p} \hat{h}_v} - 1} - 1} \leq 1 \Rightarrow \begin{cases} \underline{w}^{*T} T_s \underline{w} = e^{\frac{2\sigma h_v}{\cos \theta_0}} L(\underline{w}) s(\underline{w}) \\ \underline{w}^{*T} T_V \underline{w} = s(\underline{w}) - \underline{w}^{*T} T_s \underline{w} \end{cases}$$

Forest Height Estimation: Quad-Pol vs.Dual-Pol

SIR-C / Test Site: Kudara, Russia

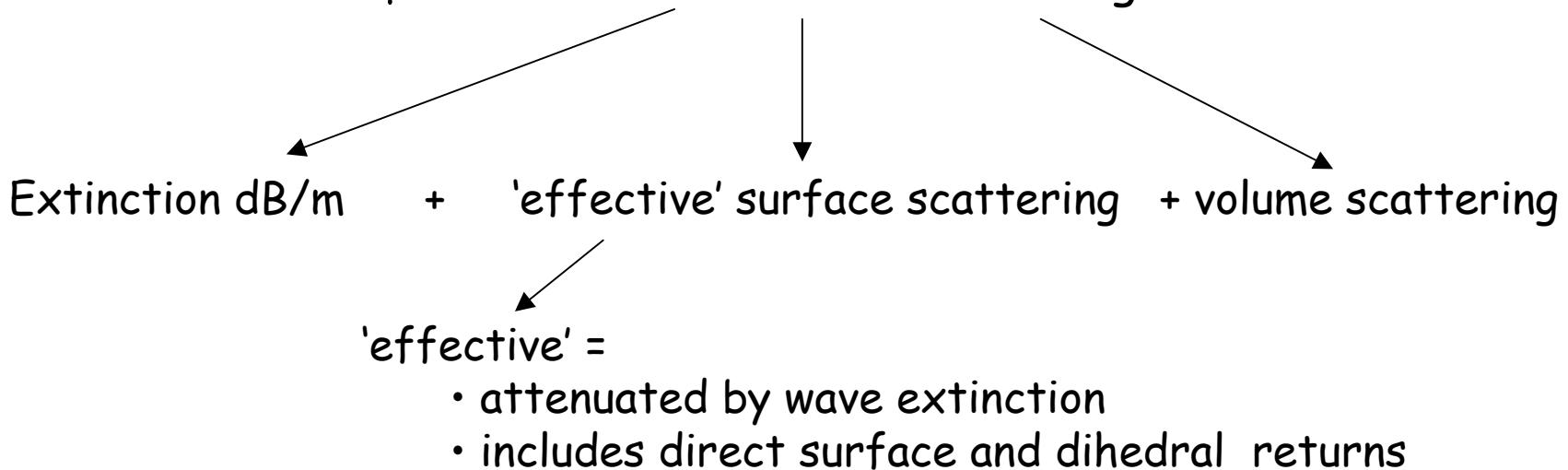


POInSAR Coherence : The 'rvog' model

$$\gamma(\underline{w}) = e^{i\phi} \frac{\frac{p}{p_1} \frac{e^{p_1 h_v} - 1}{e^{p_1 h_v} - 1} + \mu(\underline{w})}{1 + \mu(\underline{w})}$$

where $\begin{cases} p = \frac{2\sigma}{\cos\theta} \\ p_1 = p + ik_{z1} \end{cases}$

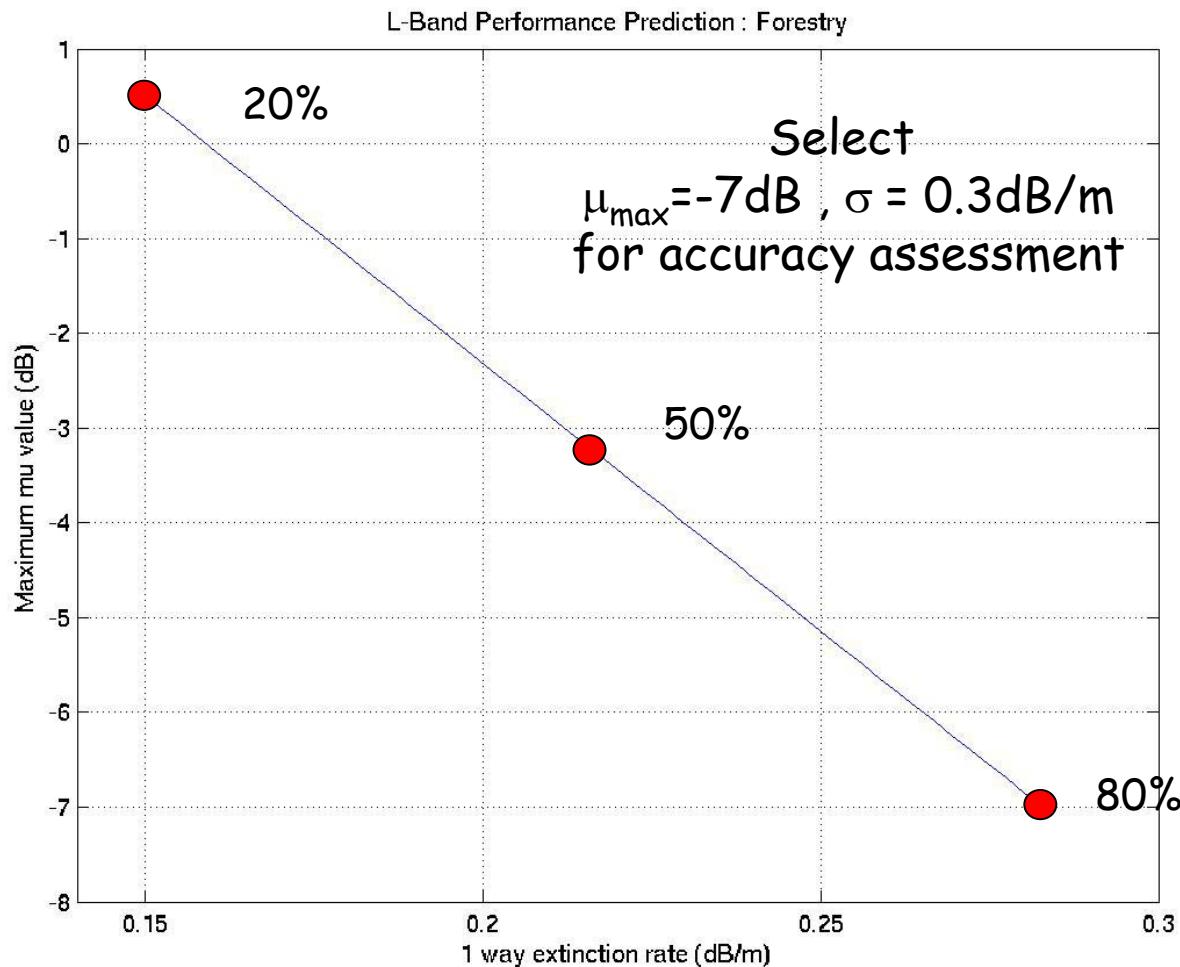
μ = surface-to-volume scattering ratio



2 issues of importance:

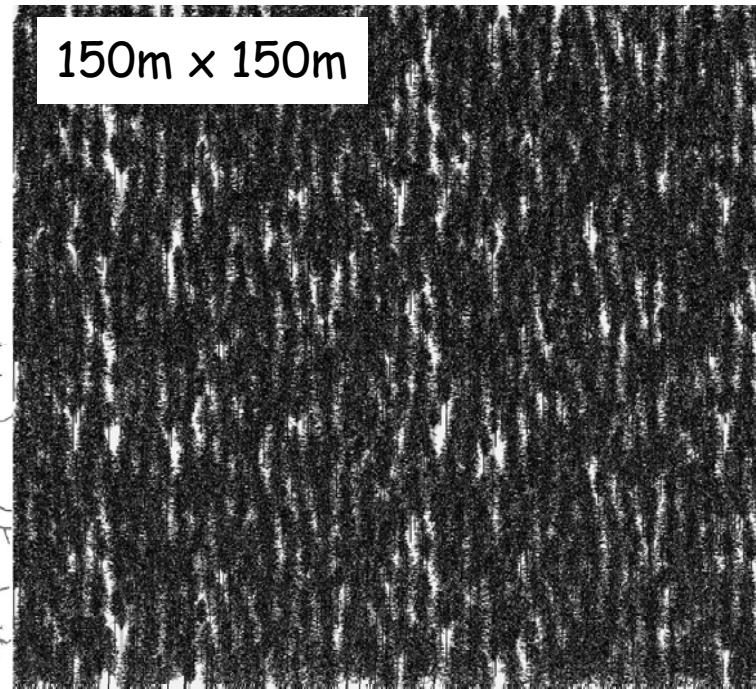
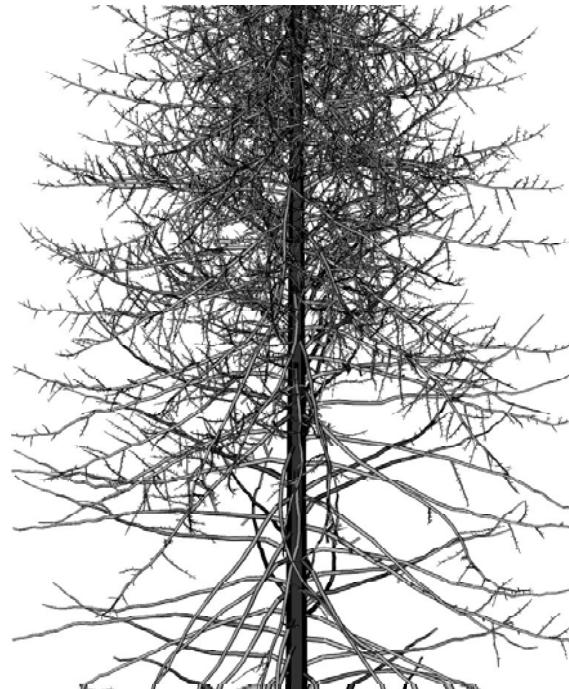
1. Must assume that for at least one polarisation $\mu = 0$ but...
2. If $\mu(\underline{w}) = 0$ inversion collapses ... $\gamma_{pq} = \gamma_{rs}$ for all polarisations
...so what is a typical range of μ_{\min} to μ_{\max} ?

Summary : Parameters used for L-band Forestry Product Accuracy assessment



This allows us to estimate μ_{\max} ...but what about μ_{\min} ?

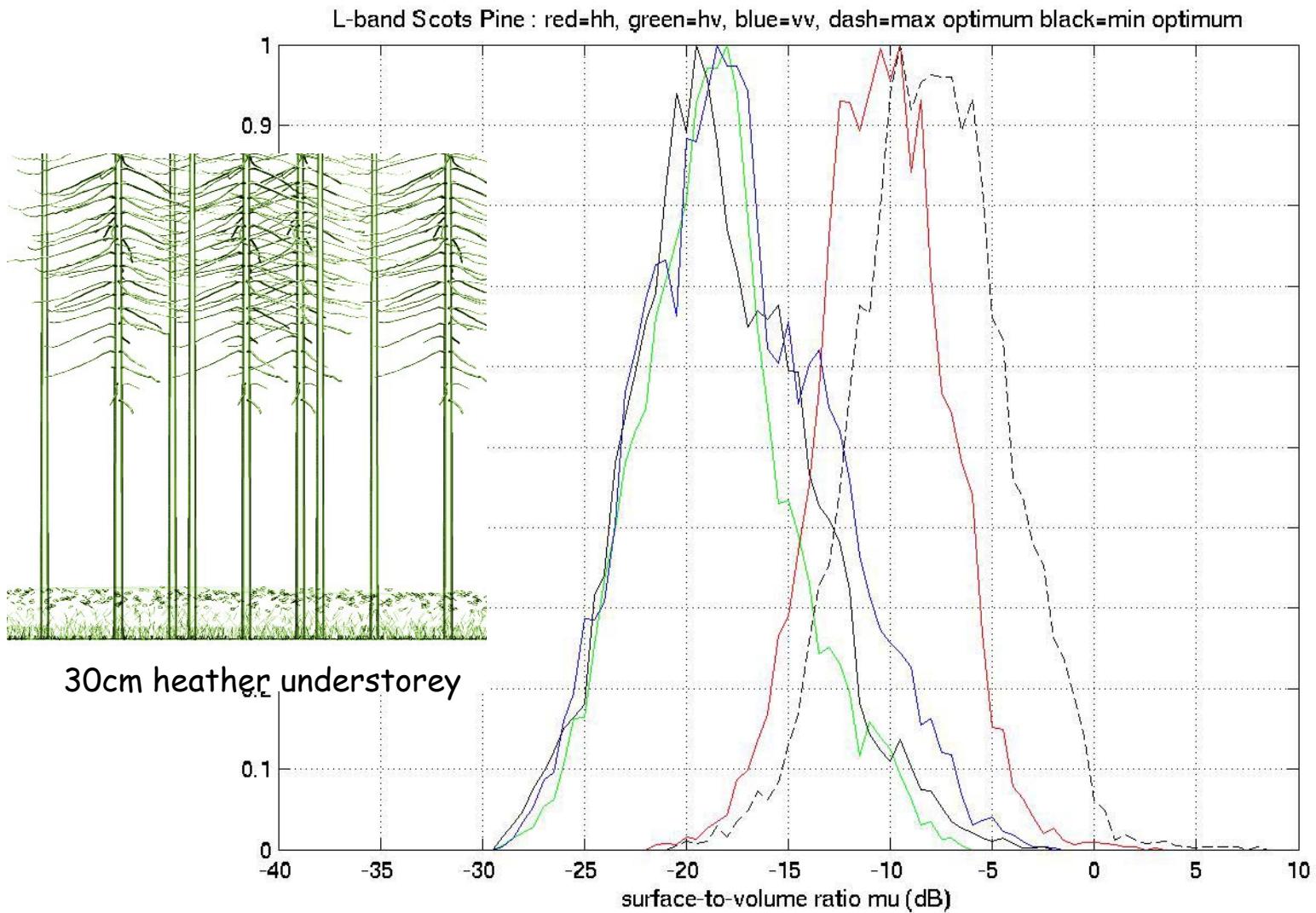
Architectural tree model courtesy of University of Joensuu, Finland
Simulations Carried out by Dr Mark Williams, DSTO



Stand density = 0.055 stems/m²
Mean height = 18m...std = 0.6m

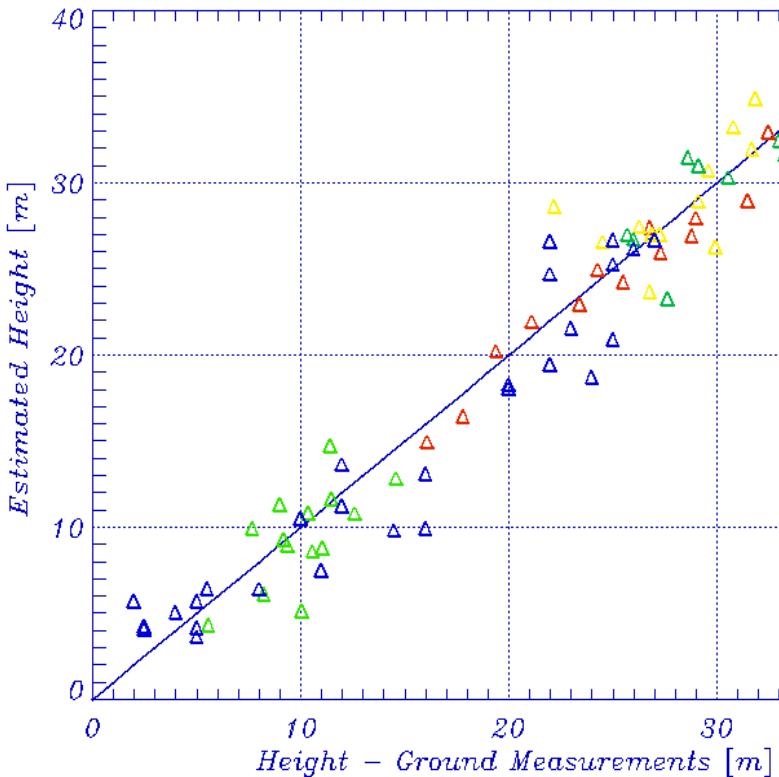
L-band $\theta=45$ degrees...can be used to calculate extinction and μ values ..
...Mean extinction = 0.28 dB/m.. μ depends on polarisation as..

4-layer Understorey Models



Can use the dynamic range of μ with polarisation to assess system performance (the phase tube)

Summary: POrInSAR Height Estimation



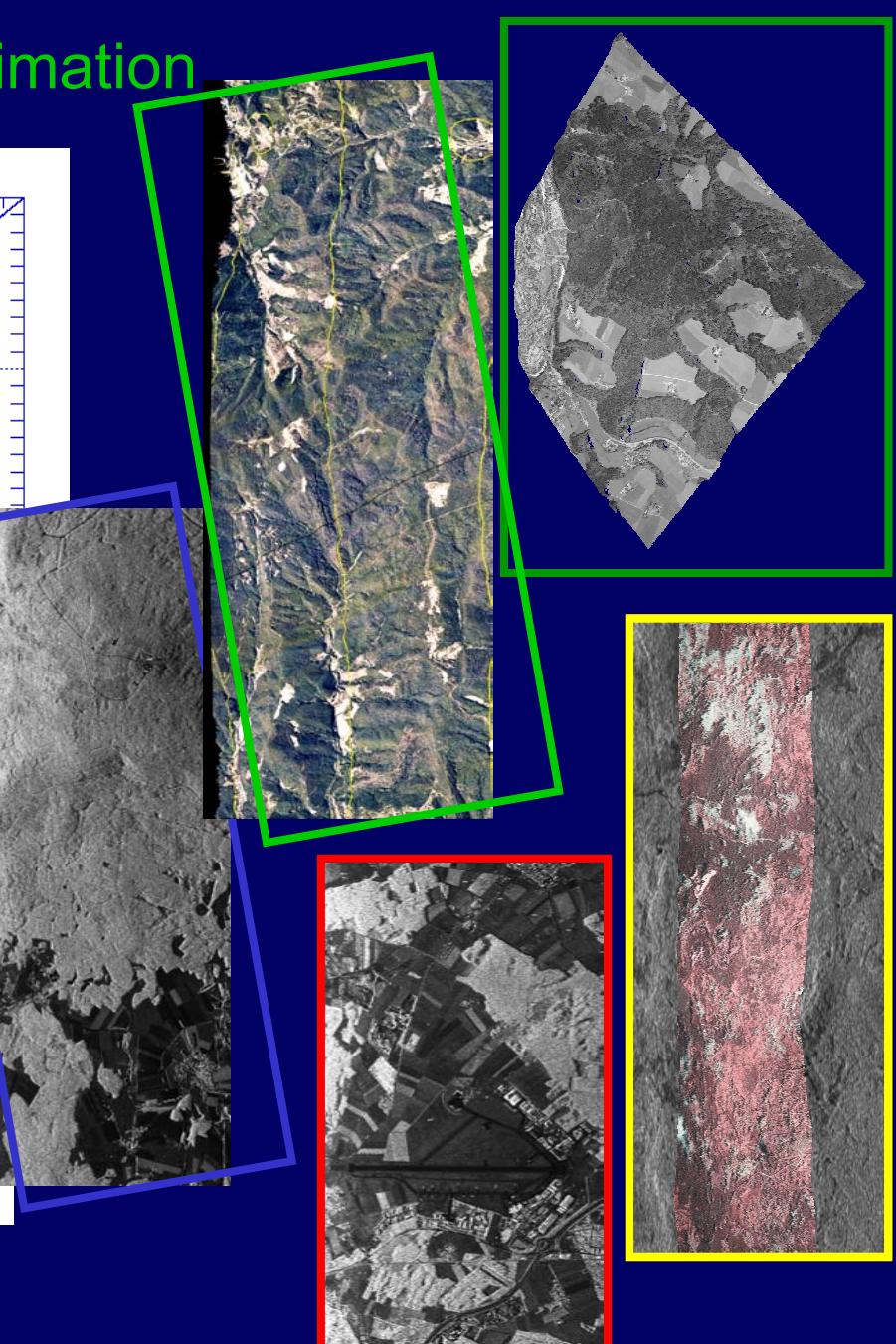
Fichtelgebirge / Germany

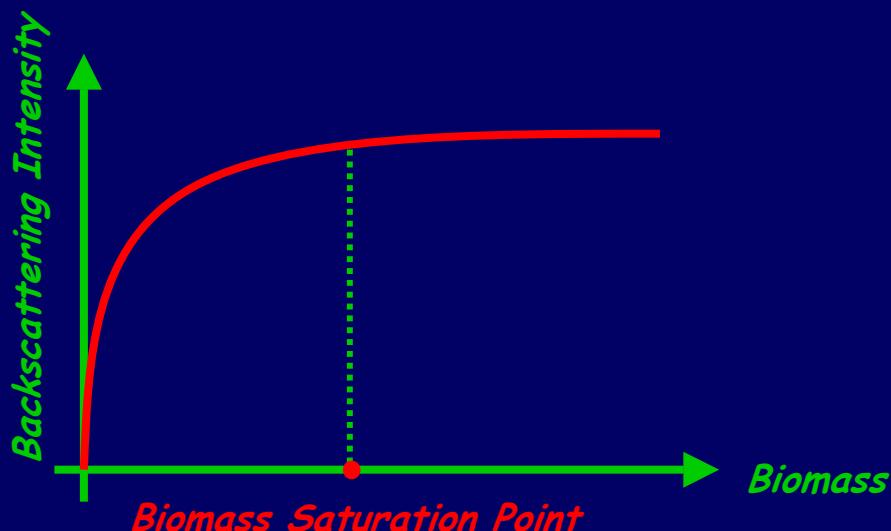
Corridor / Spain

Bayrischer Wald / Germany

Traunstein / Germany

Oberpfaffenhofen / Germany





	<i>Biomass Saturation Limit</i> [T/ha]	<i>% of Earths Vegetated Area</i>	<i>% of Total Biomass Stock</i>
	[Kg/(m ²)]		

Backscatter Saturation:

<i>C-band</i>	20*	2	25%	4%
<i>L-band</i>	40*- 60	4 - 6	35%	8%
<i>P-band</i>	100*-150	10 -15	60-65%	20-25%

* M. L. Imhoff, "Radar Backscatter and Biomass Saturation: Ramifications for Global Biomass Inventory", IEEE TGARS, Vol. 33, No. 2, Mar.

Self-similar 3 parameter model for forests in equilibrium with resources

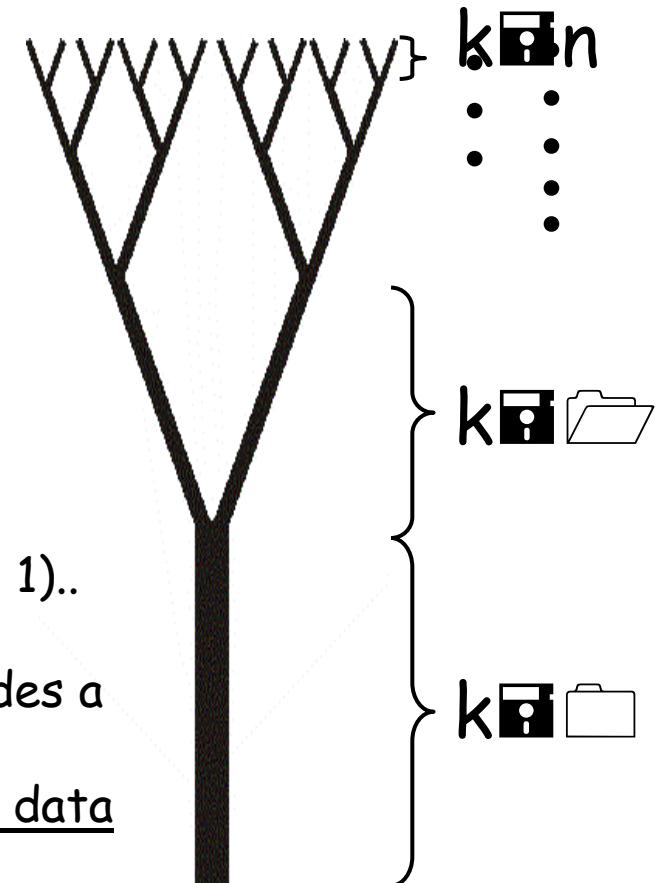
Example Biomass-Height Relationship :

$$\left. \begin{array}{l} M \propto h^4 \\ N \propto M^{-\frac{3}{4}} \end{array} \right\} \Rightarrow \bar{M} = M * N \propto \bar{h}$$

More detailed analysis shows that $\bar{M} \propto h^\alpha$

Where α depends on latitude (for tropical forest $\alpha = 1$)..

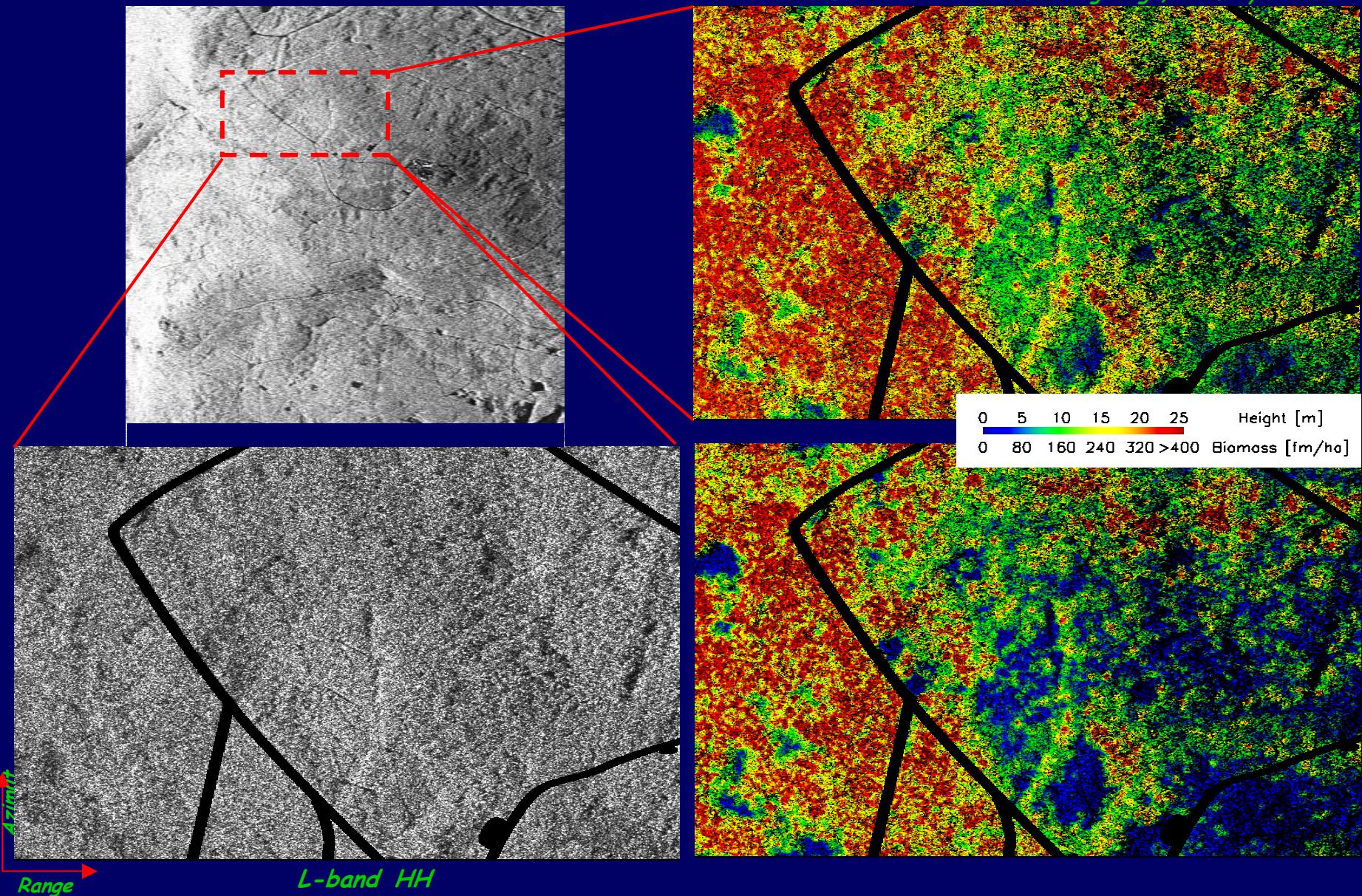
These results indicate that height measurement provides a non-saturating robust estimate of biomass..
...but need to reliably estimate tree height from radar data



G.B West, J.H.Brown,B.J.Enquist, "A General Model For the Structure and Allometry of Plant Vascular Systems", NATURE, Vol. 400, 12 August 1999

Forest Height & Biomass Maps : Airborne Sensors

ESAR / Test Site: Fichtelgebirge, Germany





THE UNIVERSITY
OF ADELAIDE
AUSTRALIA

AIRBORNE SAR CAMPAIGN OVER TROPICAL FOREST



INDEX 2

INDONESIA RADAR EXPERIMENT

Mawas-Gunung Meratus-Sungai Wain-Balikpapan Bay Mangrove-Samboja Lestari

NOVEMBER, 2004







BOS SarVision

AIRBORNE SAR CAMPAIGN OVER TROPICAL FOREST IN P-L-C and X-BAND

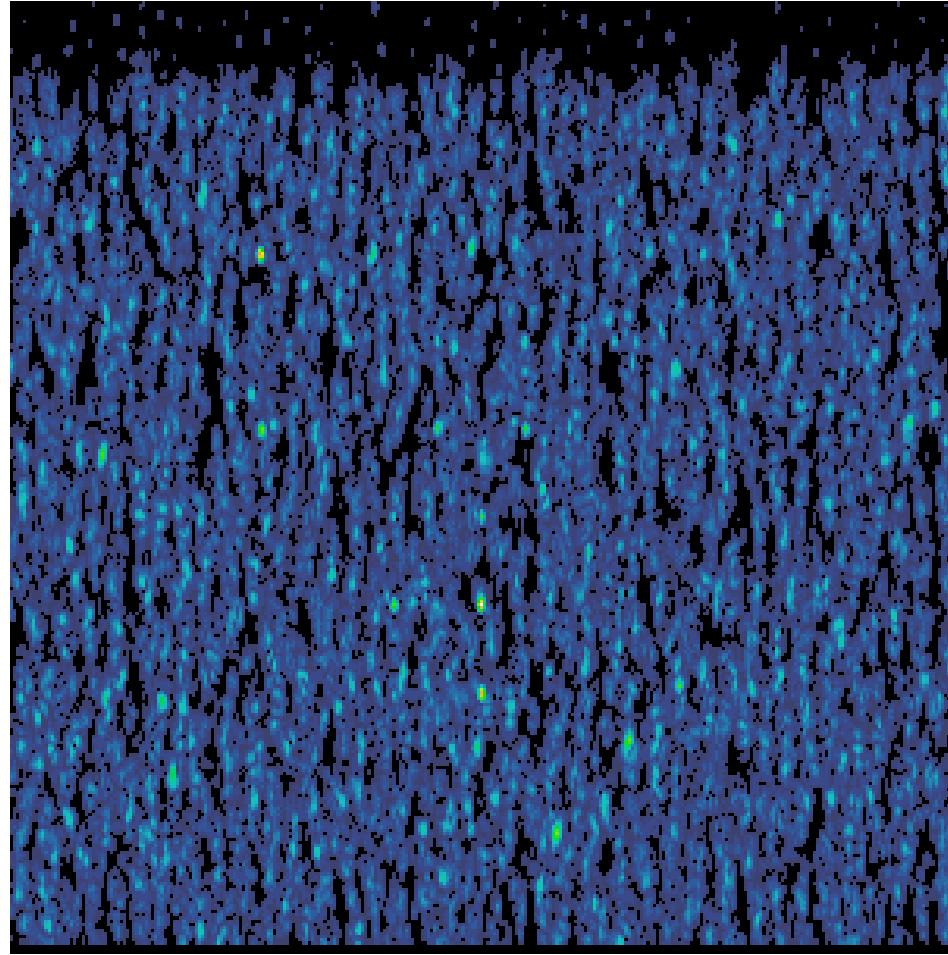
SAR, Synthetic Aperture Radar

European Space Agency-ESA ~ German Aerospace Centre-DLR ~ Wageningen University-WUR ~ Ministry of Forestry-MoF
Borneo Orangutan Survival Foundation-BOS ~ Sarvision The Netherlands-SVBV and Sarvision Indonesia-SVI

Future POLInSAR Application Developments:

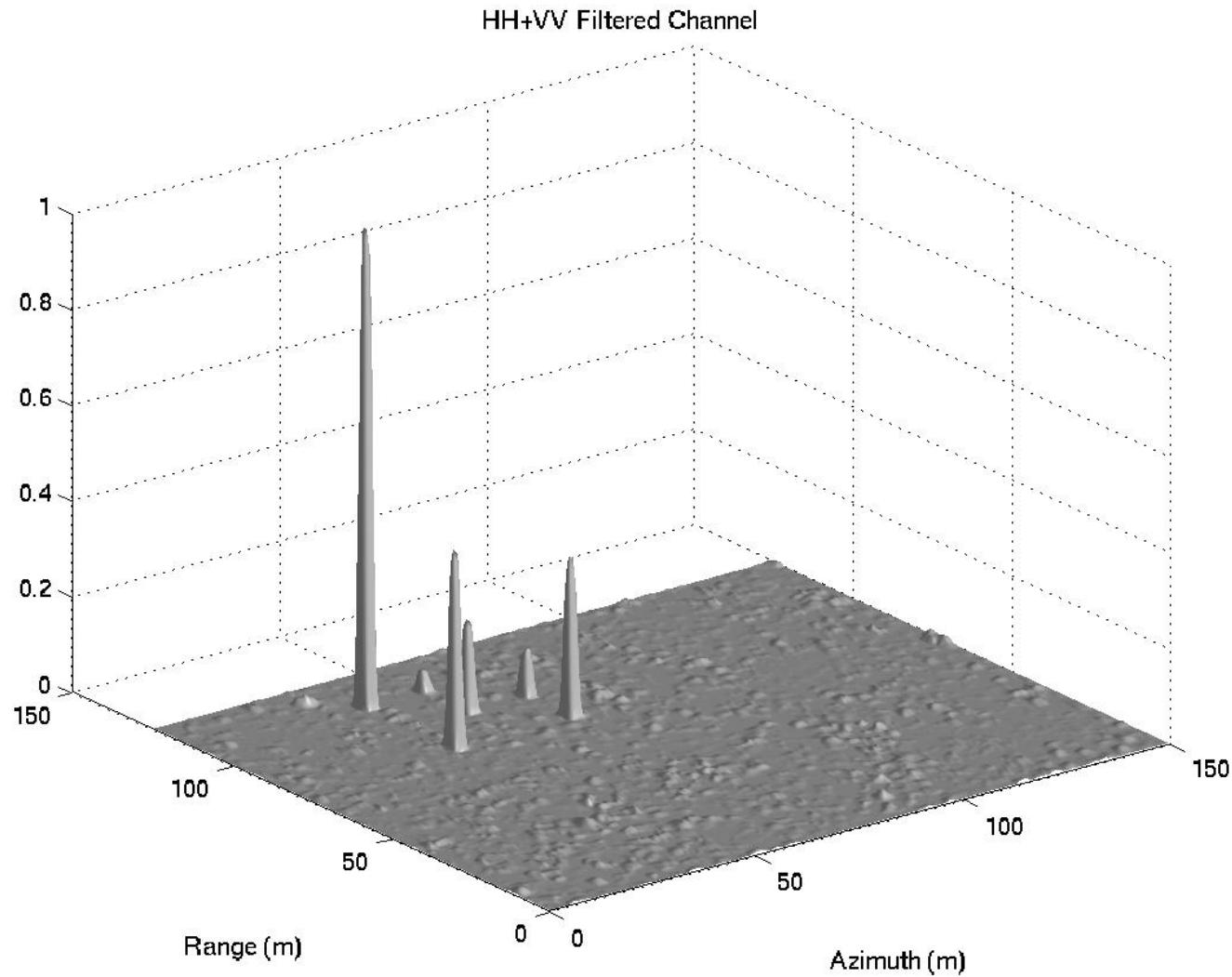
- Concealed Target Detection (FOPEN)

POLInSAR can be used to separate surface and volume contributions..with applications in target detection



L-Band FOPEN Simulations: Corner Reflectors in Scots Pine Forest
Courtesy of Dr. Mark Williams, DSTO, Australia

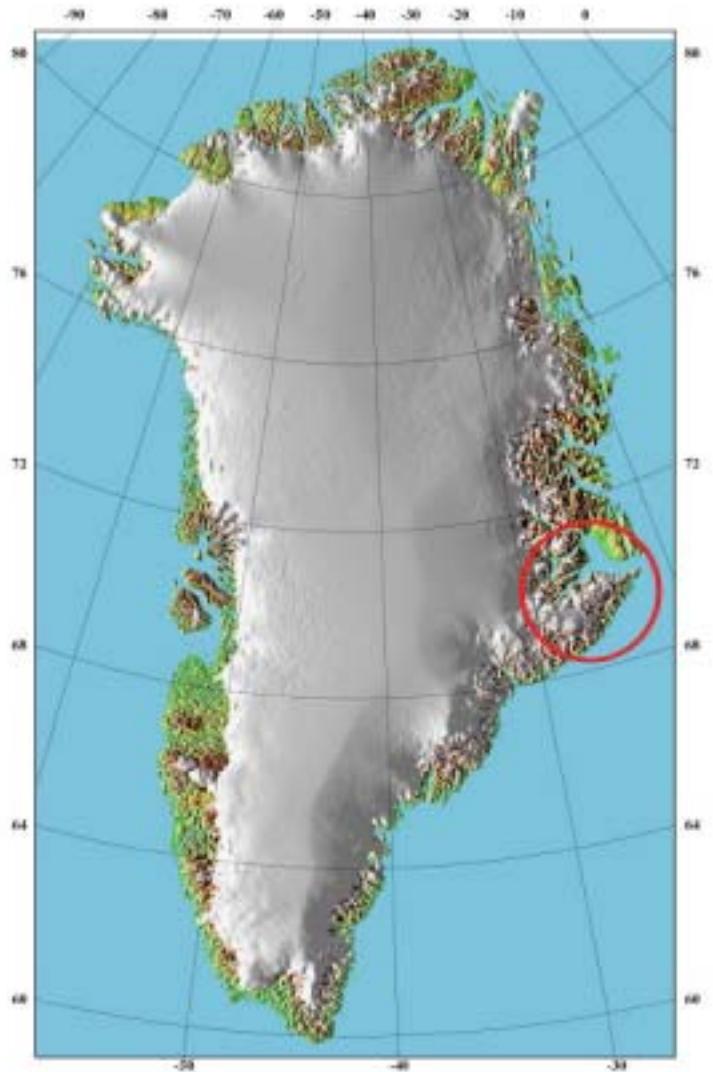
Detection of Obscured Corner Reflectors using POLInSAR



S.R. Cloude, D.G. Corr, M.L. Williams, "Target Detection Beneath Foliage Using Polarimetric SAR Interferometry", Waves in Random Media, volume 14, issue 2, pages S393 - S414., 2004

Land Ice and Snow Applications

Land ice site



Geikie ice cap, Greenland

Ice zones: percolation, (wet-snow)
Penetration: up to 13 m at C-band
Accumulation: 2 – 3 m per year
Elevation: 1600 – 2300 m
Latitude: 69°56' N
Size: 80 km (east-west)
15 km (north-south)
SAR mapping: Aug. 1997 and 1998

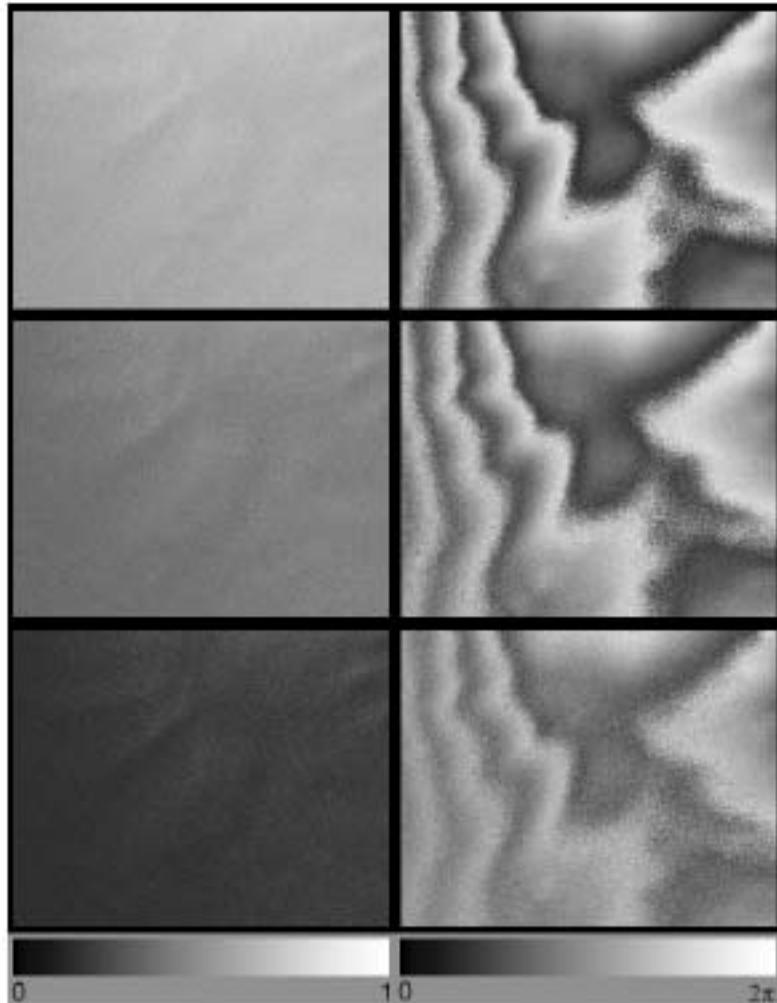
Optimization

amplitude

phase

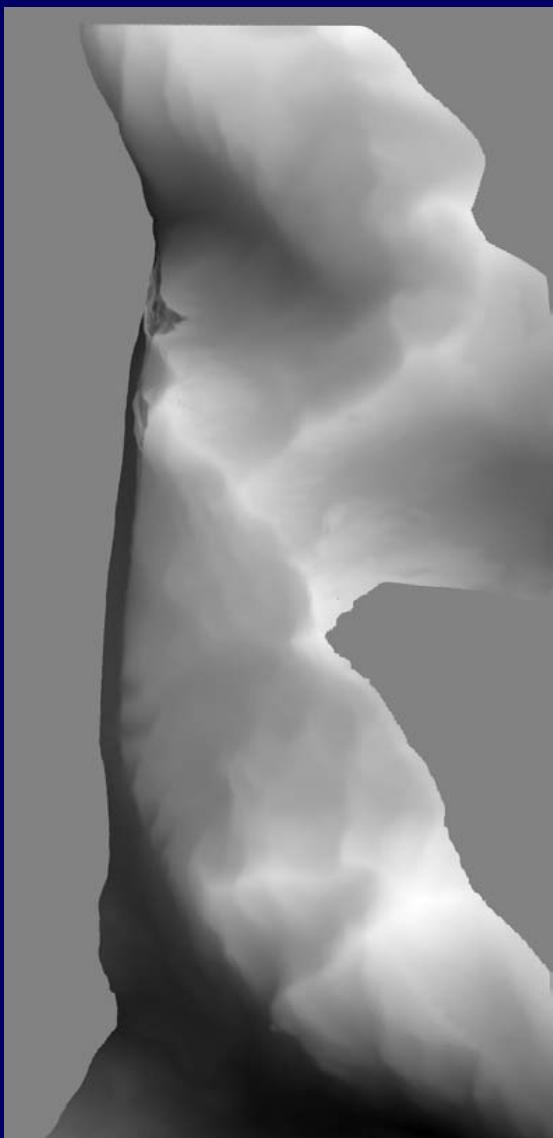
 $|\gamma_{\text{opt}1}|$ $\angle \gamma_{\text{opt}1}$

...need new model
developments
for interpretation
of data

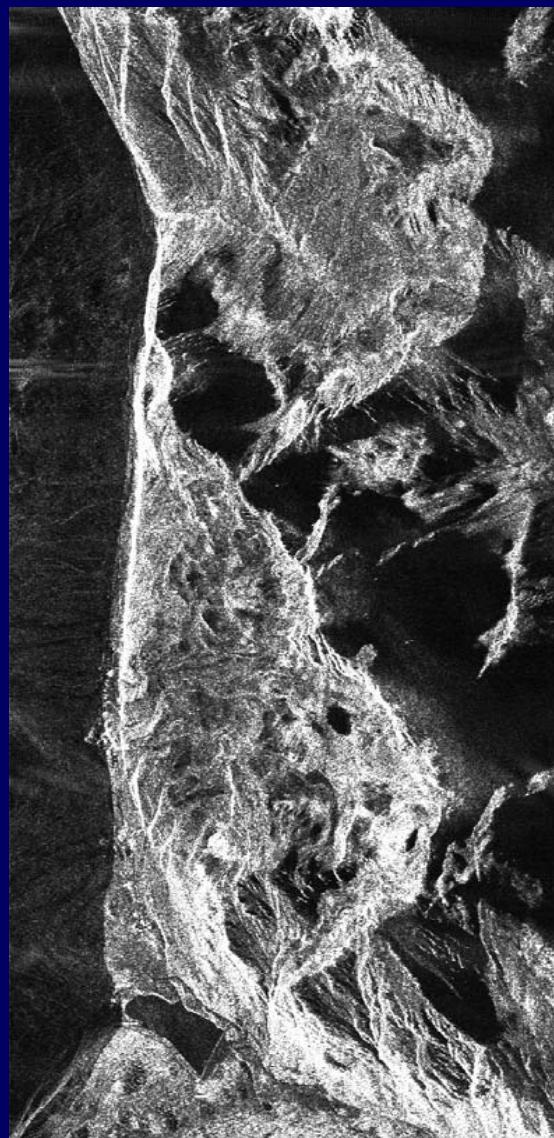
 $|\gamma_{\text{opt}2}|$ $\angle \gamma_{\text{opt}2}$ $|\gamma_{\text{opt}3}|$ $\angle \gamma_{\text{opt}3}$ 

Kühtai Test Site

L-band



X-band DEM



HV

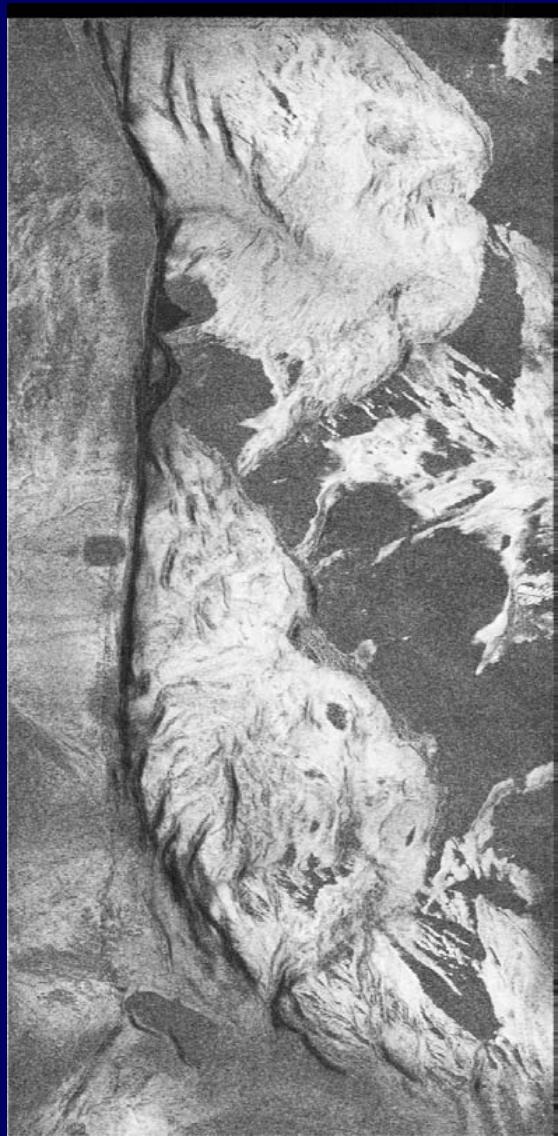
E-SAR / Test Site: Kuehtai / Austria

L-band

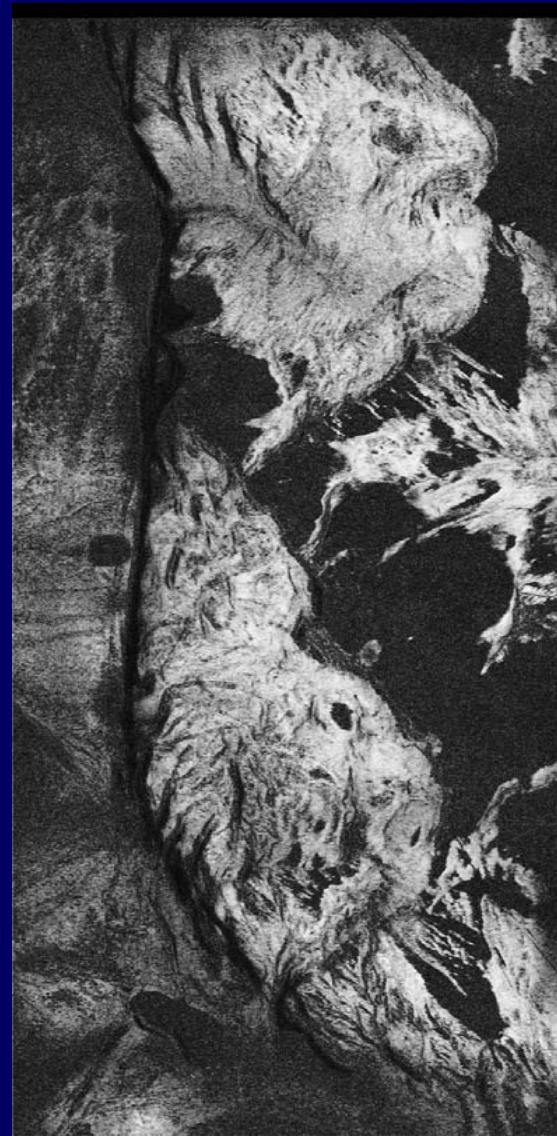


Baseline=20m

Opt 1

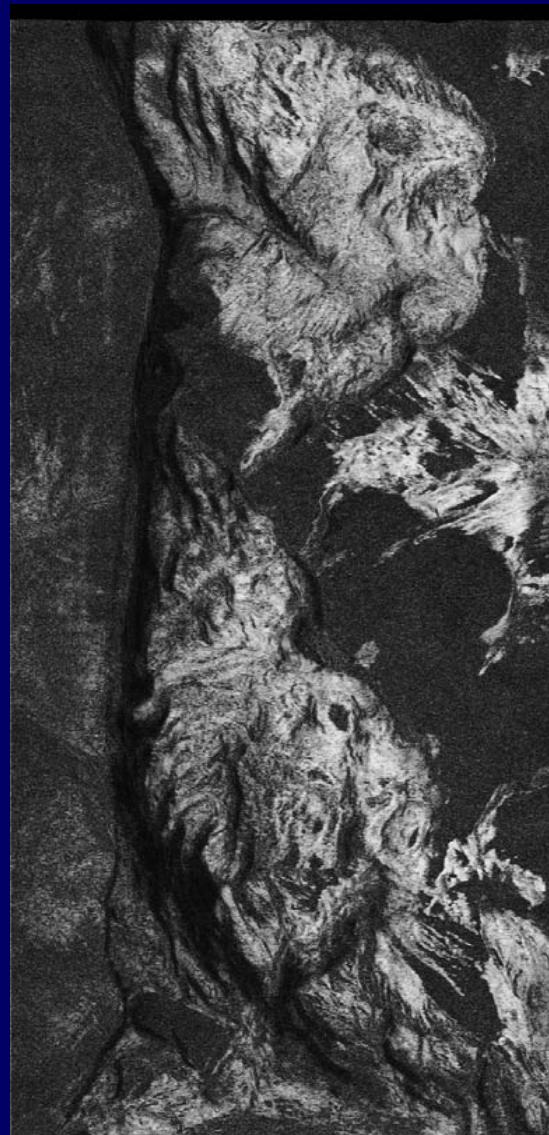


Opt 2



Opt 3

E-SAR / Test Site: Kuehtai / Austria

L-band*Baseline=40m**Opt 1**Opt 2**E-SAR / Test Site: Kuehtai / Austria**Opt 3*

Multi-Baseline Techniques:

a) Vertical Structure

Structural Ambiguity in Single Baseline Interferometry (SBPI)

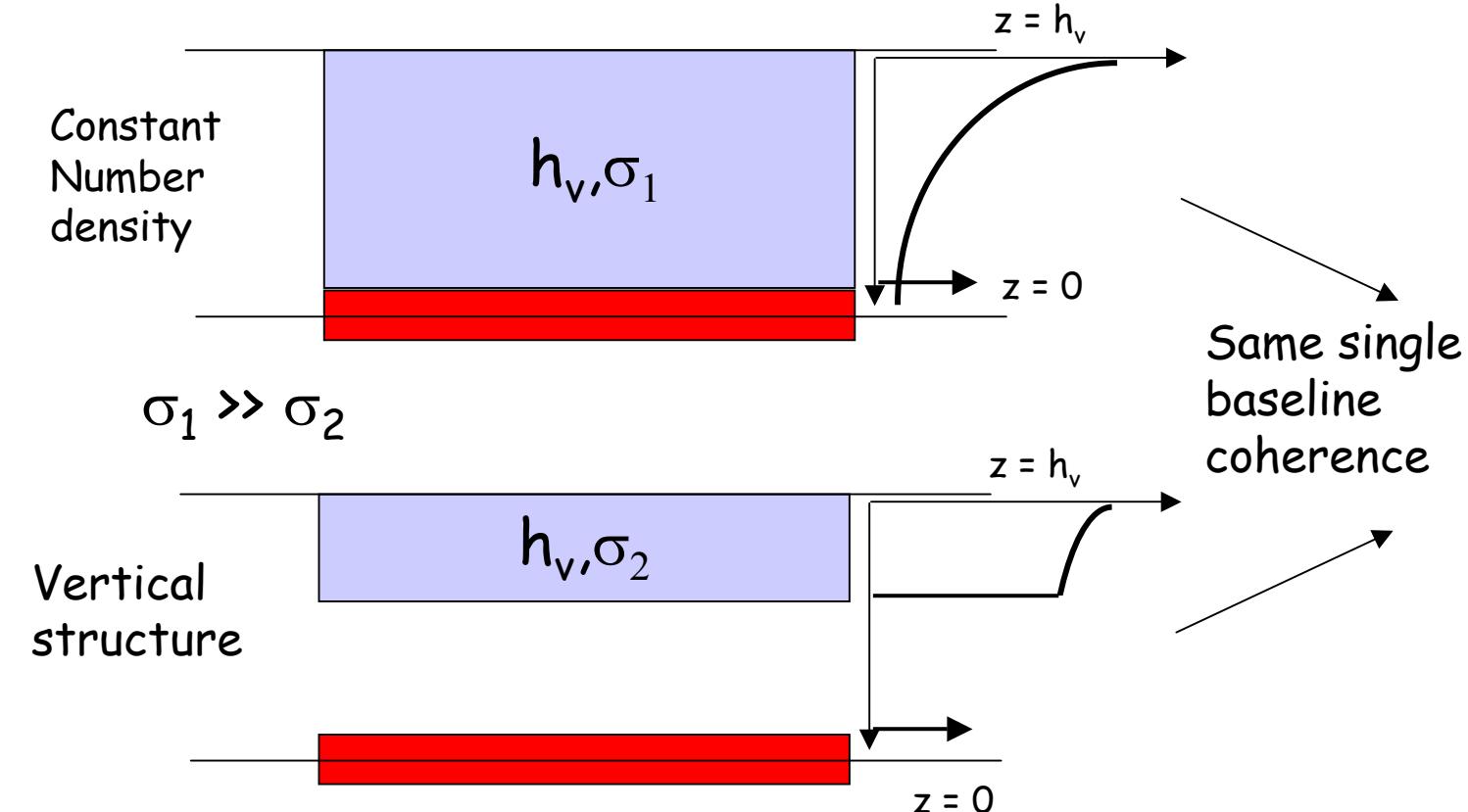


Constant
Number
density

$$\sigma_1 \gg \sigma_2$$

Vertical
structure

e.g Scots Pine



Same single
baseline
coherence

$$z = 0$$

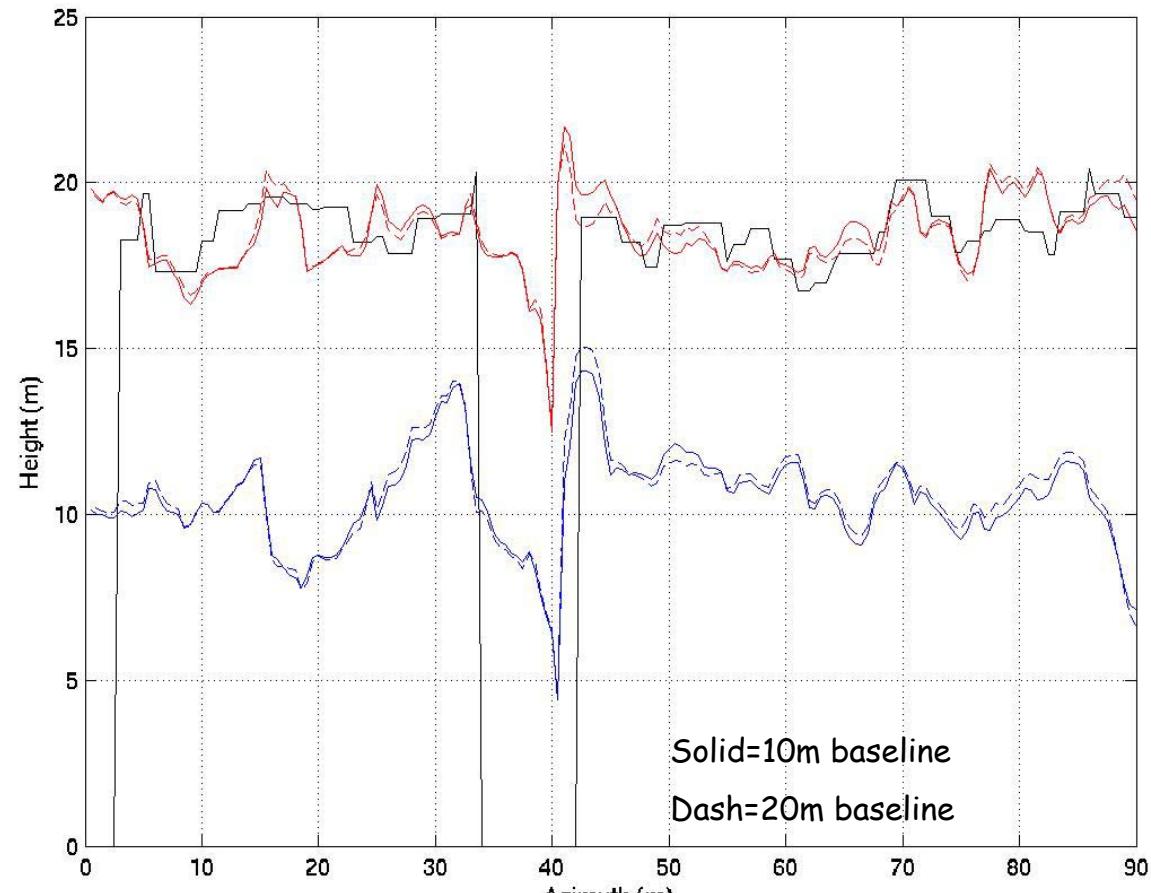
...need multi-baseline interferometry to resolve this ambiguity



The solution...dual baseline interferometry

...leads to better height estimation (red)

+ an estimate of crown depth (blue)

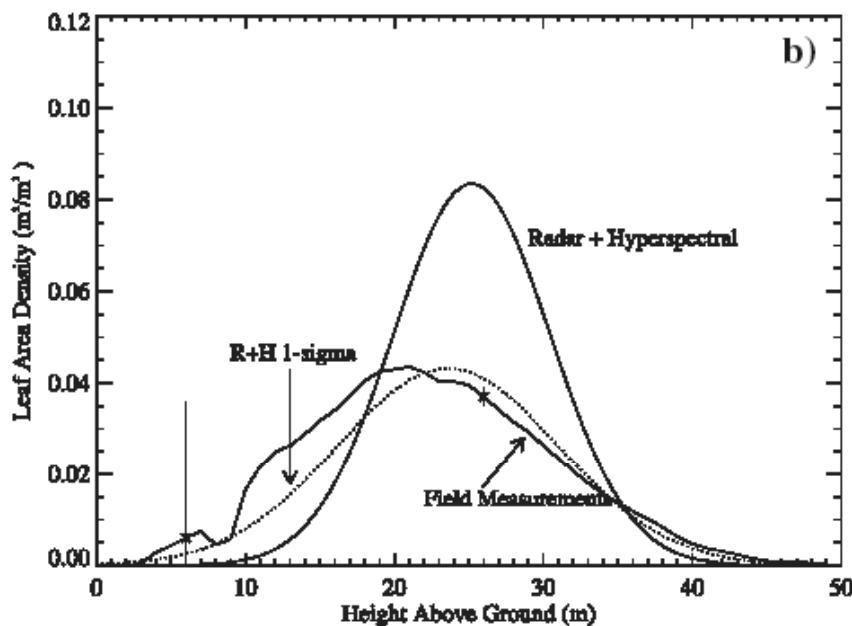


..Natural extension is to consider multiple baselines..

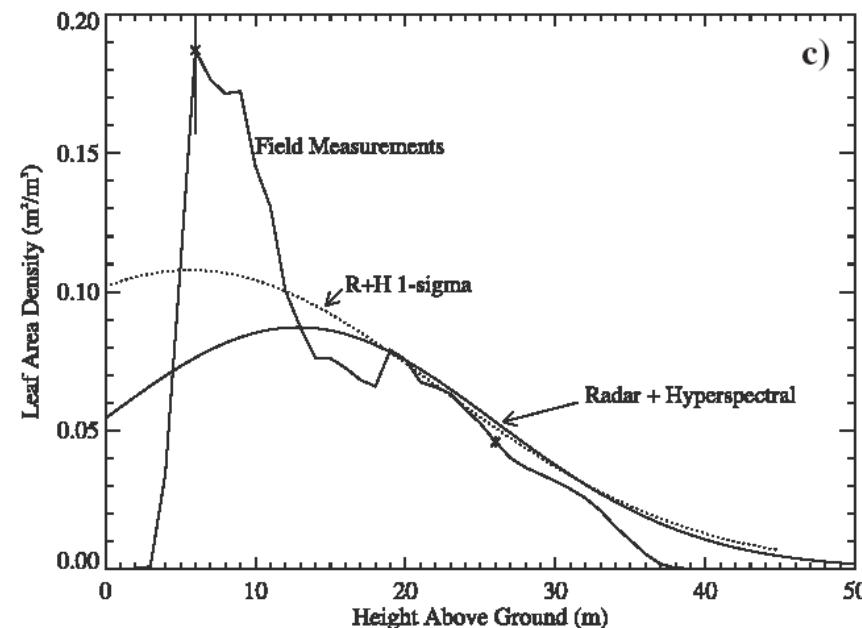


Example of LAD estimates using multi-baseline Interferometry + hyperspectral data

good fit...



...bad fit



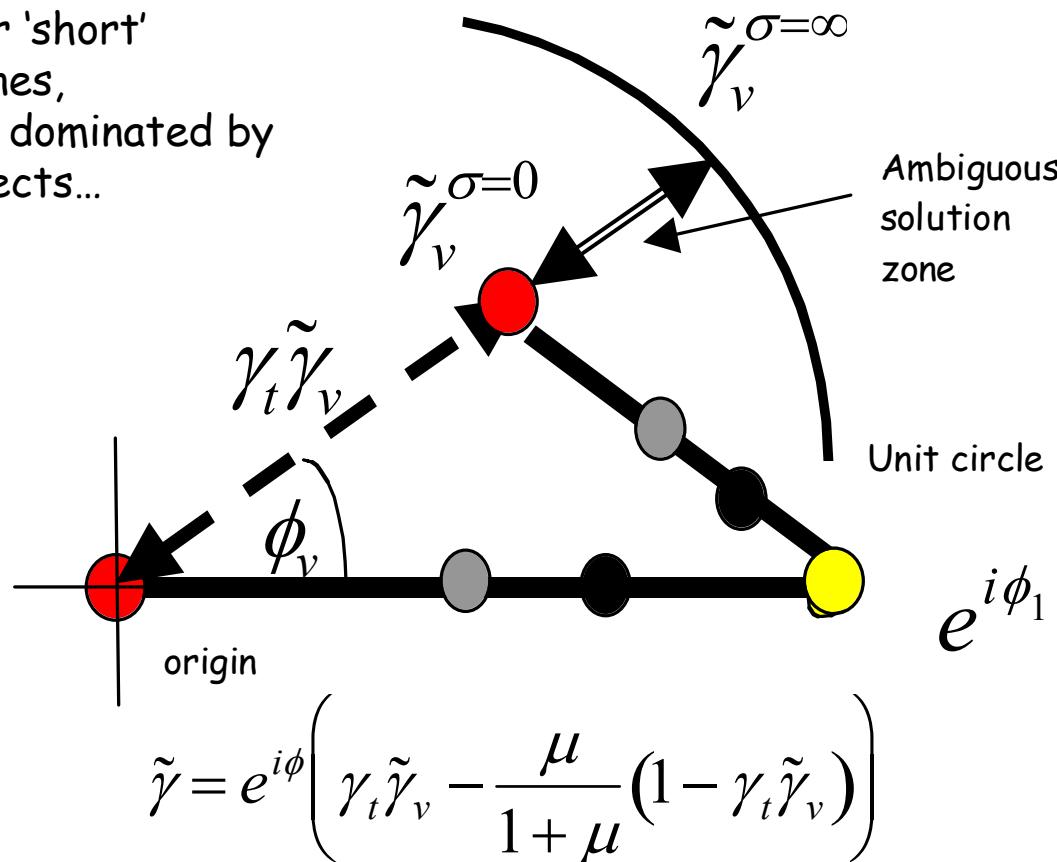
R.N. Treuhaft, G.P. Asner, B.E. Law, S. Van Tuyl, "Forest Leaf Area Density Profiles from the quantitative fusion of radar and hyperspectral data", J. Geophys. Res., 107(D21), 4568, 2002

Multi-Baseline Techniques:

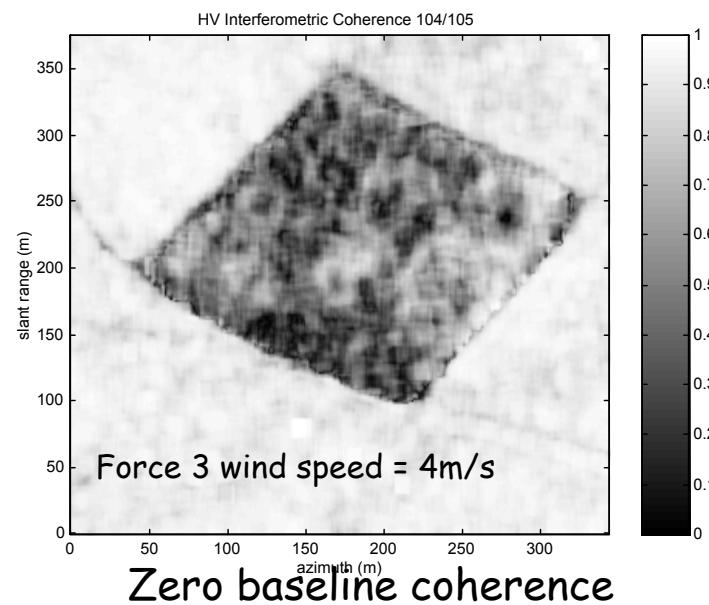
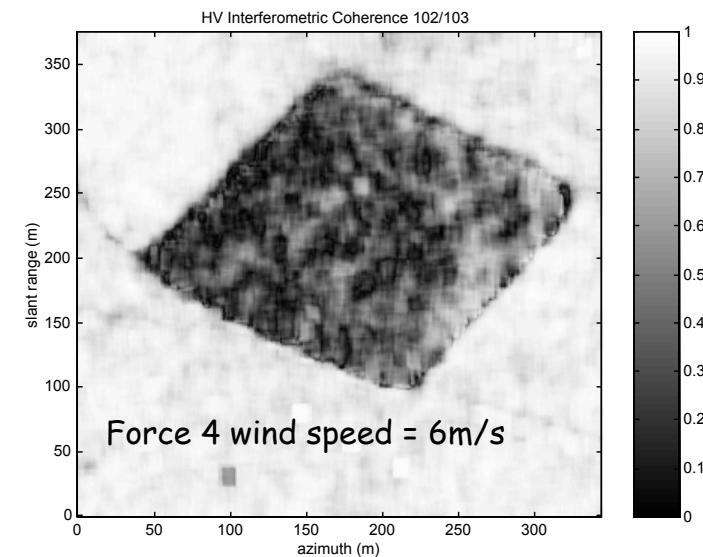
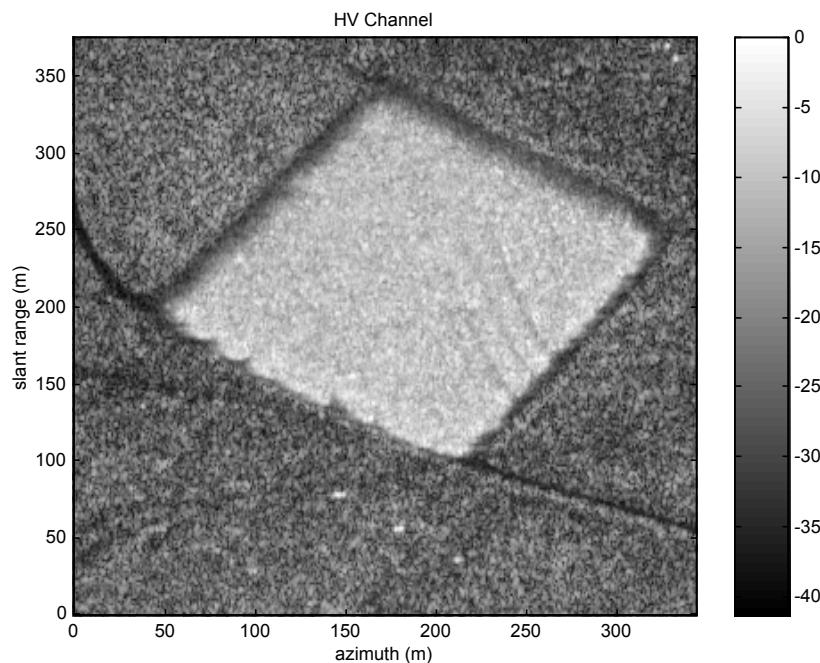
b) Temporal Decorrelation

Geometrical model for temporal decorrelation

Assume that for 'short' temporal baselines, decorrelation is dominated by wind driven effects...



Temporal decorrelation changes the observed coherence variation with polarisation but maintains the line model and causes an unknown rotation about the ground topography point...to test this model we use E-SAR/SIR-C data



Uniform Birch stand

Mean tree height = 17.4m

May 2002

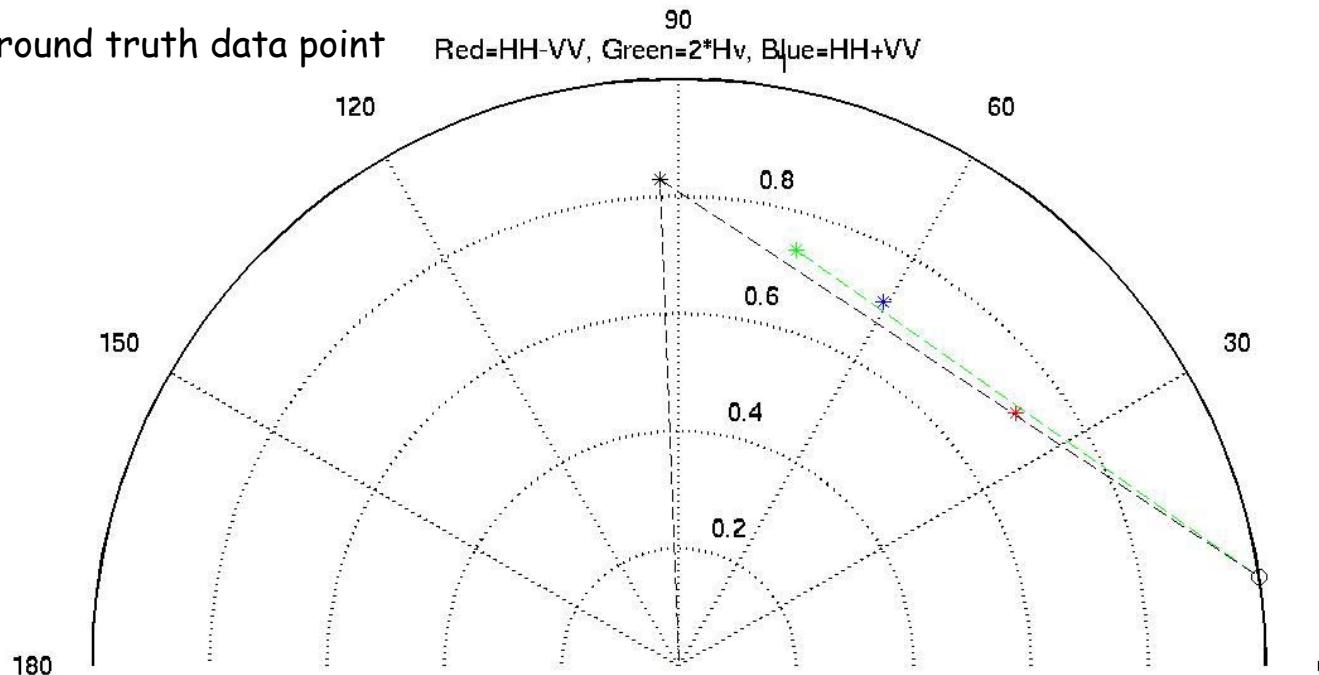
Weather conditions, dry/ gusting force 3-5

Zero baseline coherence

POLInSAR Coherence Loci: 8m baseline using known tree height and ground phase

black star = ground truth data point

Red=HH-VV, Green=2*Hv, Blue=HH+VV

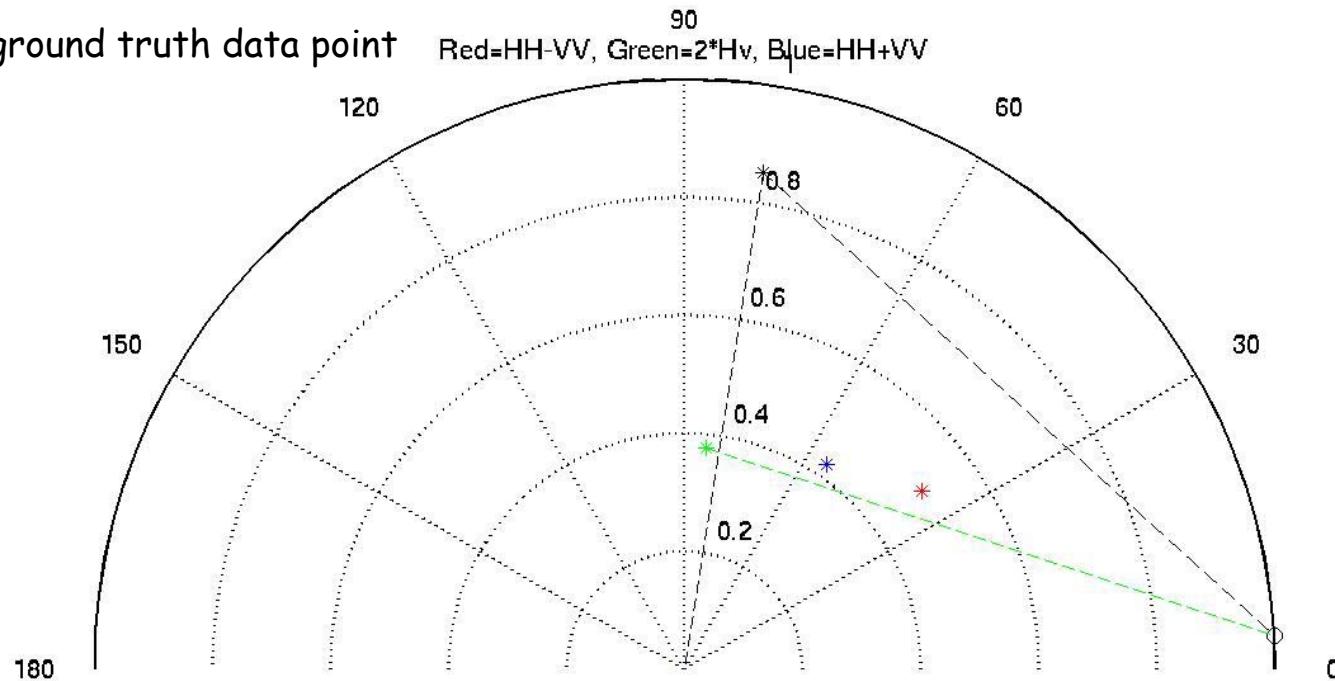


Fox Covert data point : zero temporal effect, $\mu_{\min} > 0$

POLInSAR Coherence Loci: 8m baseline using known tree height and ground phase

black star = ground truth data point

Red=HH-VV, Green=2*Hv, Blue=HH+VV

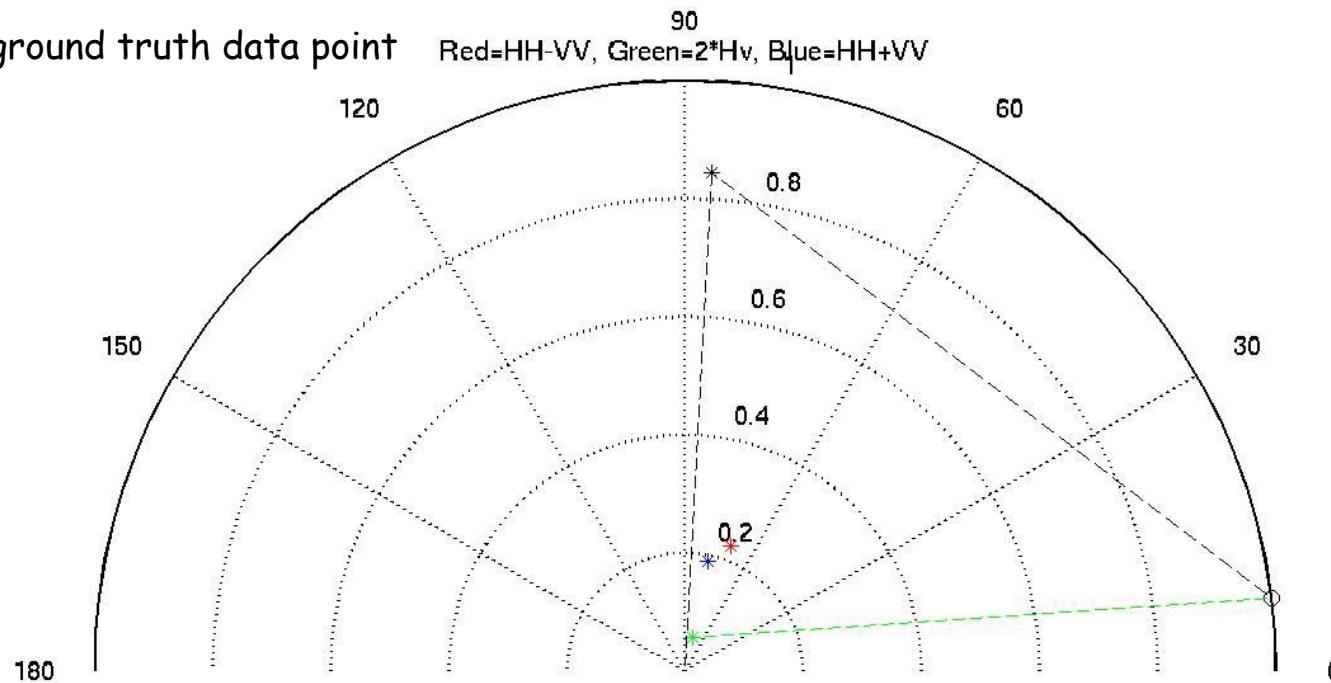


Fox Covert data point : moderate temporal effect, $\mu_{\min} = 0$

POLInSAR Coherence Loci: 8m baseline using known tree height and ground phase

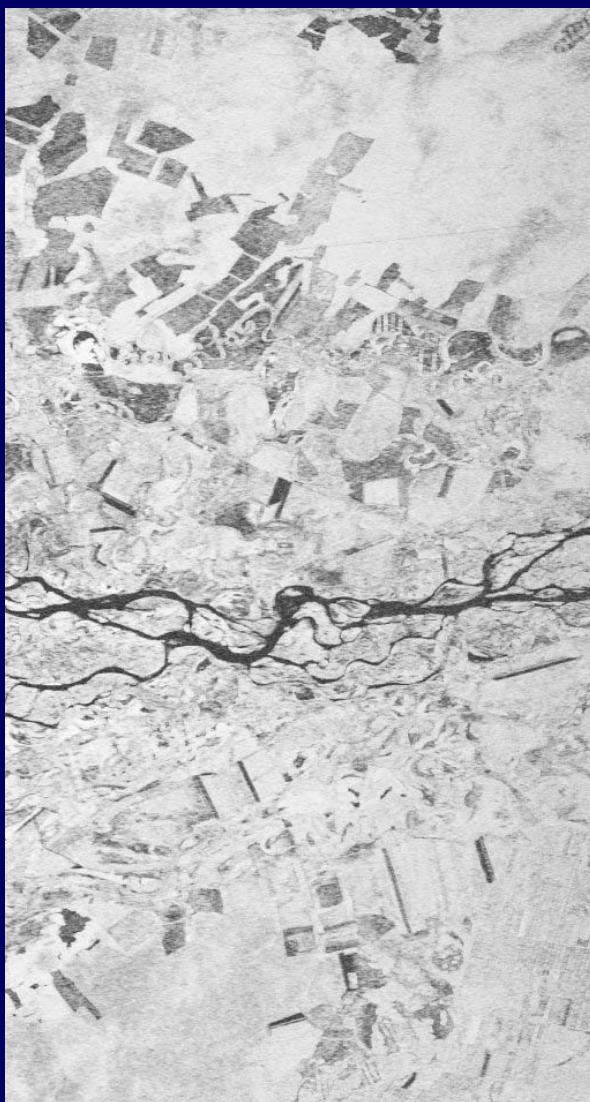
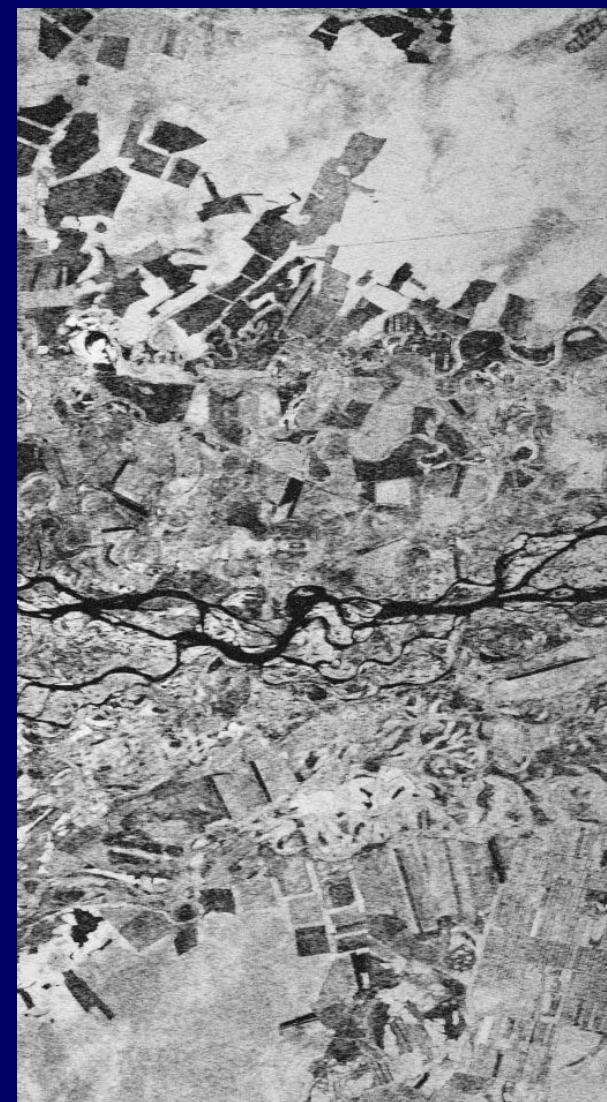
black star = ground truth data point

Red=HH-VV, Green=2*Hv, Blue=HH+VV



Fox Covert data point : strong temporal effect, $\mu_{\min} = 0$

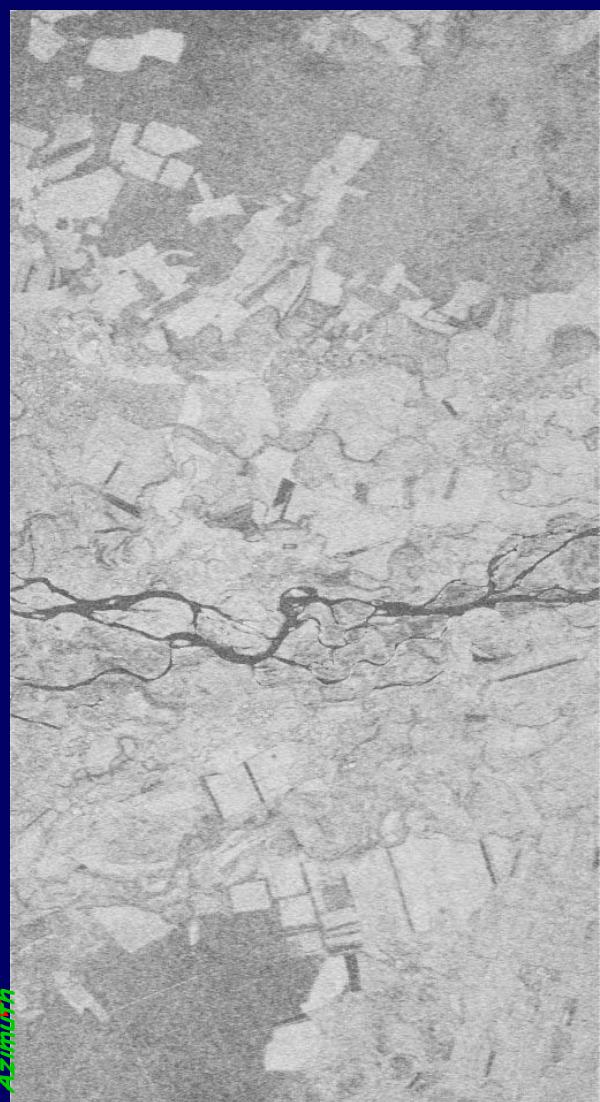
Test Data : SIR-C L-Band

*L-band**SIR-C / Test Site: Kudara, Russia**Opt 1**Opt 2**Opt 3*

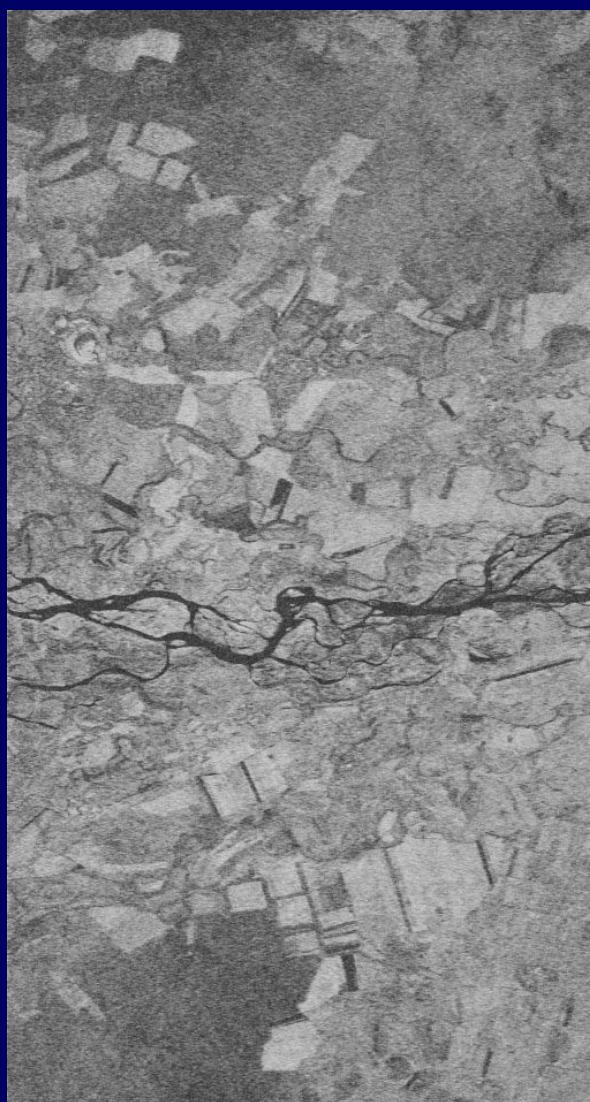
Test Data : SIR-C C-Band

C-band

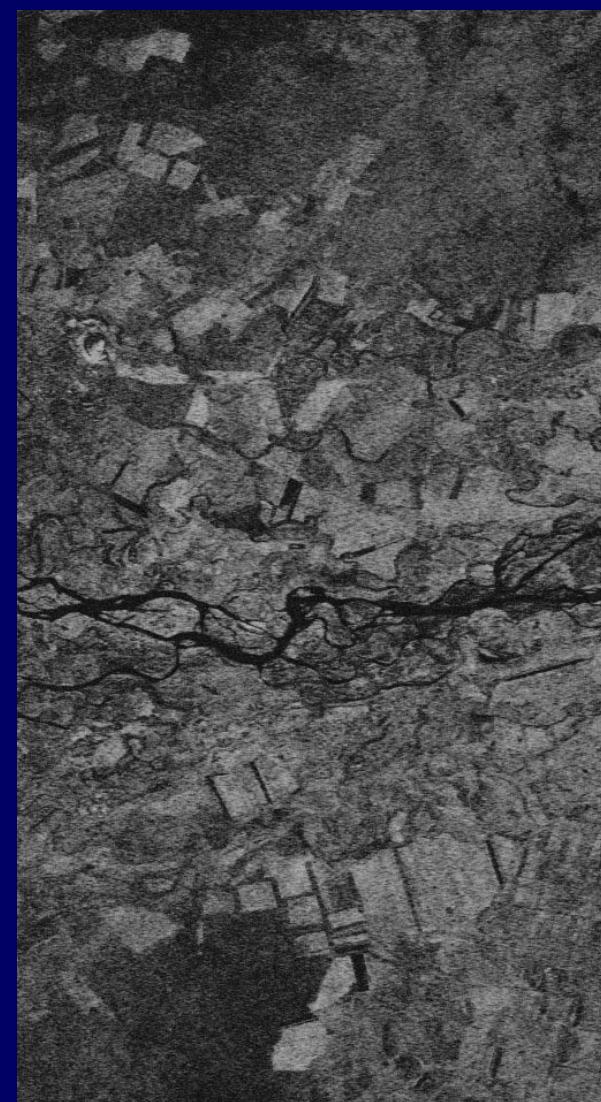
SIR-C / Test Site: Kudara, Russia



Opt 1



Opt 2



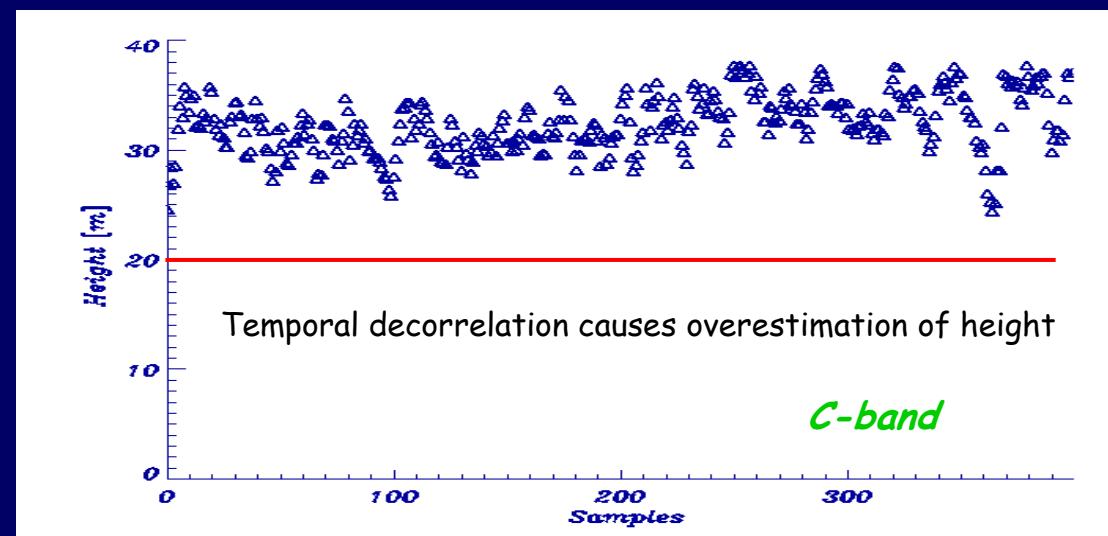
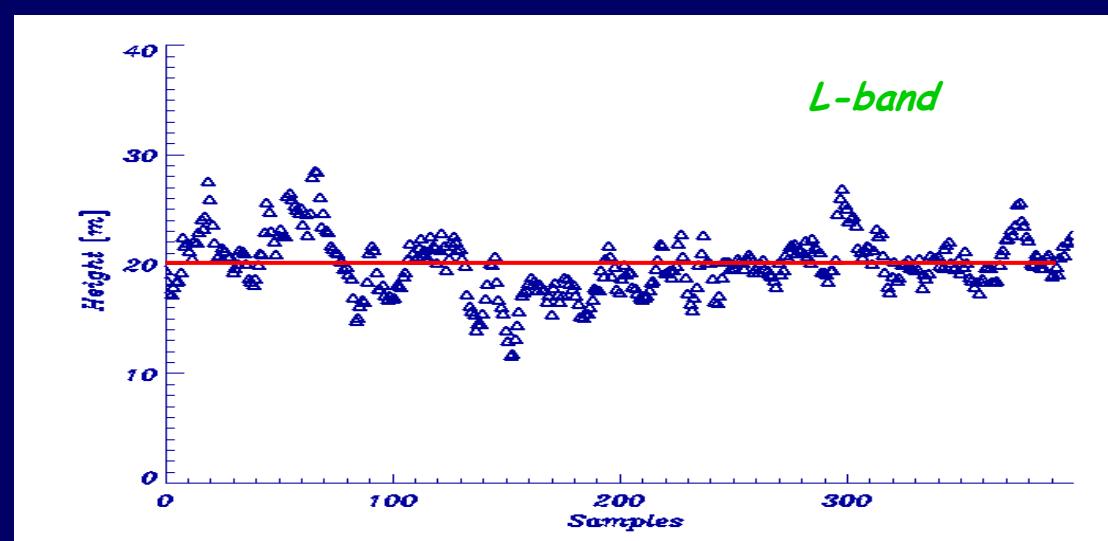
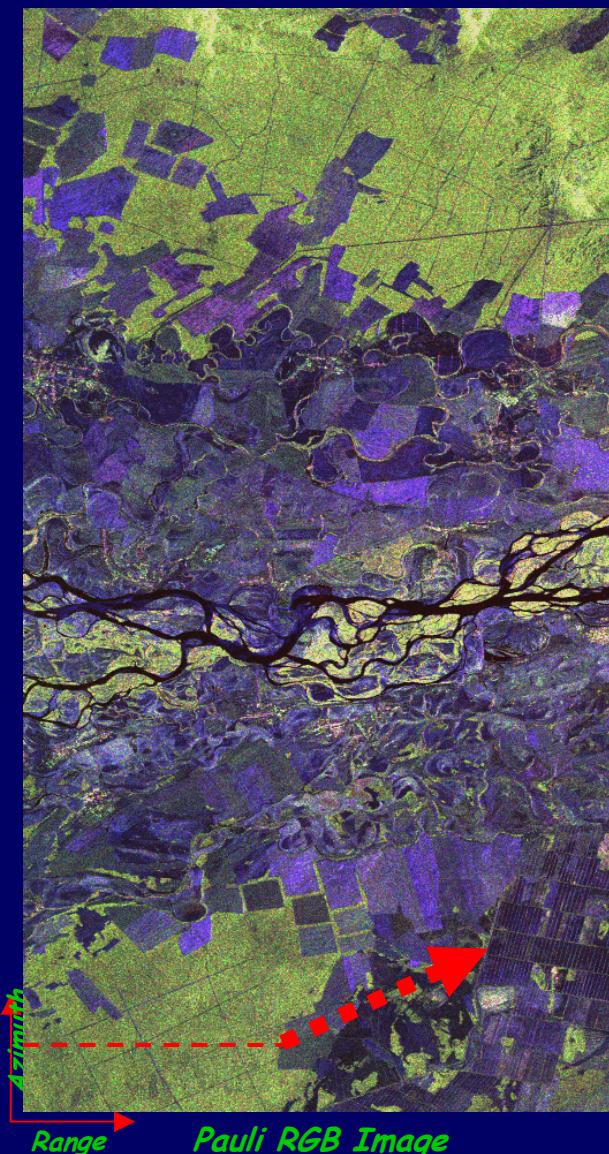
Opt 3

Range

Tree Height Estimation

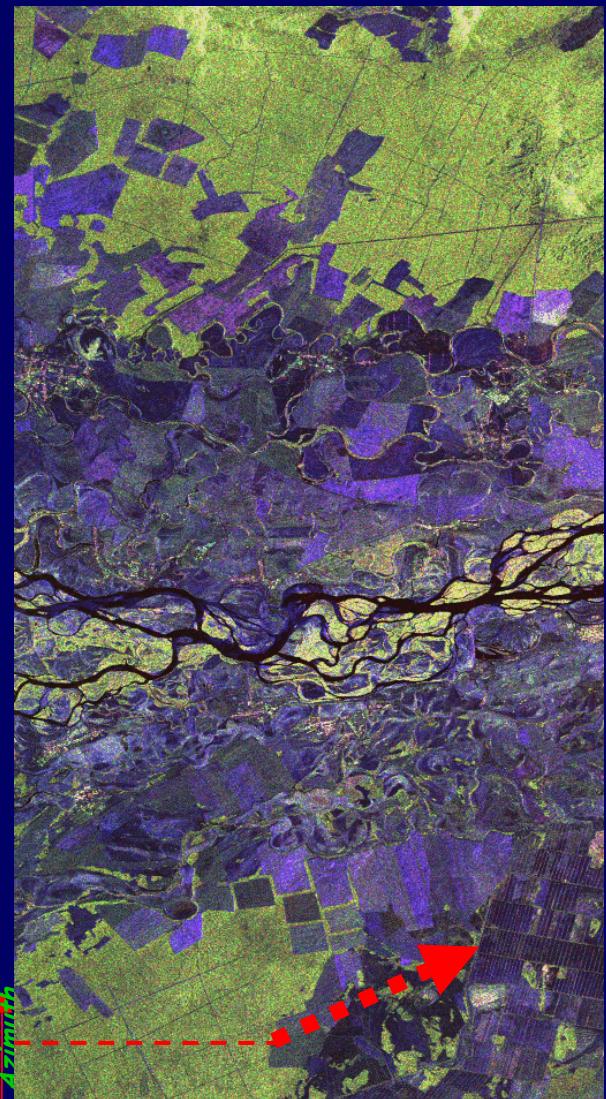
Temporal Baseline: 48 Hours

SIR-C / Test Site: Kudara, Russia



Dual Frequency Compensation for Temporal Effects

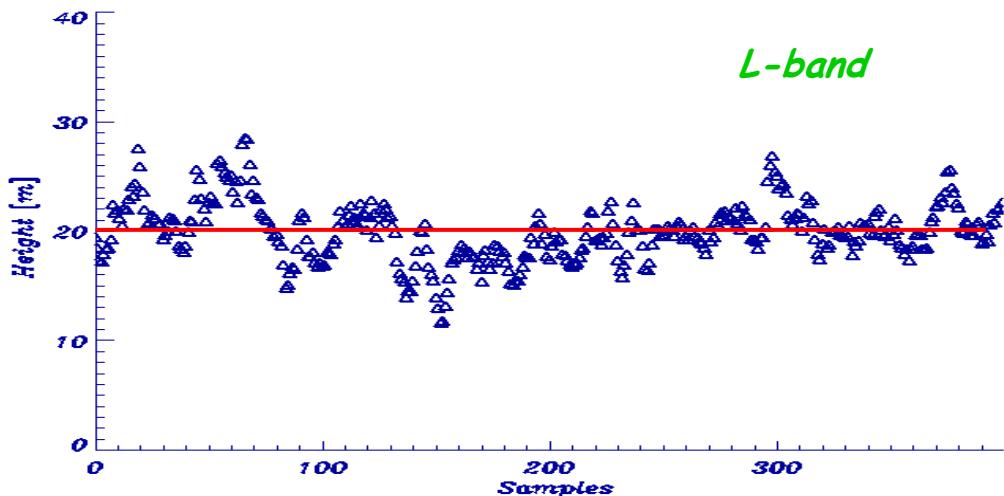
Temporal Baseline: 48 Hours



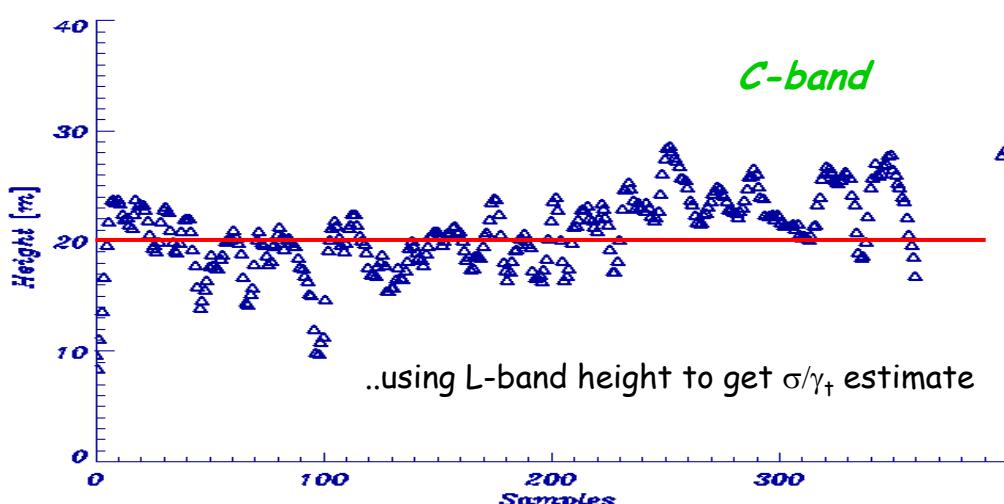
Pauli RGB Image

SIR-C / Test Site: Kudara, Russia

L-band



C-band



...using L-band height to get σ/γ_t estimate

Agriculture:

Plant Water Content

Ulaby Uniaxial Vegetation Model

Mixture of 2 components:

Leaf (L) + Stalks (S)

\downarrow Azimuthal \nearrow uniaxial
Symmetry crystal

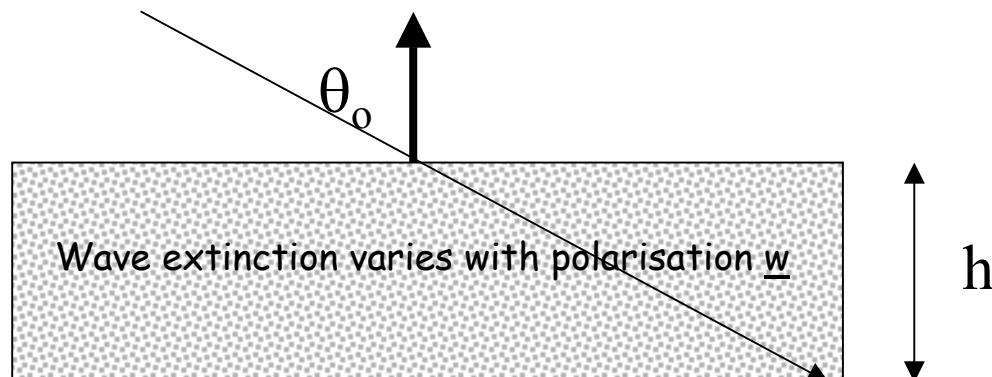
$$L(\underline{w}) = L_L + L_S(\underline{w})$$

where

$$L_L \approx \exp\left(-\frac{4\pi\nu_L \epsilon''_L h}{3\lambda \cos\theta_o}\right) \Rightarrow h\nu_L = LAI \bar{t} \quad \text{..in small albedo regime absorption loss} \gg \text{scattering loss}$$

$$L_S \Rightarrow \begin{cases} L_{xx} \approx \exp\left(-\frac{4\pi n''_o h}{\lambda \cos\theta_o}\right) & n''_o = \text{Im}(\sqrt{\epsilon_o}) \quad \epsilon_o \approx (1+2\nu_s) - i\left(\frac{4\nu_s \epsilon''_s}{(\epsilon''_s)^2 + (\dot{\epsilon}_s)^2}\right) \\ L_{yy} \approx \exp\left(-\frac{4\pi(\cos^2\theta_o n''_o + \sin^2\theta_o n''_e)h}{\lambda \cos\theta_o}\right) & n''_e = \text{Im}(\sqrt{\epsilon_e}) \quad \epsilon_e \approx (1+\nu_s(\dot{\epsilon}_s - 1)) - i\nu_s \epsilon''_s \end{cases}$$

x and y are the eigenpolarisations: typically h and v



L component matches the random volume assumption..

.. but the S component requires a multi-channel coherence description

...the oriented volume of 'ov' model.. When $S \gg L$

Differential Extinction and Oriented Volume (OV) Model

If $\sigma_y \gg \sigma_x$ (strong uniaxial component) then $|\tilde{\gamma}_1| > |\tilde{\gamma}_2| > |\tilde{\gamma}_3| \geq 0$

..so we get a measurable difference between the coherences in different polarisations which in turn can be related to physical parameters as:

$$\tilde{\gamma}_3 = \frac{2\sigma_x e^{i\phi(z_o)}}{\cos \theta_o (e^{2\sigma_x h_v / \cos \theta_o} - 1)} \int_0^h e^{ik_z z'} e^{\frac{2\sigma_x z'}{\cos \theta_o}} dz'$$

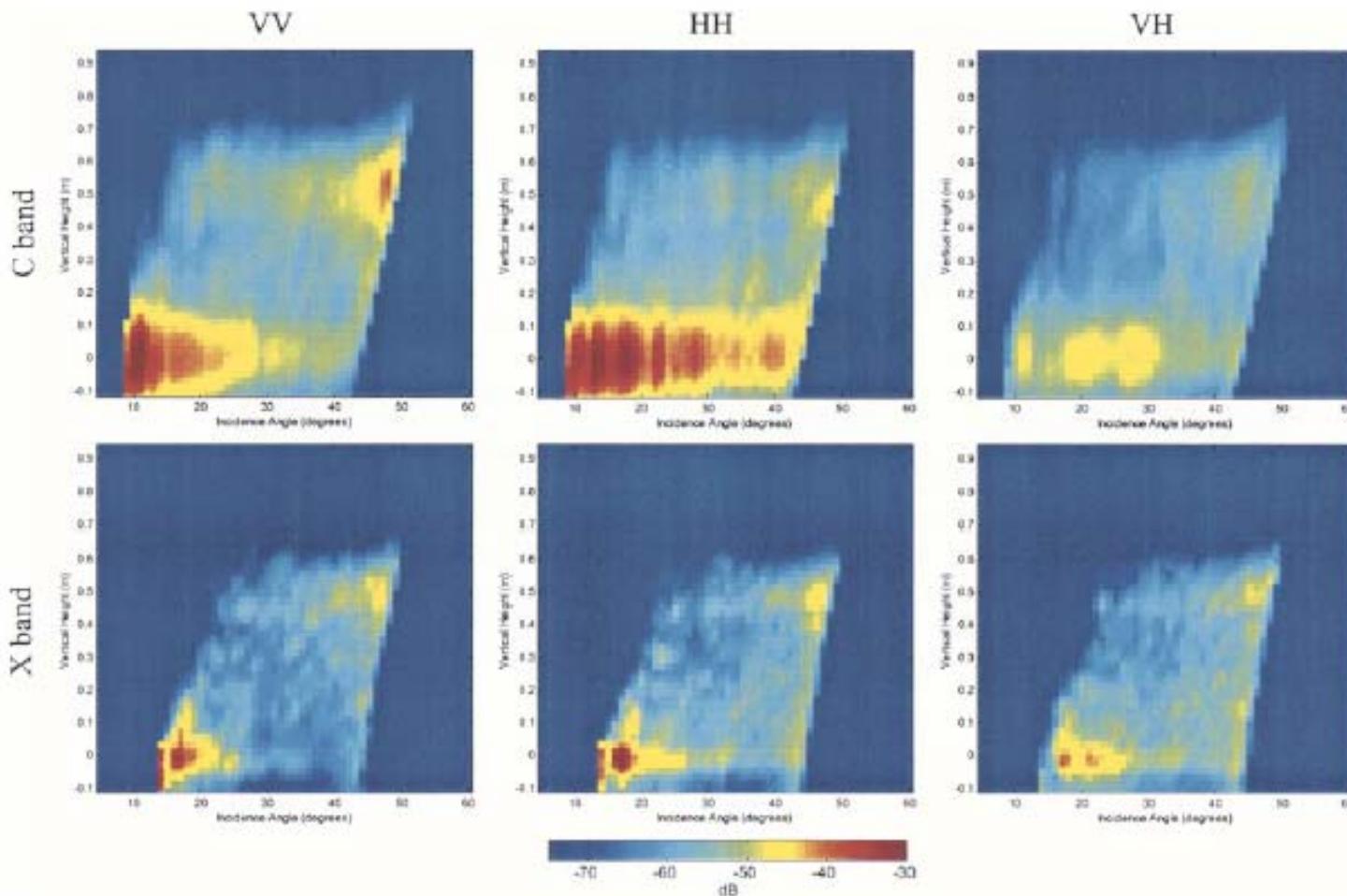
$$\tilde{\gamma}_2 = \frac{\sigma_x + \sigma_y e^{i\phi(z_o)}}{\cos \theta_o (e^{(\sigma_x + \sigma_y) h_v / \cos \theta_o} - 1)} \int_0^h e^{ik_z z'} e^{\frac{(\sigma_x + \sigma_y) z'}{\cos \theta_o}} dz'$$

$$\tilde{\gamma}_1 = \frac{2\sigma_y e^{i\phi(z_o)}}{\cos \theta_o (e^{2\sigma_y h_v / \cos \theta_o} - 1)} \int_0^h e^{ik_z z'} e^{\frac{2\sigma_y z'}{\cos \theta_o}} dz'$$

...now 6 observations with 4 unknowns ($\sigma_x, \sigma_y, h_v, \phi$)..can be inverted..but..

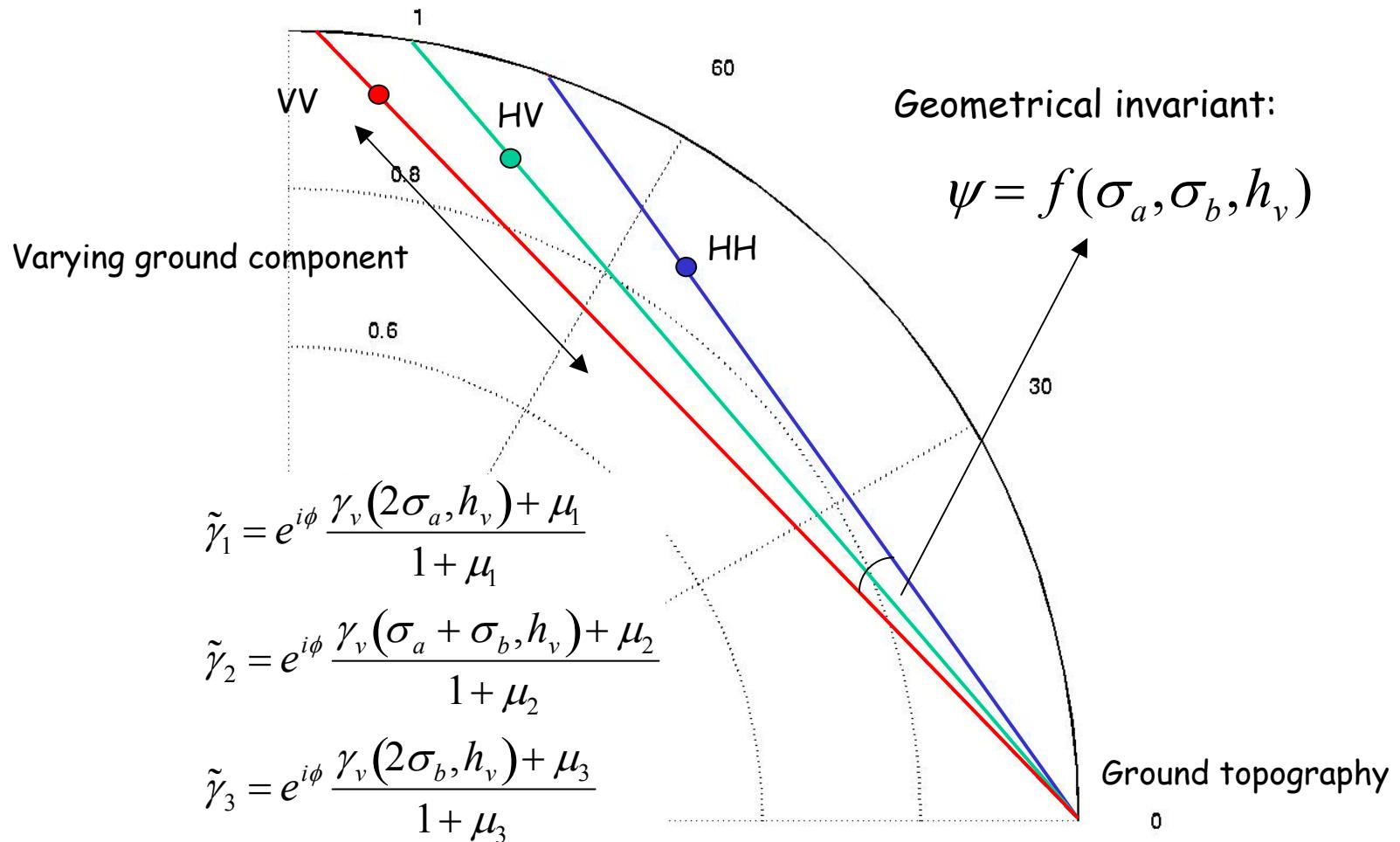
...need to consider the influence of surface scattering
..leads to oriented volume over a ground (ovog) model

Example : Ground Effects in Wheat Scattering



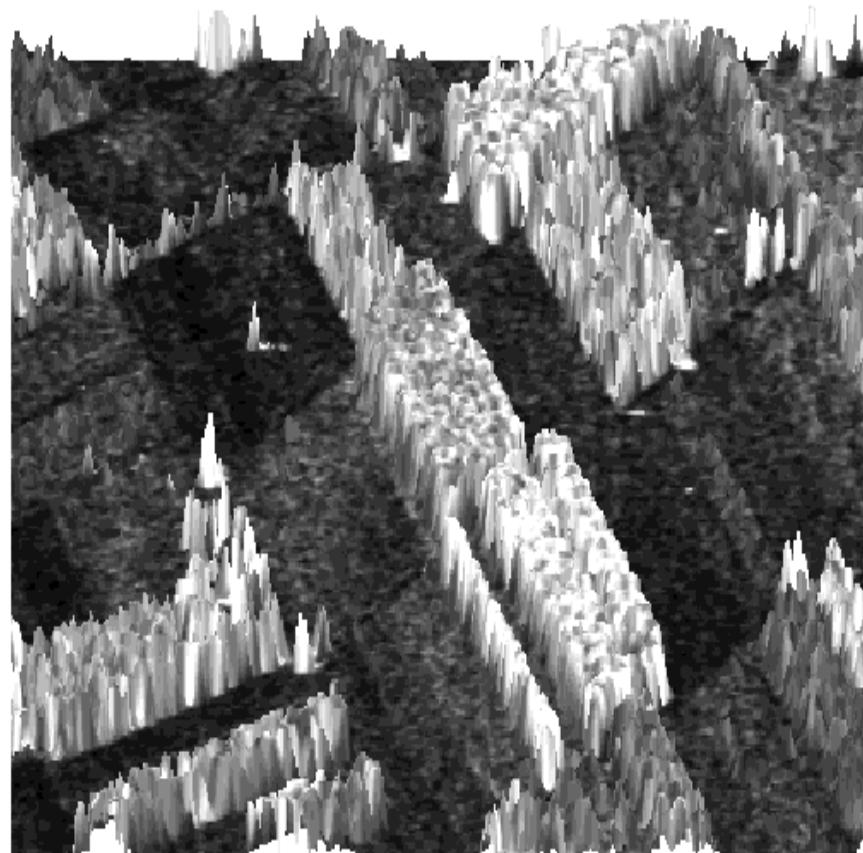
S.C.M. Brown, S Quegan, K Morrison, J Bennett, G Cookmartin,
 "High Resolution Measurements of Scattering in Wheat Canopies-Implications for Crop Parameter Retrieval",
 IEEE Trans GRS 41 (7), July 2003, pp 1602-1610

Geometry of the oriented-volume-over-ground or 'ovog' model



POLInSAR Agricultural Applications

..using volume only 'ovog' inversion

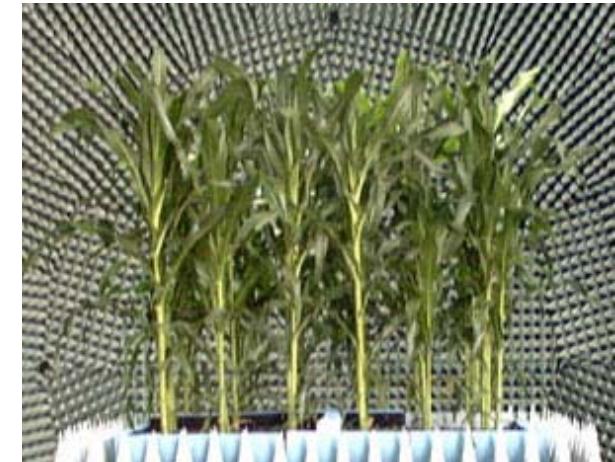
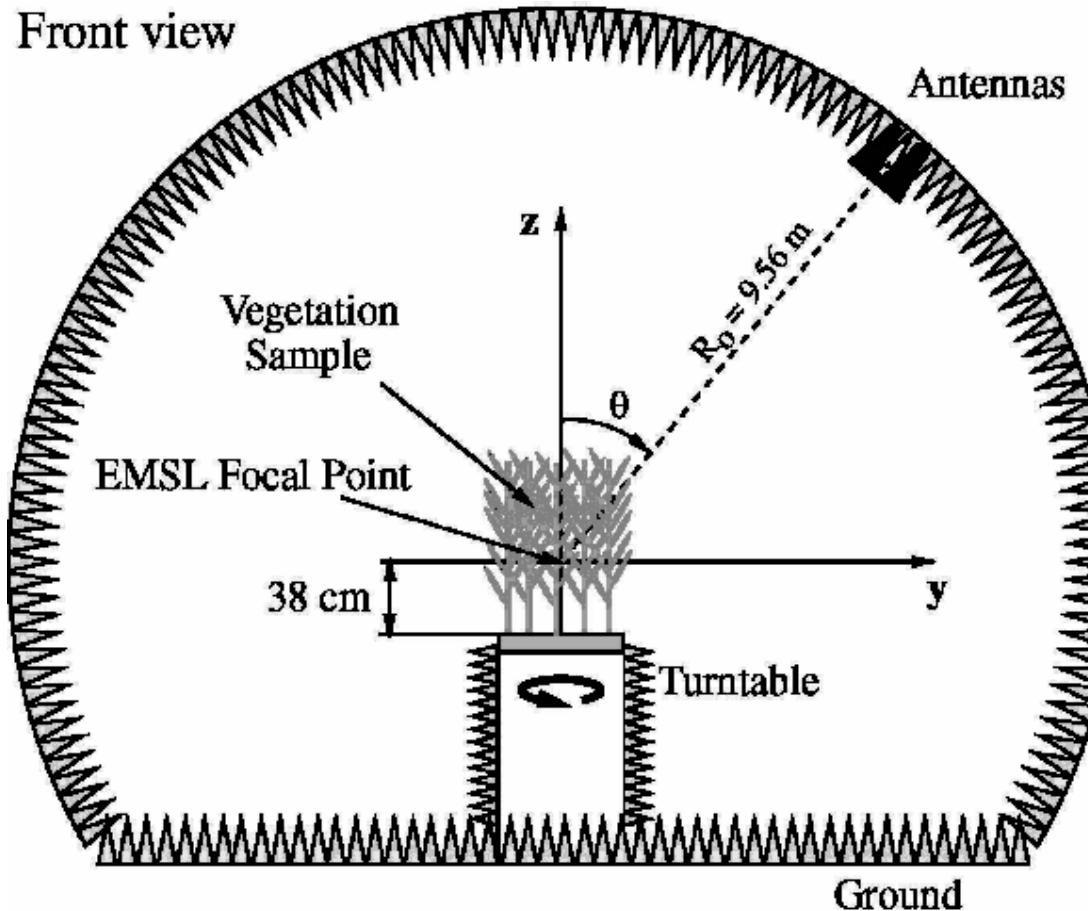


...potentially Crop Height, Vegetation Moisture Content, Surface Moisture..

...use GB-POLInSAR and Coherent EM Modelling to investigate..

EMSL POIInSAR Maize Experiment

Front view



6×6 maize plants ($2\text{m} \times 2\text{m}$)

$$hv = 1.8\text{m}$$

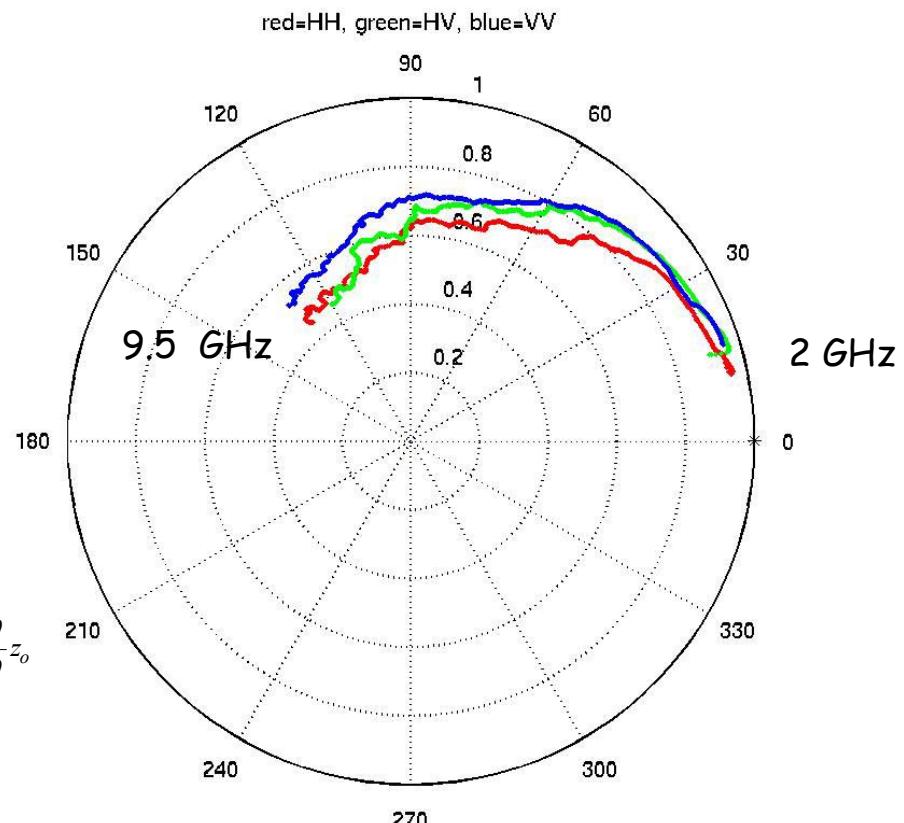
$1.5 - 9.5 \text{ GHz}$ (10MHz steps)

$$\theta = 44:0.25:45 \text{ degrees}$$

$$\phi = 0:5:360 \text{ degrees}$$

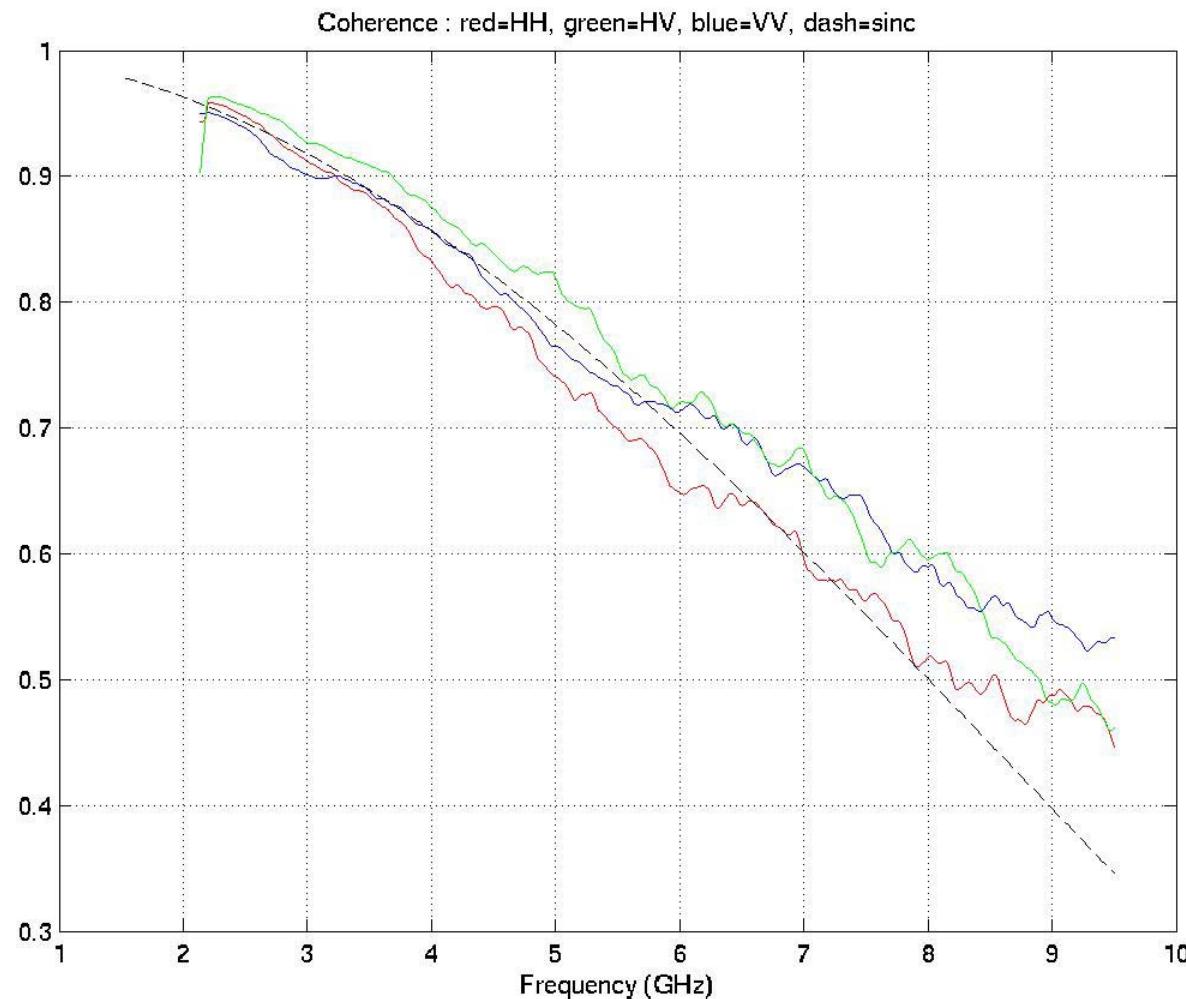
GB-POLInSAR Processing

$$\begin{aligned}
 & E_{\theta}^{pq}(f) \quad E_{\theta+\Delta\theta}^{pq}(f) \\
 \downarrow & \\
 & f \rightarrow f(1 - \frac{\Delta\theta}{\tan\theta}) \\
 \downarrow & \\
 & k_z = \frac{4\pi f \Delta\theta}{c \cdot \sin\theta} \\
 \downarrow & \\
 & s_1 s_2^* = E_{\theta}^{pq}(f).conj(E_{\theta+\Delta\theta}^{pq}\left(f - \frac{f\Delta\theta}{\tan\theta}\right)) e^{-i \frac{4\pi f \Delta\theta}{c \sin\theta} z_o} \\
 \downarrow & \\
 & \tilde{\gamma}_{pq}(f) = \frac{\langle s_1 s_2^* \rangle}{\sqrt{\langle s_1 s_1^* \rangle \langle s_2 s_2^* \rangle}}
 \end{aligned}$$

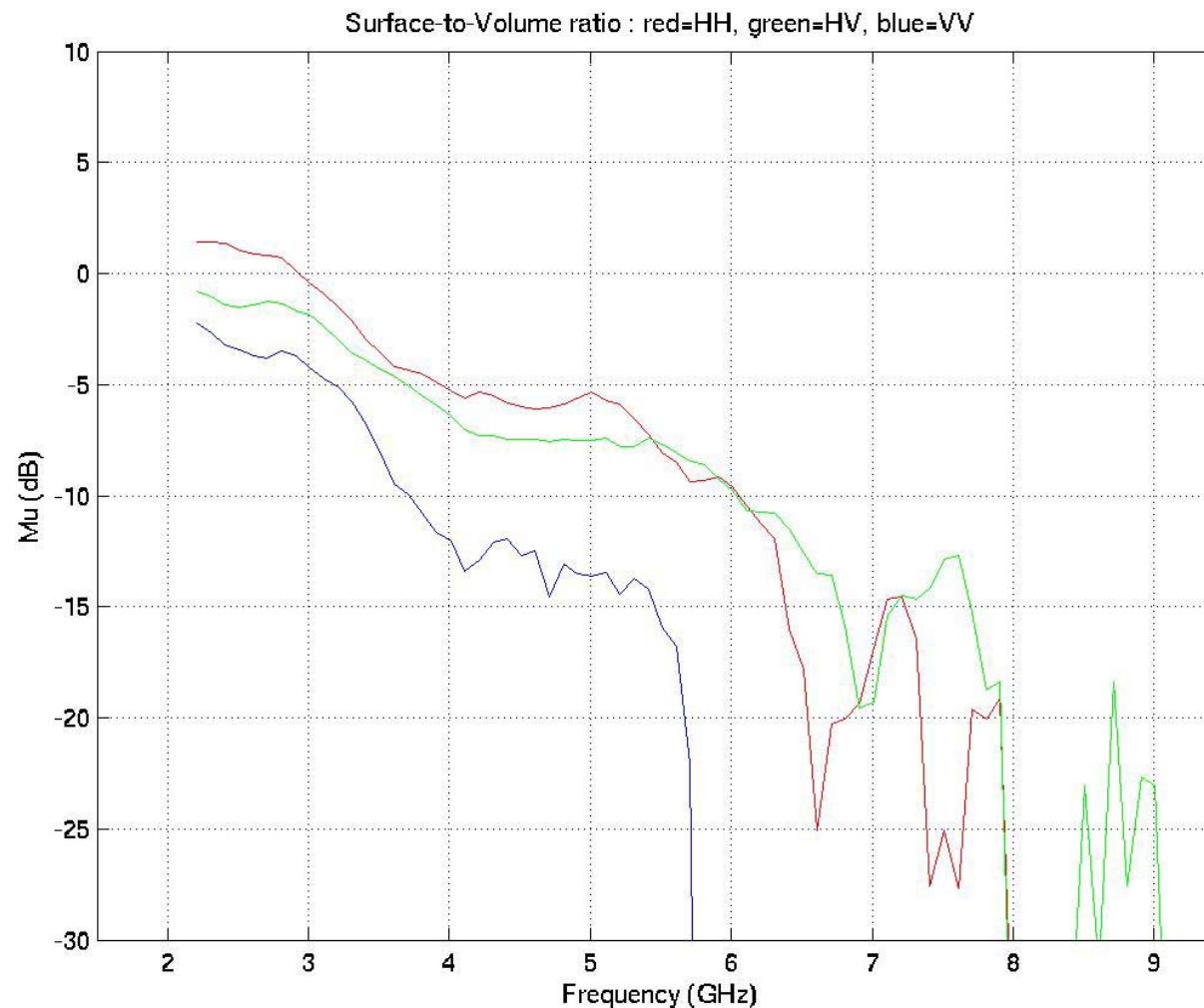


Complex coherence loci for 3 polarisations

Coherence Amplitude vs. Sinc Coherence Prediction

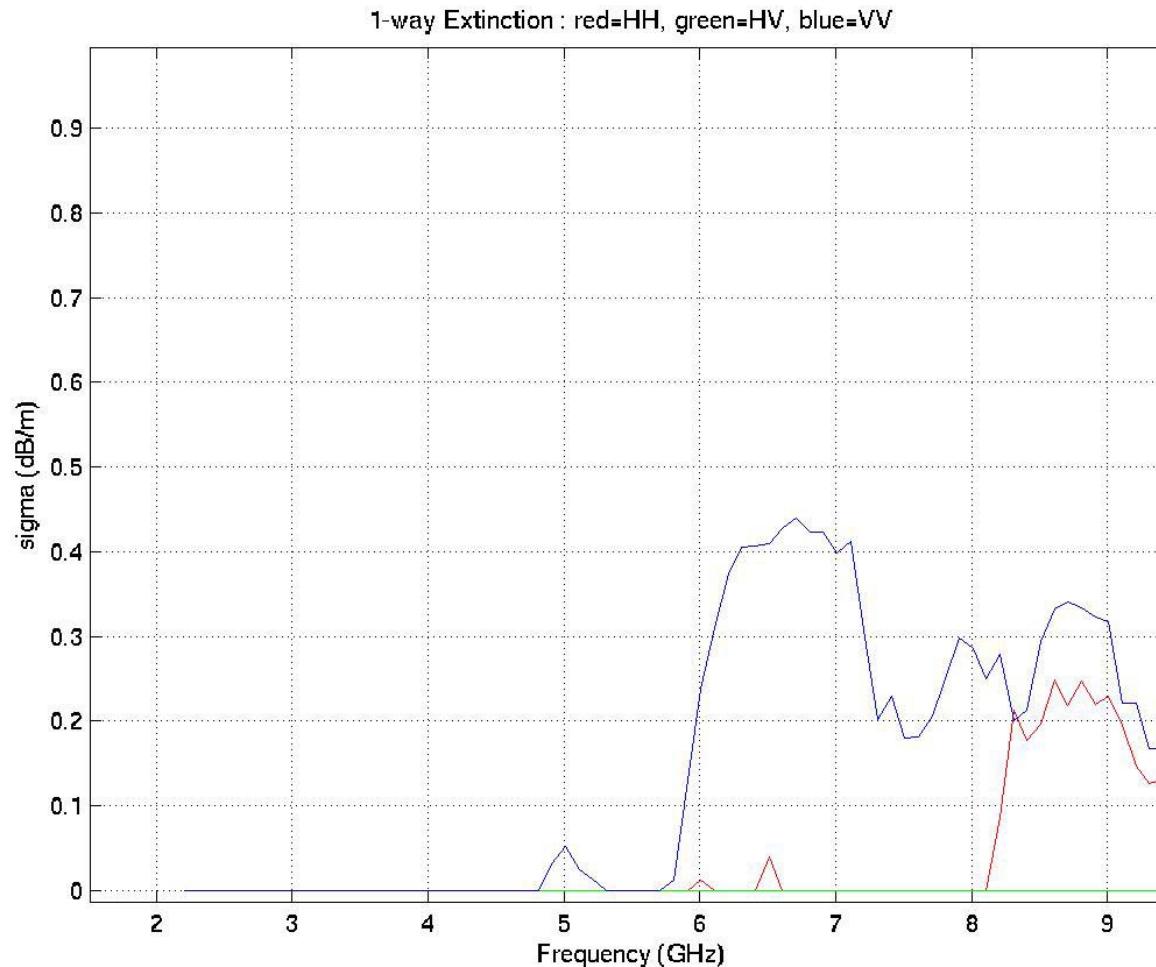


Estimate of μ vs Frequency



Can be used to help design air and space borne POLInSAR sensors
...e.g. Terrasar X, radarsat 2

Estimate of extinction vs Frequency

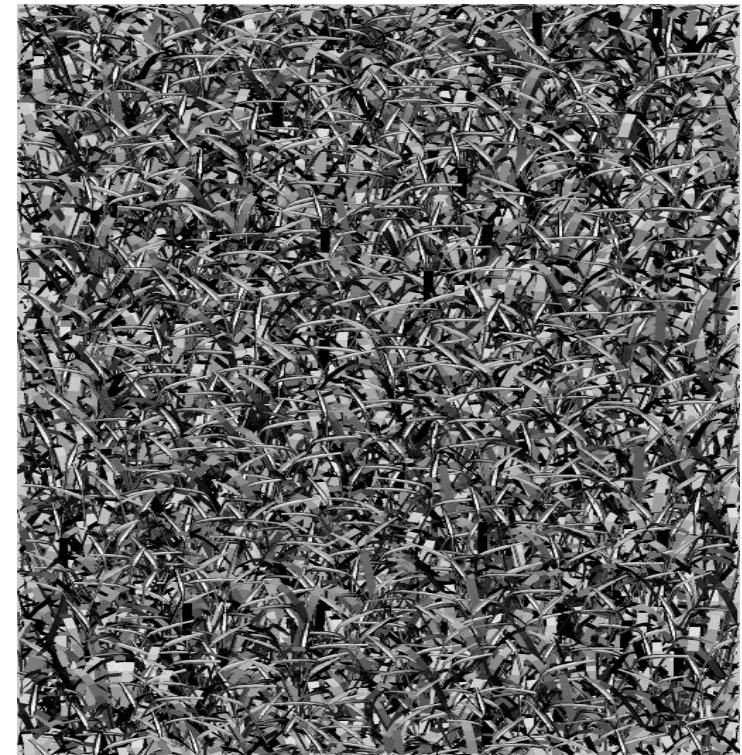
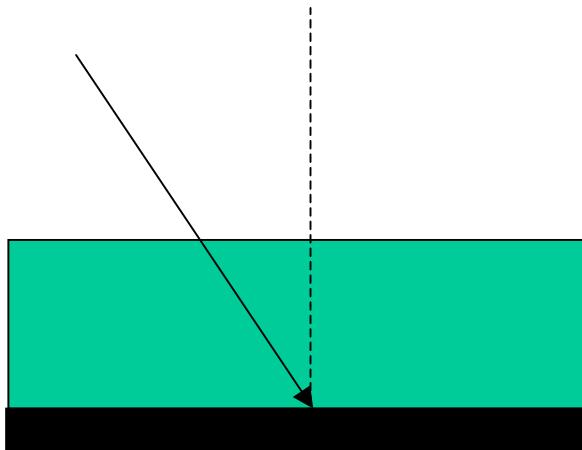


Can be used to select best frequency for studying vegetation effects

Simulated Wheat+Surface Scattering

Coherent wave propagation and scattering:

- Wave extinction
- Direct volume+
- Direct ground+
- Ground-volume and volume-ground+
- Ground-volume-ground..



DSTO Simulated GB-POLInSAR scene
(C-Band analysis
to be presented @ IGARSS 2005)

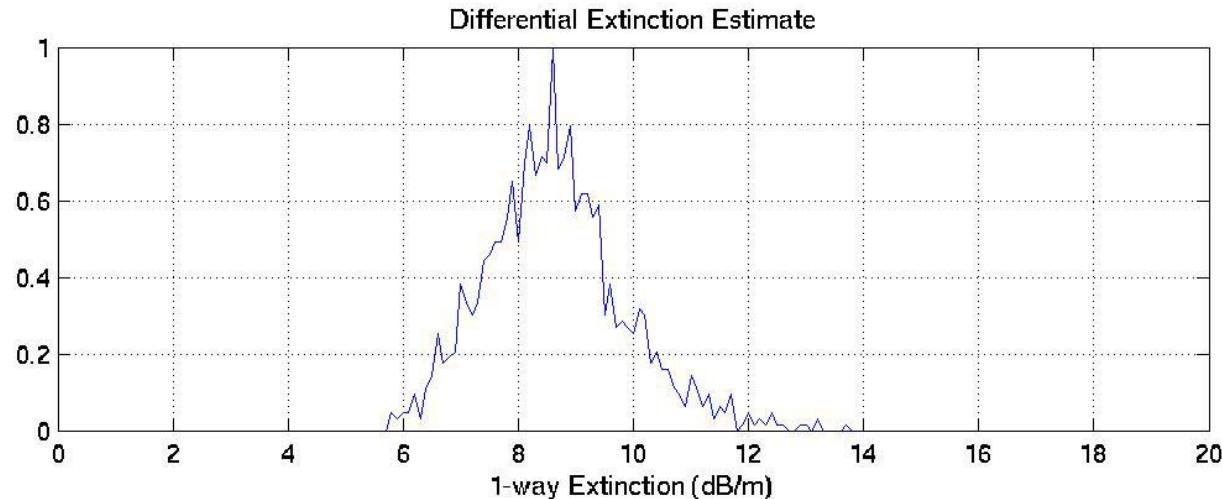
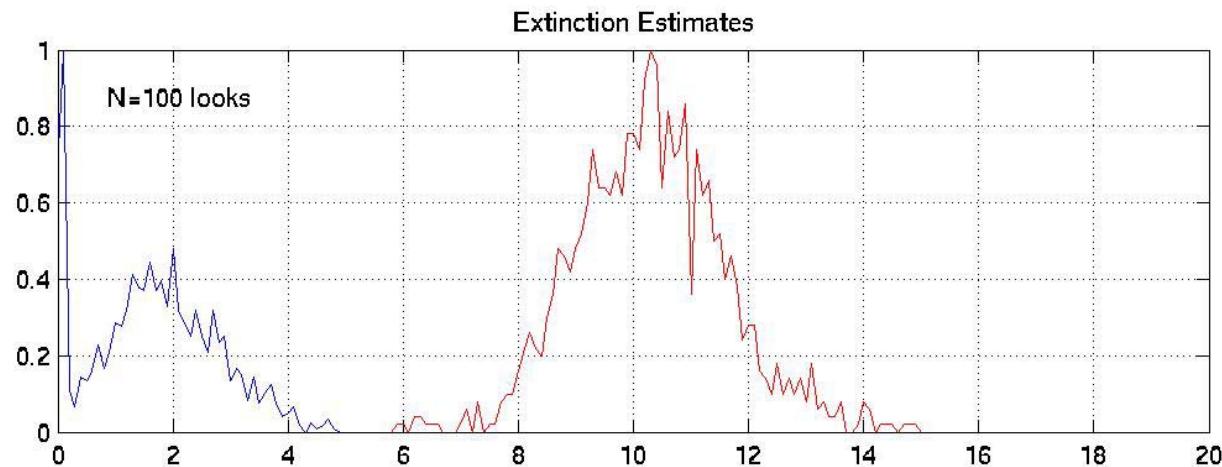
2 coherent models analysed:

Dr Pierre Borderies, ONERA, France

Dr Mark Williams, DSTO, Australia

Ovog Inversion

C-Band Wheat (PolInSAR Simulator)



Conclusions

- POLSAR phase is most useful in low entropy situations, where it can be used for improved ship detection, oil slick monitoring, littoral zone remote sensing
- Vegetation cover of land surfaces raises entropy...
reduces the impact of quantitative parameter estimation using polarimetry alone...
One solution is to employ radar interferometry ...user 'control' of vegetation entropy
- But single channel interferometry is underdetermined for vegetation cover
...multi-parameter interferometry is an important research topic
.. GB-SAR systems can help design 'best' parameter set...
- One example is polarimetric SAR interferometry ..POLInSAR
which is well suited to planned space-borne satellites (ALOS-PALSAR/Terrasar-L)
(single wavelength, single baseline...)
... but suffers from problems with temporal decorrelation in repeat pass systems
...well suited to single pass interferometer designs of the future...tandem/cartwheel etc.

Acknowledgements



QinetiQ



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Analysis of Polarimetric Interferometric
SAR data

ESA ESRIN Contract 17893/03/I-LG
PolarimetricInterferometric
Mission and Application Study